

Automatic Variable Selection

```
title2 'Automatic variable selection: Goal is to predict grade';
%include 'readmath.sas';
options pagesize=1000; /* Print fewer page headings */

/* The data step continues */
if ethnic ne 6;
if course ne 4; /* Otherwise, throw the case out */

/* Dummy variables for ethnic background */
if ethnic=. then e1=.;
  else if ethnic=1 then e1=1;
  else e1=0;
if ethnic=. then e2=.;
  else if ethnic=2 then e2=1;
  else e2=0;
if ethnic=. then e3=.;
  else if ethnic=3 then e3=1;
  else e3=0;
if ethnic=. then e4=.;
  else if ethnic=4 then e4=1;
  else e4=0;

/* Ethnic
      1 = 'Asian'
      2 = 'Eastern European'
      3 = 'European not Eastern'
      4 = 'Middle-Eastern and Pakistani'
      5 = 'East Indian'
      6 was deleted.
*/
label e1 = 'Asian vs East Ind.'
      e2 = 'East Eur. vs East Ind.'
      e3 = 'Other Eur. vs East Ind.'
      e4 = 'Mid. East & Pak. vs East Ind.';

if sex = 'Female' then gender=1; else if sex = 'Male' then gender=0;
if tongue = 'English' then mtongue=1; else if tongue='Other' then mtongue=0;

if course=. then c1=.; else if course=1 then c1=1; else c1=0;
if course=. then c2=.; else if course=2 then c2=1; else c2=0;

proc freq;
  title3 'Check dummy variables for course';
  tables (c1 c2) * course / norow nocol nopercnt missing;

proc stepwise;
  title3 'Forward selection';
  model grade = gender mtongue e1-e4
            hsgpa hscal hsenl
            c1 c2 precalc calc totscore
            / forward slentry=0.05;
            /* Default signif level for entry is 0.5 */
```

```

proc stepwise;
  title3 'Stepwise (mixed) selection';
  model grade = gender mtongue e1-e4
           hsgpa hscalc hsengl
           c1 c2 precalc calc totscore
           / stepwise slentry=0.05 slstay=0.05;
           /* Default slentry = slstay = 0.15 */

proc reg;
  title3 'Test English language variables together';
  model grade = hsgpa hscalc hsengl  totscore  mtongue;
  English: test hsengl=mtongue=0;

proc iml;
  title3 'Proportion of remaining variation';
  print "hsengl and mtongue controlling for hsgpa, hscalc, totscore";
  F = 6.80; s = 2; dfe = 274;      /* dfe = n-p */
  a = s*F / (dfe + s*F); print a;

```

Proc freq output, before adding if course ne 4;

Table of c1 by course

| c1 | course | | | | | | Total |
|-----------|--------|----|-----|----|---------|-----|-------|
| Frequency | . | 1 | 2 | 3 | No Resp | | |
| . | 79 | 0 | 0 | 0 | 0 | 79 | |
| 0 | 0 | 0 | 363 | 39 | 4 | 406 | |
| 1 | 0 | 54 | 0 | 0 | 0 | 54 | |
| Total | 79 | 54 | 363 | 39 | 4 | 539 | |

Table of c2 by course

| c2 | course | | | | | | Total |
|-----------|--------|----|-----|----|---------|-----|-------|
| Frequency | . | 1 | 2 | 3 | No Resp | | |
| . | 79 | 0 | 0 | 0 | 0 | 79 | |
| 0 | 0 | 54 | 0 | 39 | 4 | 97 | |
| 1 | 0 | 0 | 363 | 0 | 0 | 363 | |
| Total | 79 | 54 | 363 | 39 | 4 | 539 | |

Forward selection

The STEPWISE Procedure

Model: MODEL1

Dependent Variable: grade Final mark (if any)

| | |
|--|-----|
| Number of Observations Read | 535 |
| Number of Observations Used | 280 |
| Number of Observations with Missing Values | 255 |

Forward Selection: Step 1

Variable hsgpa Entered: R-Square = 0.3537 and C(p) = 57.2365

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 1 | 33894 | 33894 | 152.17 | <.0001 |
| Error | 278 | 61921 | 222.73759 | | |
| Corrected Total | 279 | 95815 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | -87.40438 | 12.04376 | 11731 | 52.67 | <.0001 |
| hsgpa | 1.82819 | 0.14820 | 33894 | 152.17 | <.0001 |

Bounds on condition number: 1, 1

Values of $C(p)$ are supposed to be better when they are small, and when they are close to p -- the number of regression coefficients.

Forward Selection: Step 2

Variable totscore Entered: R-Square = 0.4120 and C(p) = 29.2151

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 2 | 39473 | 19736 | 97.03 | <.0001 |
| Error | 277 | 56343 | 203.40270 | | |
| Corrected Total | 279 | 95815 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | -77.36795 | 11.66763 | 8943.62142 | 43.97 | <.0001 |
| hsgpa | 1.55985 | 0.15061 | 21819 | 107.27 | <.0001 |
| totscore | 1.32372 | 0.25276 | 5578.50005 | 27.43 | <.0001 |

Bounds on condition number: 1.1309, 4.5236

Forward Selection: Step 3

Variable hsengl Entered: R-Square = 0.4414 and C(p) = 16.0143

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 3 | 42297 | 14099 | 72.71 | <.0001 |
| Error | 276 | 53518 | 193.90578 | | |
| Corrected Total | 279 | 95815 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | -72.63764 | 11.45922 | 7791.20117 | 40.18 | <.0001 |
| hsgpa | 1.94884 | 0.17892 | 23006 | 118.65 | <.0001 |
| hsengl | -0.45289 | 0.11866 | 2824.55260 | 14.57 | 0.0002 |
| totscore | 1.17049 | 0.25004 | 4249.35806 | 21.91 | <.0001 |

Bounds on condition number: 1.6742, 12.964

Forward Selection: Step 4

Variable mtongue Entered: R-Square = 0.4530 and C(p) = 12.0592

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 4 | 43404 | 10851 | 56.93 | <.0001 |
| Error | 275 | 52411 | 190.58700 | | |
| Corrected Total | 279 | 95815 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | -68.15382 | 11.51212 | 6679.79905 | 35.05 | <.0001 |
| mtongue | -5.19142 | 2.15448 | 1106.57185 | 5.81 | 0.0166 |
| hsgpa | 1.88196 | 0.17954 | 20941 | 109.88 | <.0001 |
| hsengl | -0.38223 | 0.12124 | 1894.23591 | 9.94 | 0.0018 |
| totscore | 1.13240 | 0.24839 | 3961.19628 | 20.78 | <.0001 |

Bounds on condition number: 1.7152, 22.144

Forward Selection: Step 5

Variable hscalC Entered: R-Square = 0.4616 and C(p) = 9.6135

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 5 | 44230 | 8846.02865 | 46.99 | <.0001 |
| Error | 274 | 51585 | 188.26767 | | |
| Corrected Total | 279 | 95815 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | -66.74563 | 11.46159 | 6384.57537 | 33.91 | <.0001 |
| mtongue | -4.71674 | 2.15329 | 903.34525 | 4.80 | 0.0293 |
| hsgpa | 1.59500 | 0.22496 | 9464.04494 | 50.27 | <.0001 |
| hscalC | 0.21769 | 0.10392 | 826.08202 | 4.39 | 0.0371 |
| hsengl | -0.30921 | 0.12544 | 1143.87785 | 6.08 | 0.0143 |
| totscore | 0.98959 | 0.25612 | 2810.72834 | 14.93 | 0.0001 |

Bounds on condition number: 2.726, 44.206

No other variable met the 0.0500 significance level for entry into the model.

Summary of Forward Selection

| Step | Variable Entered | Label | Number Vars In | Partial R-Square | Model R-Square |
|------|------------------|----------------------------------|----------------|------------------|----------------|
| 1 | hsgpa | High School GPA | 1 | 0.3537 | 0.3537 |
| 2 | totscore | Total # right on diagnostic test | 2 | 0.0582 | 0.4120 |
| 3 | hsengl | HS English | 3 | 0.0295 | 0.4414 |
| 4 | mtongue | | 4 | 0.0115 | 0.4530 |
| 5 | hscal | HS Calculus | 5 | 0.0086 | 0.4616 |

Summary of Forward Selection

| Step | C(p) | F Value | Pr > F |
|------|---------|---------|--------|
| 1 | 57.2365 | 152.17 | <.0001 |
| 2 | 29.2151 | 27.43 | <.0001 |
| 3 | 16.0143 | 14.57 | 0.0002 |
| 4 | 12.0592 | 5.81 | 0.0166 |
| 5 | 9.6135 | 4.39 | 0.0371 |

Mixed forward and backwards selection gave exactly the same results we've just seen, because no variables were removed. Output has been deleted.

Gender, Ethnicity and Math performance

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Test English language variables together

The REG Procedure

Model: MODEL1

Dependent Variable: grade Final mark (if any)

| | |
|--|-----|
| Number of Observations Read | 535 |
| Number of Observations Used | 280 |
| Number of Observations with Missing Values | 255 |

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 5 | 44230 | 8846.02865 | 46.99 | <.0001 |
| Error | 274 | 51585 | 188.26767 | | |
| Corrected Total | 279 | 95815 | | | |

| | | | |
|----------------|----------|----------|--------|
| Root MSE | 13.72107 | R-Square | 0.4616 |
| Dependent Mean | 60.75714 | Adj R-Sq | 0.4518 |
| Coeff Var | 22.58346 | | |

Parameter Estimates

| Variable | Label | DF | Parameter Estimate | Standard Error |
|-----------|----------------------------------|----|--------------------|----------------|
| Intercept | Intercept | 1 | -66.74563 | 11.46159 |
| hsgpa | High School GPA | 1 | 1.59500 | 0.22496 |
| hscal | HS Calculus | 1 | 0.21769 | 0.10392 |
| hsengl | HS English | 1 | -0.30921 | 0.12544 |
| totscore | Total # right on diagnostic test | 1 | 0.98959 | 0.25612 |
| mtongue | | 1 | -4.71674 | 2.15329 |

Parameter Estimates

| Variable | Label | DF | t Value | Pr > t |
|-----------|----------------------------------|----|---------|---------|
| Intercept | Intercept | 1 | -5.82 | <.0001 |
| hsgpa | High School GPA | 1 | 7.09 | <.0001 |
| hscal | HS Calculus | 1 | 2.09 | 0.0371 |
| hsengl | HS English | 1 | -2.46 | 0.0143 |
| totscore | Total # right on diagnostic test | 1 | 3.86 | 0.0001 |
| mtongue | | 1 | -2.19 | 0.0293 |

Gender, Ethnicity and Math performance

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Test English language variables together

The REG Procedure

Model: MODEL1

Test English Results for Dependent Variable grade

| Source | DF | Mean Square | F Value | Pr > F |
|-------------|-----|----------------|---------|--------|
| Numerator | 2 | 1280.91501 | 6.80 | 0.0013 |
| Denominator | 274 | 188.26767 | | |

Gender, Ethnicity and Math performance

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Proportion of remaining variation

hsengl and mtongue controlling for hsgpa, hscal, totscore

a

0.0472879