Student Number \_\_\_\_\_

## STA 431 Quiz 9

1. Let

$$z_1 = \lambda_1 F_1 + \lambda_2 F_2 + \lambda_3 F_3 + e_1$$
  

$$z_2 = \lambda_4 F_1 + \lambda_5 F_2 + \lambda_6 F_3 + e_2$$

where all expected values are zero, variances of the factors equal one, and all the factors and error terms are independent. As the notation suggests,  $Var(z_1) = Var(z_2) = 1$ . Only  $z_1$  and  $z_2$  are observable. Please give Greek letter answers to the following.

(a) (2 points) What is  $Var(e_1)$ ? Show a bit of work. Circle your answer.

(b) (1 point) What is  $Corr(z_1, F_3)$ ? Show a bit of work.

(c) (1 point) What is the reliability of  $z_1$  as a measurement of  $F_1$ ? Just write down the answer.

(d) (2 points) What is the reliability of  $s = z_1 + z_2$  as a measurement of  $F_1$ ? Show your work. Circle your answer.

- 2. For the R part of the assignment (last question), you fit a 4-factor model to the statclass data.
  - (a) (2 points) What is the estimated correlation between Factor 2 and mark on Computer Assignment 5? The answer is a number from your printout. Write the answer in the space below. Circle the number on your printout, and write "Q2a" beside it.
  - (b) (2 points) What estimated proportion of the variance of the Midterm is explained by the common factors? The answer is a number from your printout. *Write the answer in the space below.* Circle the number on your printout, and write "Q2b" beside it.

Please attach your printout to the quiz paper. The printout should show your *complete* **R input and output.** Make sure your name and student number appear on the printout.