

Time Series analysis of Experimental data

```
% cat expseries.data
1 1 11.64
2 1 11.83
3 1 11.69
4 1 10.08
```

Skipping ...

```
148 3 10.48
149 3 8.89
150 3 8.71
```

```
/* expseries.sas */
options nodate linesize=79 noovp formdlim=' ';
title 'Experimental data with autocorrelated errors';
```

```
data test;
  infile 'expseries.data';
  input time group y;
  if group=1 then g1=1; else g1=0;
  if group=2 then g2=1; else g2=0;
```

```
proc glm;
  class group;
  model y = group;
  means group;
```

```
proc reg;
  model y = g1 g2 / dw;
  output out=test2 residual = e;
```

```
proc arima;
  identify var = e;
```

```
proc autoreg;
  model y = g1 g2 / nlag=1 method = ml;
  group: test g1=g2=0;
```

Experimental data with autocorrelated errors

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The GLM Procedure

Class Level Information

| Class | Levels | Values |
|-------|--------|--------|
| group | 3 | 1 2 3 |

Number of observations 150

Experimental data with autocorrelated errors

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The GLM Procedure

Dependent Variable: y

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 2 | 6.5766093 | 3.2883047 | 4.18 | 0.0171 |
| Error | 147 | 115.5570740 | 0.7861025 | | |
| Corrected Total | 149 | 122.1336833 | | | |

| R-Square | Coeff Var | Root MSE | y Mean |
|----------|-----------|----------|----------|
| 0.053848 | 9.098870 | 0.886624 | 9.744333 |

| Source | DF | Type I SS | Mean Square | F Value | Pr > F |
|--------|----|------------|-------------|---------|--------|
| group | 2 | 6.57660933 | 3.28830467 | 4.18 | 0.0171 |

| Source | DF | Type III SS | Mean Square | F Value | Pr > F |
|--------|----|-------------|-------------|---------|--------|
| group | 2 | 6.57660933 | 3.28830467 | 4.18 | 0.0171 |

Experimental data with autocorrelated errors

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The GLM Procedure

| Level of group | N | Mean | Std Dev |
|----------------|----|------------|------------|
| 1 | 50 | 9.45360000 | 1.06639151 |
| 2 | 50 | 9.93840000 | 0.74053307 |
| 3 | 50 | 9.84100000 | 0.82019970 |

Experimental data with autocorrelated errors

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The REG Procedure

Model: MODEL1

Dependent Variable: y

Analysis of Variance

| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
|-----------------|-----|----------------|-------------|---------|--------|
| Model | 2 | 6.57661 | 3.28830 | 4.18 | 0.0171 |
| Error | 147 | 115.55707 | 0.78610 | | |
| Corrected Total | 149 | 122.13368 | | | |

| | | | |
|----------------|---------|----------|--------|
| Root MSE | 0.88662 | R-Square | 0.0538 |
| Dependent Mean | 9.74433 | Adj R-Sq | 0.0410 |
| Coeff Var | 9.09887 | | |

Parameter Estimates

| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
|-----------|----|--------------------|----------------|---------|---------|
| Intercept | 1 | 9.84100 | 0.12539 | 78.48 | <.0001 |
| g1 | 1 | -0.38740 | 0.17732 | -2.18 | 0.0305 |
| g2 | 1 | 0.09740 | 0.17732 | 0.55 | 0.5837 |

Experimental data with autocorrelated errors

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The REG Procedure

Model: MODEL1

Dependent Variable: y

| | |
|---------------------------|-------|
| Durbin-Watson D | 0.464 |
| Number of Observations | 150 |
| 1st Order Autocorrelation | 0.742 |

The ARIMA Procedure

Name of Variable = e

Mean of Working Series -134E-17
 Standard Deviation 0.877713
 Number of Observations 150

Autocorrelations

| Lag | Covariance | Correlation | -1 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | | |
|-----|------------|-------------|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|
| 0 | 0.770380 | 1.00000 | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0.571561 | 0.74192 | | | | | | | | | | . | | | | | | | | | | | | | |
| 2 | 0.395913 | 0.51392 | | | | | | | | | . | | | | | | | | | | | | | | |
| 3 | 0.258485 | 0.33553 | | | | | | | | | . | | | | | | | | | | | | | | |
| 4 | 0.204559 | 0.26553 | | | | | | | | | . | | | | | | | | | | | | | | |
| 5 | 0.128356 | 0.16661 | | | | | | | | | . | | | | | | | | | | | | | | |
| 6 | 0.061202 | 0.07944 | | | | | | | | | . | | | | | | | | | | | | | | |
| 7 | 0.026507 | 0.03441 | | | | | | | | | . | | | | | | | | | | | | | | |
| 8 | 0.023097 | 0.02998 | | | | | | | | | . | | | | | | | | | | | | | | |
| 9 | 0.080783 | 0.10486 | | | | | | | | | . | | | | | | | | | | | | | | |
| 10 | 0.090297 | 0.11721 | | | | | | | | | . | | | | | | | | | | | | | | |
| 11 | 0.094371 | 0.12250 | | | | | | | | | . | | | | | | | | | | | | | | |
| 12 | 0.096083 | 0.12472 | | | | | | | | | . | | | | | | | | | | | | | | |
| 13 | 0.104496 | 0.13564 | | | | | | | | | . | | | | | | | | | | | | | | |
| 14 | 0.073087 | 0.09487 | | | | | | | | | . | | | | | | | | | | | | | | |
| 15 | 0.059903 | 0.07776 | | | | | | | | | . | | | | | | | | | | | | | | |
| 16 | 0.071046 | 0.09222 | | | | | | | | | . | | | | | | | | | | | | | | |
| 17 | 0.027189 | 0.03529 | | | | | | | | | . | | | | | | | | | | | | | | |
| 18 | -0.0037552 | -.00487 | | | | | | | | | . | | | | | | | | | | | | | | |
| 19 | -0.042520 | -.05519 | | | | | | | | | . | * | | | | | | | | | | | | | |
| 20 | -0.046061 | -.05979 | | | | | | | | | . | * | | | | | | | | | | | | | |
| 21 | -0.035253 | -.04576 | | | | | | | | | . | * | | | | | | | | | | | | | |
| 22 | -0.039347 | -.05107 | | | | | | | | | . | * | | | | | | | | | | | | | |
| 23 | -0.029089 | -.03776 | | | | | | | | | . | * | | | | | | | | | | | | | |
| 24 | -0.032854 | -.04265 | | | | | | | | | . | * | | | | | | | | | | | | | |

"." marks two standard errors

Partial Autocorrelations

| Lag | Correlation | -1 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 |
|-----|-------------|----|---|---|---|---|---|---|---|------|---|---|-------|---|---|---|---|---|---|---|---|---|
| 1 | 0.74192 | | | | | | | | | | . | | ***** | | | | | | | | | |
| 2 | -0.08125 | | | | | | | | | . ** | | | . | | | | | | | | | |
| 3 | -0.03685 | | | | | | | | | . * | | | . | | | | | | | | | |
| 4 | 0.11498 | | | | | | | | | . | | | **. | | | | | | | | | |
| 5 | -0.11479 | | | | | | | | | . ** | | | . | | | | | | | | | |
| 6 | -0.03894 | | | | | | | | | . * | | | . | | | | | | | | | |
| 7 | 0.04243 | | | | | | | | | . | | | * | | | | | | | | | |
| 8 | 0.01823 | | | | | | | | | . | | | . | | | | | | | | | |
| 9 | 0.17710 | | | | | | | | | . | | | **** | | | | | | | | | |
| 10 | -0.06309 | | | | | | | | | . * | | | . | | | | | | | | | |
| 11 | 0.02322 | | | | | | | | | . | | | . | | | | | | | | | |
| 12 | 0.05470 | | | | | | | | | . | | | * | | | | | | | | | |
| 13 | -0.01641 | | | | | | | | | . | | | . | | | | | | | | | |
| 14 | -0.06735 | | | | | | | | | . * | | | . | | | | | | | | | |
| 15 | 0.06857 | | | | | | | | | . | | | * | | | | | | | | | |
| 16 | 0.06780 | | | | | | | | | . | | | * | | | | | | | | | |
| 17 | -0.15710 | | | | | | | | | *** | | | . | | | | | | | | | |
| 18 | 0.01457 | | | | | | | | | . | | | . | | | | | | | | | |
| 19 | -0.04774 | | | | | | | | | . * | | | . | | | | | | | | | |
| 20 | -0.00633 | | | | | | | | | . | | | . | | | | | | | | | |
| 21 | 0.05326 | | | | | | | | | . | | | * | | | | | | | | | |
| 22 | -0.08965 | | | | | | | | | . ** | | | . | | | | | | | | | |
| 23 | 0.08299 | | | | | | | | | . | | | **. | | | | | | | | | |
| 24 | -0.04418 | | | | | | | | | . * | | | . | | | | | | | | | |

Experimental data with autocorrelated errors

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The ARIMA Procedure

Autocorrelation Check for White Noise

| To Lag | Chi-Square | DF | Pr > ChiSq | -----Autocorrelations----- | | | | | |
|--------|------------|----|------------|----------------------------|--------|--------|--------|--------|--------|
| 6 | 158.75 | 6 | <.0001 | 0.742 | 0.514 | 0.336 | 0.266 | 0.167 | 0.079 |
| 12 | 168.13 | 12 | <.0001 | 0.034 | 0.030 | 0.105 | 0.117 | 0.122 | 0.125 |
| 18 | 175.39 | 18 | <.0001 | 0.136 | 0.095 | 0.078 | 0.092 | 0.035 | -0.005 |
| 24 | 177.97 | 24 | <.0001 | -0.055 | -0.060 | -0.046 | -0.051 | -0.038 | -0.043 |

The AUTOREG Procedure

Dependent Variable y

Ordinary Least Squares Estimates

| | | | |
|------------------|------------|----------------|------------|
| SSE | 115.557074 | DFE | 147 |
| MSE | 0.78610 | Root MSE | 0.88662 |
| SBC | 401.582855 | AIC | 392.550949 |
| Regress R-Square | 0.0538 | Total R-Square | 0.0538 |
| Durbin-Watson | 0.4637 | | |

| Variable | DF | Estimate | Standard Error | t Value | Approx Pr > t |
|-----------|----|----------|----------------|---------|----------------|
| Intercept | 1 | 9.8410 | 0.1254 | 78.48 | <.0001 |
| g1 | 1 | -0.3874 | 0.1773 | -2.18 | 0.0305 |
| g2 | 1 | 0.0974 | 0.1773 | 0.55 | 0.5837 |

Test GROUP

| Source | DF | Mean Square | F Value | Pr > F |
|-------------|-----|-------------|---------|--------|
| Numerator | 2 | 3.288305 | 4.18 | 0.0171 |
| Denominator | 147 | 0.786103 | | |

Estimates of Autocorrelations

| Lag | Covariance | Correlation | -1 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 |
|-----|------------|-------------|----|---|---|---|---|---|---|---|---|---|---|-------|---|---|---|---|---|---|---|---|---|
| 0 | 0.7704 | 1.000000 | | | | | | | | | | | | ***** | | | | | | | | | |
| 1 | 0.5716 | 0.741920 | | | | | | | | | | | | ***** | | | | | | | | | |

Preliminary MSE 0.3463

Estimates of Autoregressive Parameters

| Lag | Coefficient | Standard Error | t Value |
|-----|-------------|----------------|---------|
| 1 | -0.741920 | 0.055490 | -13.37 |

Algorithm converged.

The AUTOREG Procedure

Maximum Likelihood Estimates

| | | | |
|------------------|------------|----------------|------------|
| SSE | 48.2614905 | DFE | 146 |
| MSE | 0.33056 | Root MSE | 0.57494 |
| SBC | 276.561592 | AIC | 264.519051 |
| Regress R-Square | 0.0023 | Total R-Square | 0.6048 |
| Durbin-Watson | 1.8478 | | |

| Variable | DF | Estimate | Standard Error | t Value | Approx Pr > t |
|-----------|----|-----------|----------------|---------|----------------|
| Intercept | 1 | 9.8353 | 0.3211 | 30.63 | <.0001 |
| g1 | 1 | -0.2100 | 0.4430 | -0.47 | 0.6363 |
| g2 | 1 | 0.0000922 | 0.3899 | 0.00 | 0.9998 |
| AR1 | 1 | -0.7800 | 0.0520 | -15.01 | <.0001 |

Test GROUP

| Source | DF | Mean Square | F Value | Pr > F |
|-------------|-----|-------------|---------|--------|
| Numerator | 2 | 0.054820 | 0.17 | 0.8473 |
| Denominator | 146 | 0.330558 | | |

Autoregressive parameters assumed given.

| Variable | DF | Estimate | Standard Error | t Value | Approx Pr > t |
|-----------|----|-----------|----------------|---------|----------------|
| Intercept | 1 | 9.8353 | 0.3209 | 30.65 | <.0001 |
| g1 | 1 | -0.2100 | 0.4429 | -0.47 | 0.6361 |
| g2 | 1 | 0.0000922 | 0.3899 | 0.00 | 0.9998 |