## Handout 1.5: Proportion of remaining variation for the Grades data

```
/********************** grades2.sas ***********************************
options linesize=79 noovp formdlim=' ';
title 'Predicting First-Year GPA from SAT Scores';
title2 'Test quadratic terms, calculate explained variation';
data sat;
    infile 'grades.data' firstobs=2 ; /* Skipping the header on line 1 */
    input id verbal math gpa;
    sat = verbal+math;
    v2 = verbal**2;
    m2 = math**2;
    label gpa = 'First-year GPA'
            sat = 'Total SAT score'
            v2 = 'Verbal Squared'
            m2 = 'Math Squared';
proc reg;
    model gpa = verbal v2 math m2;
    V2andM2: test v2=m2=0; /* Meaning: Test this null hypothesis about the
                corresponding regression coefficients */
/* Calculate proportion of remaining variation with proc iml. First do the
contribution of v2 and m2, in two ways. The model with just verbal and math
had an R-squared of 0.116054 (from grades.lst). With verbal-squared and
math-squared, get R-squared = 0.1408 */
proc iml;
    title3 'Calculate explained variation 2 ways';
    print "Proportion of remaining variation explained by V2 and M2";
    a1 = (0.1408-0.116054)/(1-0.116054); print al;
    /* Now the formula based on the F statistic*/
    n = 200 ; p = 5 ; s=2 ; F = 2.81;
    a2 = s*f / (n - p + s*F); print a2;
/* Controlling for the other variables, what proportion of the remaining
variation does verbal explain? For a test of one variable, F = t-squared. */
proc iml;
    title3 'Proportion of remaining variation from a t statistic';
    print "Proportion of remaining variation explained by verbal";
    T = 2.13; F = T**2;
    n = 200 ; p = 5 ; s = 1 ;
    a = s*f / (n - p + s*F); print a;
```


## grades2.lst

Predicting First-Year GPA from SAT Scores
Test quadratic terms, calculate explained variation
22:08 Sunday, October 7, 2007

|  | ```The REG Procedure Model: MODEL1 Dependent Variable: gpa First-year GPA Analysis of Variance``` |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | DF | Sum of Squares | Mean Square | F | Value | $\mathrm{Pr}>\mathrm{F}$ |
| Model | 4 | 9.43549 | 2.35887 |  | 7.99 | <. 0001 |
| Error | 195 | 57.58451 | 0.29531 |  |  |  |
| Corrected Total | 199 | 67.02000 |  |  |  |  |


| Root MSE | 0.54342 | R-Square | 0.1408 |
| :--- | ---: | :--- | :--- |
| Dependent Mean | 2.63000 | Adj R-Sq | 0.1232 |
| Coeff Var | 20.66235 |  |  |


| Variable | Parameter Estimates |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Label | DF | Parameter Estimate | Standard Error | t Value | $\operatorname{Pr}>\|t\|$ |
| Intercept | Intercept | 1 | 1.71058 | 3.08521 | 0.55 | 0.5799 |
| verbal |  | 1 | 0.01310 | 0.00614 | 2.13 | 0.0341 |
| v2 | Verbal Squared | 1 | -0.00000912 | 0.00000515 | -1.77 | 0.0783 |
| math |  | 1 | -0.01247 | 0.00806 | -1.55 | 0.1235 |
| m2 | Math Squared | 1 | 0.00001056 | 0.00000625 | 1.69 | 0.0926 |

Predicting First-Year GPA from SAT Scores
Test quadratic terms, calculate explained variation
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The REG Procedure
Model: MODEL1
Test V2andM2 Results for Dependent Variable gpa

| Source | DF | Mean <br> Square | F Value | Pr $>$ F |
| :--- | ---: | ---: | :---: | :---: |
| Numerator | 2 | 0.82878 | 2.81 | 0.0629 |
| Denominator | 195 | 0.29531 |  |  |

Predicting First-Year GPA from SAT Scores

Proportion of remaining variation explained by V2 and M2

## A1

### 0.0279949

A2
0.0280132
/dos/brunner/429f07/grades > sas grades2 ; cat grades2.lst ; chk

Predicting First-Year GPA from SAT Scores
Test quadratic terms, calculate explained variation
22:12 Sunday, October 7, 2007

|  | ```The REG Procedure Model: MODEL1 Dependent Variable: gpa First-year GPA Analysis of Variance``` |  |  | F |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | DF | Sum of Squares | Mean Square |  | Value | $\mathrm{Pr}>\mathrm{F}$ |
| Model | 4 | 9.43549 | 2.35887 |  | 7.99 | <.0001 |
| Error | 195 | 57.58451 | 0.29531 |  |  |  |
| Corrected Total | 199 | 67.02000 |  |  |  |  |


| Root MSE | 0.54342 | R-Square | 0.1408 |
| :--- | ---: | :--- | :--- |
| Dependent Mean | 2.63000 | Adj R-Sq | 0.1232 |
| Coeff Var | 20.66235 |  |  |


| Variable | Parameter Estimates |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Label | DF | Parameter Estimate | Standard Error | t Value | $\operatorname{Pr}>\|t\|$ |
| Intercept | Intercept | 1 | 1.71058 | 3.08521 | 0.55 | 0.5799 |
| verbal |  | 1 | 0.01310 | 0.00614 | 2.13 | 0.0341 |
| v2 | Verbal Squared | 1 | -0.00000912 | 0.00000515 | -1.77 | 0.0783 |
| math |  | 1 | -0.01247 | 0.00806 | -1.55 | 0.1235 |
| m2 | Math Squared | 1 | 0.00001056 | 0.00000625 | 1.69 | 0.0926 |

Test quadratic terms, calculate explained variation
22:12 Sunday, October 7, 2007
The REG Procedure
Model: MODEL1
Test V2andM2 Results for Dependent Variable gpa

| Source | Mean <br> SF |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
| Sumare | F Value | Pr $>$ F |  |  |
| Numerator | 2 | 0.82878 | 2.81 | 0.0629 |
| Denominator | 195 | 0.29531 |  |  |

Predicting First-Year GPA from SAT Scores
Test quadratic terms, calculate explained variation Calculate explained variation 2 ways 22:12 Sunday, October 7, 2007

Proportion of remaining variation explained by V2 and M2

A1
0.0279949

A2
0.0280132

Predicting First-Year GPA from SAT Scores
Test quadratic terms, calculate explained variation
Proportion of remaining variation from a $t$ statistic
22:12 Sunday, October 7, 2007
Proportion of remaining variation explained by verbal

A
0.0227371

