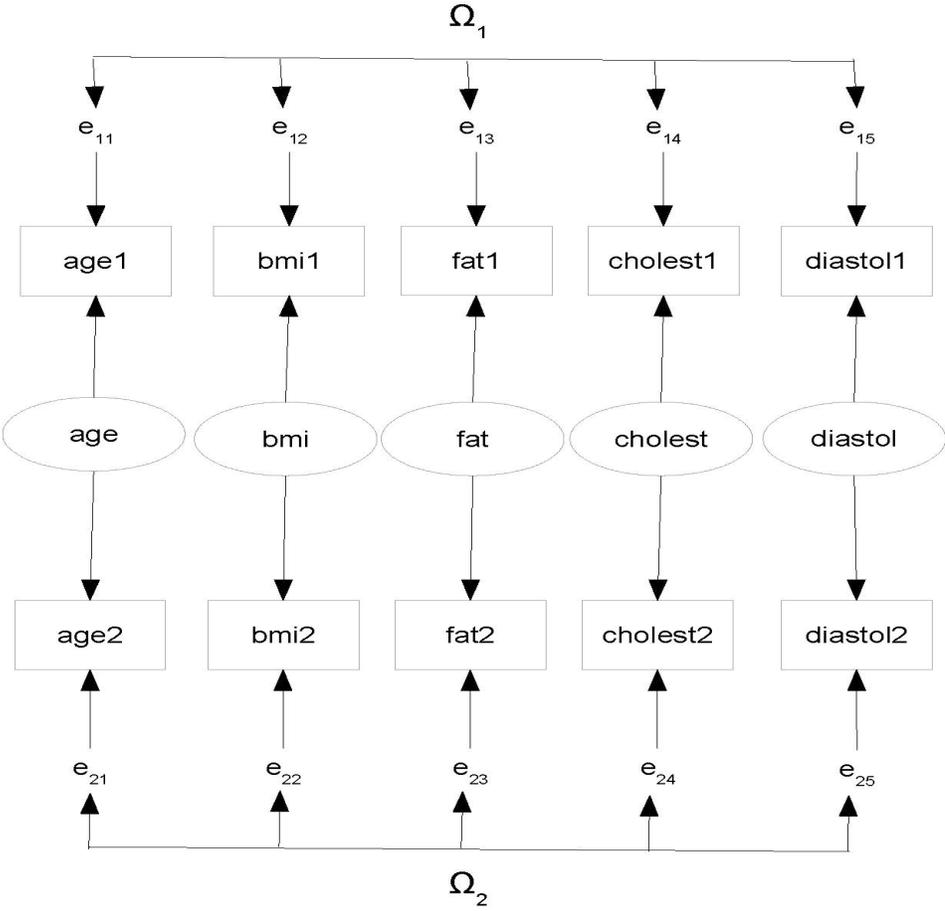
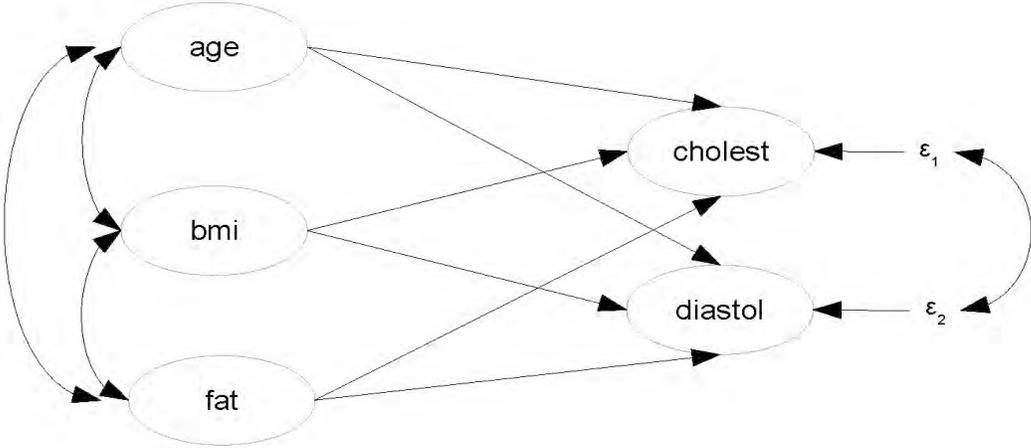


The BMI Health Study



```

> rm(list=ls()); options(scipen=999)
> bmidata =
read.table("http://www.utstat.toronto.edu/~brunner/openSEM/data/bmi.data.txt")
>
> head(bmidata)
  age1 bmi1 fat1 cholest1 diastol1 age2 bmi2 fat2 cholest2 diastol2
1   63 24.5 16.5   195.4      38   60 23.9 20.1   203.5      66
2   42 13.0  1.9   184.3      86   44 14.8  2.6   197.3      78
3   32 22.5 14.6   354.1     104   33 21.7 20.4   374.3      73
4   59 25.5 19.0   214.6      93   58 28.5 20.0   203.7     106
5   45 26.5 17.8   324.8      97   43 25.0 12.3   329.7      92
6   31 19.4 17.1   280.7      92   42 19.9 19.9   276.7      87
> dim(bmidata)
[1] 500 10
>
> #####
> # Naive surface regression      #
> #####
>
> bmi = within(bmidata,{
+ age = (age1+age2)/2; bmi = (bmi1+bmi2)/2; fat = (fat1+fat2)/2
+ cholest = (cholest1+cholest2)/2; diastol = (diastol1+diastol2)/2
+ })
> dim(bmi)
[1] 500 15
> fullmod = lm( cbind(cholest,diastol) ~ age + fat + bmi, data=bmi)
> summary(fullmod)
Response cholest :

Call:
lm(formula = cholest ~ age + fat + bmi, data = bmi)

Residuals:
    Min       1Q   Median       3Q      Max
-148.550  -34.243   2.626   33.661  165.582

Coefficients:
            Estimate Std. Error t value      Pr(>|t|)
(Intercept) 220.0610    21.0109  10.474 < 0.0000000000000002 ***
age          -0.2714     0.2002  -1.356    0.17578
fat           2.2334     0.5792   3.856    0.00013 ***
bmi           0.5164     1.0154   0.509    0.61128
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 52.43 on 496 degrees of freedom
Multiple R-squared:  0.09701, Adjusted R-squared:  0.09155
F-statistic: 17.76 on 3 and 496 DF,  p-value: 0.00000000005762

Response diastol :

Call:
lm(formula = diastol ~ age + fat + bmi, data = bmi)

Residuals:
    Min       1Q   Median       3Q      Max
 -44.841  -7.140  -0.408   7.612  41.377

Coefficients:
            Estimate Std. Error t value      Pr(>|t|)
(Intercept) 49.69194    4.52512  10.981 < 0.0000000000000002 ***
age           0.12648     0.04311   2.934    0.003504 **
fat           0.64056     0.12474   5.135    0.000000406 ***
bmi           0.82627     0.21869   3.778    0.000177 ***

```

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 11.29 on 496 degrees of freedom
Multiple R-squared:  0.3333, Adjusted R-squared:  0.3293
F-statistic: 82.67 on 3 and 496 DF,  p-value: < 0.000000000000000022
>
> restrictedmod = update(fullmod, . ~ . - bmi) # Remove var(s) being tested
> anova(fullmod,restrictedmod) # Gives multivariate test.
Analysis of Variance Table

Model 1: cbind(cholest, diastol) ~ age + fat + bmi
Model 2: cbind(cholest, diastol) ~ age + fat
  Res.Df Df Gen.var.  Pillai approx F num Df den Df    Pr(>F)
1     496     591.89
2     497  1  599.36 0.02869    7.3106      2    495 0.0007431 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

>
> #####
> # Structural equation model      #
> #####
> # install.packages("lavaan", dependencies = TRUE) # Only need to do this once
> library(lavaan)
This is lavaan 0.6-11
lavaan is FREE software! Please report any bugs.
>

```

```

bmimodel1 =
#####
# Latent variable model
# -----
'Lcholest ~ beta11*Lage + beta12*Lbmi + beta13*Lfat
Ldiastol ~ beta21*Lage + beta22*Lbmi + beta23*Lfat
#
# Measurement model
# -----
Lage =~ 1*age1 + 1*age2
Lbmi =~ 1*bmi1 + 1*bmi2
Lfat =~ 1*fat1 +1*fat2
Lcholest =~ 1*cholest1 + 1*cholest2
Ldiastol =~ 1*diastol1 + 1*diastol2
#
# Variances and covariances
# -----
# Of latent explanatory variables
Lage ~~ phi11*Lage; Lage ~~ phi12*Lbmi; Lage ~~ phi13*Lfat
Lbmi ~~ phi22*Lbmi; Lbmi ~~ phi23*Lfat
Lfat ~~ phi33*Lfat
# Of error terms in latent the regression (epsilon_ij)
Lcholest ~~ psi11*Lcholest; Lcholest ~~ psi12*Ldiastol
Ldiastol ~~ psi22*Ldiastol
# Of measurement errors (e_ijk) for measurement set 1
age1 ~~ w111*age1; age1 ~~ w112*bmi1; age1 ~~ w113*fat1;
age1 ~~ w114*cholest1; age1 ~~ w115*diastol1
bmi1 ~~ w122*bmi1; bmi1 ~~ w123*fat1; bmi1 ~~ w124*cholest1; bmi1 ~~ w125*diastol1
fat1 ~~ w133*fat1; fat1 ~~ w134*cholest1; fat1 ~~ w135*diastol1
cholest1 ~~ w144*cholest1; cholest1 ~~ w145*diastol1
diastol1 ~~ w155*diastol1
# Of measurement errors (e_ijk) for measurement set 2
age2 ~~ w211*age2; age2 ~~ w212*bmi2; age2 ~~ w213*fat2;
age2 ~~ w214*cholest2; age2 ~~ w215*diastol2
bmi2 ~~ w222*bmi2; bmi2 ~~ w223*fat2; bmi2 ~~ w224*cholest2; bmi2 ~~ w225*diastol2
fat2 ~~ w233*fat2; fat2 ~~ w234*cholest2; fat2 ~~ w235*diastol2
cholest2 ~~ w244*cholest2; cholest2 ~~ w245*diastol2
diastol2 ~~ w255*diastol2
' ##### End of bmimodel1 #####

> fit1 = lavaan(bmimodel1, data=bmidata)
Warning messages:
1: In lav_model_vcov(lavmodel = lavmodel, lavsamplestats = lavsamplestats, :
lavaan WARNING:
Could not compute standard errors! The information matrix could
not be inverted. This may be a symptom that the model is not
identified.
2: In lav_object_post_check(object) :
lavaan WARNING: some estimated lv variances are negative

```

```
> summary(fit1)
lavaan 0.6-11 ended normally after 4241 iterations
```

```
Estimator ML
Optimization method NLMINB
Number of model parameters 45

Number of observations 500
```

Model Test User Model:

```
Test statistic 89.369
Degrees of freedom 10
P-value (Chi-square) 0.000
```

Parameter Estimates:

```
Standard errors Standard
Information Expected
Information saturated (h1) model Structured
```

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
Lage =~				
age1	1.000			
age2	1.000			
Lbmi =~				
bmi1	1.000			
bmi2	1.000			
Lfat =~				
fat1	1.000			
fat2	1.000			
Lcholest =~				
cholest1	1.000			
cholest2	1.000			
Ldiastol =~				
diastol1	1.000			
diastol2	1.000			

Regressions:

	Estimate	Std.Err	z-value	P(> z)
Lcholest ~				
Lage (bt11)	-26.391	NA		
Lbmi (bt12)	-354.932	NA		
Lfat (bt13)	203.432	NA		
Ldiastol ~				
Lage (bt21)	-28.583	NA		
Lbmi (bt22)	-390.464	NA		
Lfat (bt23)	221.685	NA		

Covariances:

	Estimate	Std.Err	z-value	P(> z)
Lage ~~				
Lbmi (ph12)	3.288	NA		
Lfat (ph13)	24.865	NA		
Lbmi ~~				
Lfat (ph23)	22.225	NA		
.Lcholest ~~				
.Ldiastl (ps12)	-2633.270	NA		
.age1 ~~				
.bmi1 (w112)	4.361	NA		
.fat1 (w113)	0.994	NA		
.cholest1 (w114)	3.102	NA		
.diastl1 (w115)	12.808	NA		

```

.bmi1 ~~
.fat1 (w123) 7.385 NA
.cholst1 (w124) -0.497 NA
.diastl1 (w125) 12.340 NA
.fat1 ~~
.cholst1 (w134) 7.835 NA
.diastl1 (w135) -6.960 NA
.cholest1 ~~
.diastl1 (w145) 0.038 NA
.age2 ~~
.bmi2 (w212) 0.752 NA
.fat2 (w213) -4.120 NA
.cholst2 (w214) -2.601 NA
.diastl2 (w215) 5.903 NA
.bmi2 ~~
.fat2 (w223) -3.043 NA
.cholst2 (w224) -3.469 NA
.diastl2 (w225) 6.602 NA
.fat2 ~~
.cholst2 (w234) -10.098 NA
.diastl2 (w235) -9.933 NA
.cholest2 ~~
.diastl2 (w245) -10.026 NA

```

Variiances:

		Estimate	Std.Err	z-value	P(> z)
Lage	(ph11)	146.720	NA		
Lbmi	(ph22)	12.318	NA		
Lfat	(ph33)	42.615	NA		
.Lcholst	(ps11)	169.820	NA		
.Ldiastl	(ps22)	-2785.532	NA		
.age1	(w111)	18.767	NA		
.bmi1	(w122)	9.177	NA		
.fat1	(w133)	18.669	NA		
.cholst1	(w144)	200.123	NA		
.diastl1	(w155)	204.316	NA		
.age2	(w211)	8.326	NA		
.bmi2	(w222)	2.460	NA		
.fat2	(w233)	9.975	NA		
.cholst2	(w244)	344.031	NA		
.diastl2	(w255)	59.441	NA		

```
> p1 = parTable(fit1); p1
```

id	lhs	op	rhs	user	block	group	free	ustart	exo	label	plabel	start	est	se	
1	1	Lcholest	~	Lage	1	1	1	1	NA	0	beta11	.p1.	0.000	-26.391	NA
2	2	Lcholest	~	Lbmi	1	1	1	2	NA	0	beta12	.p2.	0.000	-354.932	NA
3	3	Lcholest	~	Lfat	1	1	1	3	NA	0	beta13	.p3.	0.000	203.432	NA
4	4	Ldiastol	~	Lage	1	1	1	4	NA	0	beta21	.p4.	0.000	-28.583	NA
5	5	Ldiastol	~	Lbmi	1	1	1	5	NA	0	beta22	.p5.	0.000	-390.464	NA
6	6	Ldiastol	~	Lfat	1	1	1	6	NA	0	beta23	.p6.	0.000	221.685	NA
7	7	Lage	==	age1	1	1	1	0	1	0		.p7.	1.000	1.000	0
8	8	Lage	==	age2	1	1	1	0	1	0		.p8.	1.000	1.000	0
9	9	Lbmi	==	bmi1	1	1	1	0	1	0		.p9.	1.000	1.000	0
10	10	Lbmi	==	bmi2	1	1	1	0	1	0		.p10.	1.000	1.000	0
11	11	Lfat	==	fat1	1	1	1	0	1	0		.p11.	1.000	1.000	0
12	12	Lfat	==	fat2	1	1	1	0	1	0		.p12.	1.000	1.000	0
13	13	Lcholest	==	cholest1	1	1	1	0	1	0		.p13.	1.000	1.000	0
14	14	Lcholest	==	cholest2	1	1	1	0	1	0		.p14.	1.000	1.000	0
15	15	Ldiastol	==	diastol1	1	1	1	0	1	0		.p15.	1.000	1.000	0
16	16	Ldiastol	==	diastol2	1	1	1	0	1	0		.p16.	1.000	1.000	0
17	17	Lage	~~	Lage	1	1	1	7	NA	0	phi11	.p17.	0.050	146.720	NA
18	18	Lage	~~	Lbmi	1	1	1	8	NA	0	phi12	.p18.	0.000	3.288	NA
19	19	Lage	~~	Lfat	1	1	1	9	NA	0	phi13	.p19.	0.000	24.865	NA
20	20	Lbmi	~~	Lbmi	1	1	1	10	NA	0	phi22	.p20.	0.050	12.318	NA
21	21	Lbmi	~~	Lfat	1	1	1	11	NA	0	phi23	.p21.	0.000	22.225	NA

22	22	Lfat	~~	Lfat	1	1	1	12	NA	0	phi33	.p22.	0.050	42.615	NA
23	23	Lcholest	~~	Lcholest	1	1	1	13	NA	0	psi11	.p23.	0.050	169.820	NA
24	24	Lcholest	~~	Ldiastol	1	1	1	14	NA	0	psi12	.p24.	0.000	-2633.270	NA
25	25	Ldiastol	~~	Ldiastol	1	1	1	15	NA	0	psi22	.p25.	0.050	-2785.532	NA
26	26	age1	~~	age1	1	1	1	16	NA	0	w111	.p26.	83.763	18.767	NA
27	27	age1	~~	bmi1	1	1	1	17	NA	0	w112	.p27.	0.000	4.361	NA
28	28	age1	~~	fat1	1	1	1	18	NA	0	w113	.p28.	0.000	0.994	NA
29	29	age1	~~	cholest1	1	1	1	19	NA	0	w114	.p29.	0.000	3.102	NA
30	30	age1	~~	diastol1	1	1	1	20	NA	0	w115	.p30.	0.000	12.808	NA
31	31	bmi1	~~	bmi1	1	1	1	21	NA	0	w122	.p31.	10.925	9.177	NA
32	32	bmi1	~~	fat1	1	1	1	22	NA	0	w123	.p32.	0.000	7.385	NA
33	33	bmi1	~~	cholest1	1	1	1	23	NA	0	w124	.p33.	0.000	-0.497	NA
34	34	bmi1	~~	diastol1	1	1	1	24	NA	0	w125	.p34.	0.000	12.340	NA
35	35	fat1	~~	fat1	1	1	1	25	NA	0	w133	.p35.	30.023	18.669	NA
36	36	fat1	~~	cholest1	1	1	1	26	NA	0	w134	.p36.	0.000	7.835	NA
37	37	fat1	~~	diastol1	1	1	1	27	NA	0	w135	.p37.	0.000	-6.960	NA
38	38	cholest1	~~	cholest1	1	1	1	28	NA	0	w144	.p38.	1548.559	200.123	NA
39	39	cholest1	~~	diastol1	1	1	1	29	NA	0	w145	.p39.	0.000	0.038	NA
40	40	diastol1	~~	diastol1	1	1	1	30	NA	0	w155	.p40.	162.507	204.316	NA
41	41	age2	~~	age2	1	1	1	31	NA	0	w211	.p41.	76.888	8.326	NA
42	42	age2	~~	bmi2	1	1	1	32	NA	0	w212	.p42.	0.000	0.752	NA
43	43	age2	~~	fat2	1	1	1	33	NA	0	w213	.p43.	0.000	-4.120	NA
44	44	age2	~~	cholest2	1	1	1	34	NA	0	w214	.p44.	0.000	-2.601	NA
45	45	age2	~~	diastol2	1	1	1	35	NA	0	w215	.p45.	0.000	5.903	NA
46	46	bmi2	~~	bmi2	1	1	1	36	NA	0	w222	.p46.	7.156	2.460	NA
47	47	bmi2	~~	fat2	1	1	1	37	NA	0	w223	.p47.	0.000	-3.043	NA
48	48	bmi2	~~	cholest2	1	1	1	38	NA	0	w224	.p48.	0.000	-3.469	NA
49	49	bmi2	~~	diastol2	1	1	1	39	NA	0	w225	.p49.	0.000	6.602	NA
50	50	fat2	~~	fat2	1	1	1	40	NA	0	w233	.p50.	27.528	9.975	NA
51	51	fat2	~~	cholest2	1	1	1	41	NA	0	w234	.p51.	0.000	-10.098	NA
52	52	fat2	~~	diastol2	1	1	1	42	NA	0	w235	.p52.	0.000	-9.933	NA
53	53	cholest2	~~	cholest2	1	1	1	43	NA	0	w244	.p53.	1608.286	344.031	NA
54	54	cholest2	~~	diastol2	1	1	1	44	NA	0	w245	.p54.	0.000	-10.026	NA
55	55	diastol2	~~	diastol2	1	1	1	45	NA	0	w255	.p55.	88.049	59.441	NA

```

> fit1B = lavaan(bmimodell, data=bmidata, start = 'Mplus')
Warning messages:
1: In lav_model_vcov(lavmodel = lavmodel, lavsamplestats = lavsamplestats, :
lavaan WARNING:
    Could not compute standard errors! The information matrix could
    not be inverted. This may be a symptom that the model is not
    identified.
2: In lav_object_post_check(object) :
lavaan WARNING: some estimated lv variances are negative
> # Same warnings, 4241 iterations again

```

```

> # Start at Method of Moment estimates.
>
> head(bmidata)
  age1 bmi1 fat1 cholest1 diastol1 age2 bmi2 fat2 cholest2 diastol2
1   63 24.5 16.5   195.4       38   60 23.9 20.1   203.5       66
2   42 13.0  1.9   184.3       86   44 14.8  2.6   197.3       78
3   32 22.5 14.6   354.1      104   33 21.7 20.4   374.3       73
4   59 25.5 19.0   214.6       93   58 28.5 20.0   203.7      106
5   45 26.5 17.8   324.8       97   43 25.0 12.3   329.7       92
6   31 19.4 17.1   280.7       92   42 19.9 19.9   276.7       87
> W1 = as.matrix(bmidata[,1:3]) # age1 bmi1 fat1
> V1 = as.matrix(bmidata[,4:5]) # cholest1 diastol1
> W2 = as.matrix(bmidata[,6:8]) # age2 bmi2 fat2
> V2 = as.matrix(bmidata[,9:10]) # cholest2 diastol2
> var(W1,W2) # Matrix of sample covariances
      age2      bmi2      fat2
age1 148.220782  3.621581 25.29808
bmi1  5.035726 13.194016 21.42201
fat1 23.542289 20.613490 45.13296
> # Using S as short for Sigmahat, and not worrying about n vs. n-1,
> S11 = var(W1); S12 = var(W1,V1); S13 = var(W1,W2); S14 = var(W1,V2)
>      S22 = var(V1);      S23 = var(V1,W2); S24 = var(V1,V2)
>      S33 = var(W2);      S34 = var(W2,V2)
>      S44 = var(V2)
> # The matrices below should all have "hat" in the name, because they are estimates
> Phi = (S13+t(S13))/2
> rownames(Phi) = colnames(Phi) = c('Lage', 'Lbmi', 'Lfat'); Phi
      Lage      Lbmi      Lfat
Lage 148.220782  4.328654 24.42019
Lbmi  4.328654 13.194016 21.01775
Lfat 24.420185 21.017749 45.13296
> # To my surprise, these are quite close to the MLEs from the first run.
> Beta = 0.5*(t(S14)+S23) %*% solve(Phi)
> rownames(Beta) = c('Lcholest', 'Ldiastol')
> colnames(Beta) = c('Lage', 'Lbmi', 'Lfat'); Beta
      Lage      Lbmi      Lfat
Lcholest -0.3851327 -0.1885072 2.968322
Ldiastol  0.0224190 -0.3556138 1.407425
> # These are miles away from the supposed MLEs
> # Can just say some of the rest are close and others are not.
>
> Psi = S24 - Beta %*% Phi %*% t(Beta)
> rownames(Psi) = colnames(Psi) = c('Lcholest', 'Ldiastol') # epsilon1, epsilon2
> Psi
      Lcholest  Ldiastol
Lcholest 2548.17303 -44.56069
Ldiastol -28.70087  57.64153
> # Oops, it should be symmetric.
> Psi = ( Psi+t(Psi) )/2; Psi
      Lcholest  Ldiastol
Lcholest 2548.17303 -36.63078
Ldiastol -36.63078  57.64153
> # Again, far away.
> Omegall = S11 - Phi; Omegall
      age1      bmi1      fat1
age1 19.640040 4.610807 1.634183
bmi1 4.610807 8.699533 8.754484
fat1 1.634183 8.754484 15.033932
> # Supposed MLEs are pretty close here.
> Omegal2 = S12 - ( S14+t(S23) )/2; Omegal2 # Not too bad
      cholest1  diastol1
age1 4.499017 12.164192
bmi1 -1.517733 10.671443
fat1 3.888565 -2.196681

```

```

> Omega22 = S22-S24 # A little rough but consistent
> Omega22 = (Omega22 + t(Omega22) )/2
> Omega22 # Variances okay, covariance off.
      cholest1  diastol1
cholest1 213.76117  11.24971
diastol1  11.24971 196.44520
> Omega33 = S33 - Phi; Omega33 # Not too bad
      age2      bmi2      fat2
age2  5.862661 -1.219843 -2.155736
bmi2 -1.219843  1.146991 -1.714769
fat2 -2.155736 -1.714769 10.033984
> Omega34 = S34 - ( S14+t(S23) )/2; Omega34 # Not too bad
      cholest2  diastol2
age2 -2.978041  0.7795992
bmi2 -1.206256  2.1081739
fat2 -6.422983 -4.9125882
> Omega44 = S44 - S24 ; Omega44 = ( Omega44 + t(Omega44) )/2
> Omega44 # Not terrible
      cholest2  diastol2
cholest2 333.45335 -21.65923
diastol2 -21.65923  47.23065
>
> # Carefully assemble the MOM estimates into a vector, same order as pl = parTable(fit1)
>
> mom = c(Beta[1,1], Beta[1,2], Beta[1,3], Beta[2,1], Beta[2,2], Beta[2,3],
+         1,1,1,1,1,1,1,1,1,1,
+         Phi[1,1], Phi[1,2], Phi[1,3], Phi[2,2], Phi[2,3], Phi[3,3],
+         Psi[1,1], Psi[1,2], Psi[2,2],
+         Omega11[1,1], Omega11[1,2], Omega11[1,3], Omega12[1,1], Omega12[1,2],
+         Omega11[2,2], Omega11[2,3], Omega12[2,1], Omega12[2,2],
+         Omega11[3,3], Omega12[3,1], Omega12[3,2],
+         Omega22[1,1], Omega22[1,2], Omega22[2,2],
+         Omega33[1,1], Omega33[1,2], Omega33[1,3], Omega34[1,1], Omega34[1,2],
+         Omega33[2,2], Omega33[2,3], Omega34[2,1], Omega34[2,2],
+         Omega33[3,3], Omega34[3,1], Omega34[3,2],
+         Omega44[1,1], Omega44[1,2], Omega44[2,2]
)
> length(mom)
[1] 55
>
> plmom = pl; plmom[14] = mom # Replace column 14 (est) with mom

> fit2 = lavaan(bmimodel1, data=bmidata, start = plmom); fit2
lavaan 0.6-11 ended normally after 242 iterations

```

Estimator	ML
Optimization method	NLMINB
Number of model parameters	45
Number of observations	500

Model Test User Model:

Test statistic	4.654
Degrees of freedom	10
P-value (Chi-square)	0.913

> summary(fit2)

lavaan 0.6-11 ended normally after 242 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	45

Number of observations	500
------------------------	-----

Model Test User Model:

Test statistic	4.654
Degrees of freedom	10
P-value (Chi-square)	0.913

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
Lage =~				
age1	1.000			
age2	1.000			
Lbmi =~				
bm1	1.000			
bmi2	1.000			
Lfat =~				
fat1	1.000			
fat2	1.000			
Lcholest =~				
cholest1	1.000			
cholest2	1.000			
Ldiastol =~				
diastol1	1.000			
diastol2	1.000			

Regressions:

		Estimate	Std.Err	z-value	P(> z)
Lcholest ~					
Lage	(bt11)	-0.320	0.228	-1.404	0.160
Lbmi	(bt12)	0.393	1.708	0.230	0.818
Lfat	(bt13)	2.774	0.980	2.829	0.005
Ldiastol ~					
Lage	(bt21)	0.020	0.050	0.407	0.684
Lbmi	(bt22)	-0.480	0.419	-1.145	0.252
Lfat	(bt23)	1.480	0.235	6.312	0.000

Covariances:

		Estimate	Std.Err	z-value	P(> z)
Lage ~~					
Lbmi	(ph12)	4.160	2.141	1.944	0.052
Lfat	(ph13)	23.320	3.986	5.851	0.000
Lbmi ~~					
Lfat	(ph23)	20.976	1.584	13.244	0.000
.Lcholest ~~					
.Ldiastl	(ps12)	-45.861	24.968	-1.837	0.066
.age1 ~~					
.bm1	(w112)	3.998	0.945	4.231	0.000
.fat1	(w113)	2.389	1.505	1.587	0.112
.cholst1	(w114)	2.702	9.091	0.297	0.766
.diastl1	(w115)	10.562	3.824	2.762	0.006

```

.bmi1 ~~
.fat1 (w123) 8.969 0.956 9.382 0.000
.cholst1 (w124) -0.884 4.178 -0.212 0.832
.diastl1 (w125) 10.060 2.274 4.424 0.000
.fat1 ~~
.cholst1 (w134) 7.923 6.741 1.175 0.240
.diastl1 (w135) -2.927 3.409 -0.859 0.390
.cholest1 ~~
.diastl1 (w145) -0.098 16.907 -0.006 0.995
.age2 ~~
.bmi2 (w212) -0.661 0.735 -0.899 0.369
.fat2 (w213) -2.703 1.369 -1.974 0.048
.cholst2 (w214) -1.962 8.962 -0.219 0.827
.diastl2 (w215) 2.273 2.710 0.839 0.402
.bmi2 ~~
.fat2 (w223) -1.849 0.705 -2.624 0.009
.cholst2 (w224) -2.653 3.476 -0.763 0.445
.diastl2 (w225) 2.652 1.487 1.784 0.074
.fat2 ~~
.cholst2 (w234) -11.376 6.546 -1.738 0.082
.diastl2 (w235) -4.839 2.536 -1.908 0.056
.cholest2 ~~
.diastl2 (w245) -8.972 12.605 -0.712 0.477

```

Variances:

	Estimate	Std.Err	z-value	P(> z)
Lage (ph11)	147.330	9.699	15.190	0.000
Lbmi (ph22)	13.341	0.986	13.528	0.000
Lfat (ph33)	44.485	3.101	14.345	0.000
.Lcholst (ps11)	2534.505	171.258	14.799	0.000
.Ldiastl (ps22)	56.169	9.221	6.092	0.000
.age1 (w111)	18.584	2.914	6.378	0.000
.bmi1 (w122)	8.665	0.708	12.239	0.000
.fat1 (w133)	16.125	1.659	9.717	0.000
.cholst1 (w144)	200.109	57.422	3.485	0.000
.diastl1 (w155)	195.040	14.323	13.617	0.000
.age2 (w211)	6.861	2.701	2.540	0.011
.bmi2 (w222)	1.089	0.491	2.220	0.026
.fat2 (w233)	9.332	1.539	6.064	0.000
.cholst2 (w244)	344.449	60.290	5.713	0.000
.diastl2 (w255)	48.349	8.246	5.864	0.000

```

>
> parTable(fit2)

```

id	lhs	op	rhs	user	block	group	free	ustart	exo	label	plabel	start	est	
1	1	Lcholest	~	Lage	1	1	1	1	NA	0	beta11	.p1.	-0.385	-0.320
2	2	Lcholest	~	Lbmi	1	1	1	2	NA	0	beta12	.p2.	-0.189	0.393
3	3	Lcholest	~	Lfat	1	1	1	3	NA	0	beta13	.p3.	2.968	2.774
4	4	Ldiastol	~	Lage	1	1	1	4	NA	0	beta21	.p4.	0.022	0.020
5	5	Ldiastol	~	Lbmi	1	1	1	5	NA	0	beta22	.p5.	-0.356	-0.480
6	6	Ldiastol	~	Lfat	1	1	1	6	NA	0	beta23	.p6.	1.407	1.480
7	7	Lage	==	age1	1	1	1	0	1	0		.p7.	1.000	1.000
8	8	Lage	==	age2	1	1	1	0	1	0		.p8.	1.000	1.000
9	9	Lbmi	==	bmi1	1	1	1	0	1	0		.p9.	1.000	1.000
10	10	Lbmi	==	bmi2	1	1	1	0	1	0		.p10.	1.000	1.000
11	11	Lfat	==	fat1	1	1	1	0	1	0		.p11.	1.000	1.000
12	12	Lfat	==	fat2	1	1	1	0	1	0		.p12.	1.000	1.000
13	13	Lcholest	==	cholest1	1	1	1	0	1	0		.p13.	1.000	1.000
14	14	Lcholest	==	cholest2	1	1	1	0	1	0		.p14.	1.000	1.000
15	15	Ldiastol	==	diastol1	1	1	1	0	1	0		.p15.	1.000	1.000
16	16	Ldiastol	==	diastol2	1	1	1	0	1	0		.p16.	1.000	1.000
17	17	Lage	~~	Lage	1	1	1	7	NA	0	phi11	.p17.	148.221	147.330
18	18	Lage	~~	Lbmi	1	1	1	8	NA	0	phi12	.p18.	4.329	4.160
19	19	Lage	~~	Lfat	1	1	1	9	NA	0	phi13	.p19.	24.420	23.320
20	20	Lbmi	~~	Lbmi	1	1	1	10	NA	0	phi22	.p20.	13.194	13.341
21	21	Lbmi	~~	Lfat	1	1	1	11	NA	0	phi23	.p21.	21.018	20.976

22	22	Lfat	~~	Lfat	1	1	1	12	NA	0	phi33	.p22.	45.133	44.485
23	23	Lcholest	~~	Lcholest	1	1	1	13	NA	0	psi11	.p23.	2548.173	2534.505
24	24	Lcholest	~~	Ldiastol	1	1	1	14	NA	0	psi12	.p24.	-36.631	-45.861
25	25	Ldiastol	~~	Ldiastol	1	1	1	15	NA	0	psi22	.p25.	57.642	56.169
26	26	age1	~~	age1	1	1	1	16	NA	0	w111	.p26.	19.640	18.584
27	27	age1	~~	bmi1	1	1	1	17	NA	0	w112	.p27.	4.611	3.998
28	28	age1	~~	fat1	1	1	1	18	NA	0	w113	.p28.	1.634	2.389
29	29	age1	~~	cholest1	1	1	1	19	NA	0	w114	.p29.	4.499	2.702
30	30	age1	~~	diastol1	1	1	1	20	NA	0	w115	.p30.	12.164	10.562
31	31	bmi1	~~	bmi1	1	1	1	21	NA	0	w122	.p31.	8.700	8.665
32	32	bmi1	~~	fat1	1	1	1	22	NA	0	w123	.p32.	8.754	8.969
33	33	bmi1	~~	cholest1	1	1	1	23	NA	0	w124	.p33.	-1.518	-0.884
34	34	bmi1	~~	diastol1	1	1	1	24	NA	0	w125	.p34.	10.671	10.060
35	35	fat1	~~	fat1	1	1	1	25	NA	0	w133	.p35.	15.034	16.125
36	36	fat1	~~	cholest1	1	1	1	26	NA	0	w134	.p36.	3.889	7.923
37	37	fat1	~~	diastol1	1	1	1	27	NA	0	w135	.p37.	-2.197	-2.927
38	38	cholest1	~~	cholest1	1	1	1	28	NA	0	w144	.p38.	213.761	200.109
39	39	cholest1	~~	diastol1	1	1	1	29	NA	0	w145	.p39.	11.250	-0.098
40	40	diastol1	~~	diastol1	1	1	1	30	NA	0	w155	.p40.	196.445	195.040
41	41	age2	~~	age2	1	1	1	31	NA	0	w211	.p41.	5.863	6.861
42	42	age2	~~	bmi2	1	1	1	32	NA	0	w212	.p42.	-1.220	-0.661
43	43	age2	~~	fat2	1	1	1	33	NA	0	w213	.p43.	-2.156	-2.703
44	44	age2	~~	cholest2	1	1	1	34	NA	0	w214	.p44.	-2.978	-1.962
45	45	age2	~~	diastol2	1	1	1	35	NA	0	w215	.p45.	0.780	2.273
46	46	bmi2	~~	bmi2	1	1	1	36	NA	0	w222	.p46.	1.147	1.089
47	47	bmi2	~~	fat2	1	1	1	37	NA	0	w223	.p47.	-1.715	-1.849
48	48	bmi2	~~	cholest2	1	1	1	38	NA	0	w224	.p48.	-1.206	-2.653
49	49	bmi2	~~	diastol2	1	1	1	39	NA	0	w225	.p49.	2.108	2.652
50	50	fat2	~~	fat2	1	1	1	40	NA	0	w233	.p50.	10.034	9.332
51	51	fat2	~~	cholest2	1	1	1	41	NA	0	w234	.p51.	-6.423	-11.376
52	52	fat2	~~	diastol2	1	1	1	42	NA	0	w235	.p52.	-4.913	-4.839
53	53	cholest2	~~	cholest2	1	1	1	43	NA	0	w244	.p53.	333.453	344.449
54	54	cholest2	~~	diastol2	1	1	1	44	NA	0	w245	.p54.	-21.659	-8.972
55	55	diastol2	~~	diastol2	1	1	1	45	NA	0	w255	.p55.	47.231	48.349

se

1	0.228
2	1.708
3	0.980
4	0.050
5	0.419
6	0.235
7	0.000
8	0.000
9	0.000
10	0.000
11	0.000
12	0.000
13	0.000
14	0.000
15	0.000
16	0.000
17	9.699
18	2.141
19	3.986
20	0.986
21	1.584
22	3.101
23	171.258
24	24.968
25	9.221
26	2.914
27	0.945
28	1.505
29	9.091
30	3.824
31	0.708
32	0.956
33	4.178
34	2.274
35	1.659
36	6.741
37	3.409

38	57.422
39	16.907
40	14.323
41	2.701
42	0.735
43	1.369
44	8.962
45	2.710
46	0.491
47	0.705
48	3.476
49	1.487
50	1.539
51	6.546
52	2.536
53	60.290
54	12.605
55	8.246