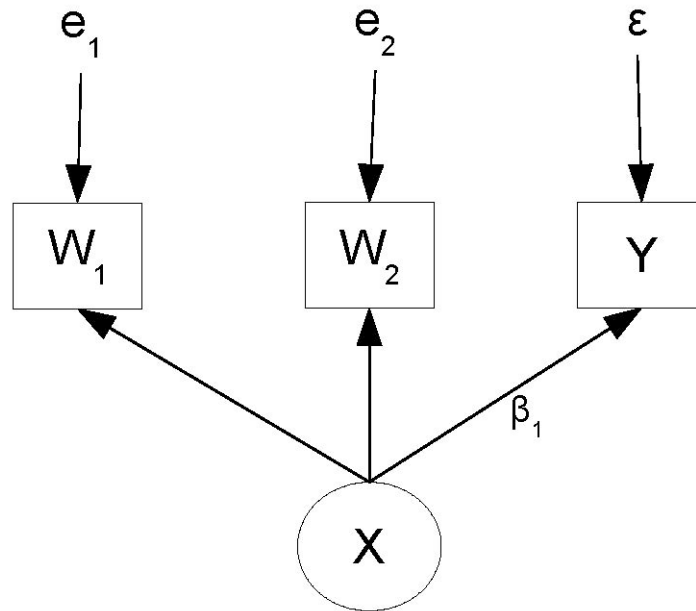


Little Double Measurement Regression Example*



```
> rm(list=ls()); options(scipen=999)
> # install.packages("lavaan", dependencies = TRUE) # Only need to do this once
> library(lavaan)
This is lavaan 0.6-11
lavaan is FREE software! Please report any bugs.
>
> babydouble =
read.table("http://www.utstat.toronto.edu/~brunner/openSEM/data/Babydouble.data.txt")
> head(babydouble)
  W1  W2  Y
1  9.94 12.24 15.23
2 12.42 11.32 14.55
3 10.43 10.40 12.40
4  9.07  9.85 17.09
5 11.04 11.98 16.83
6 10.40 10.85 15.04

> dim(babydouble)
[1] 150  3

> summary(babydouble)
      W1          W2          Y
Min.   : 6.190   Min.   : 6.76   Min.   : 3.98
1st Qu.: 8.932   1st Qu.: 9.11   1st Qu.:10.97
Median : 9.720   Median :10.05   Median :13.22
Mean   : 9.809   Mean   :10.06   Mean   :13.10
3rd Qu.:10.655   3rd Qu.:10.99   3rd Qu.:15.46
Max.   :12.830   Max.   :13.57   Max.   :21.62

> cor(babydouble)
      W1          W2          Y
W1  1.0000000  0.5748331  0.1714324
W2  0.5748331  1.0000000  0.1791539
Y   0.1714324  0.1791539  1.0000000
```

* Copyright information is on the last page.

```

>
> dmodel1 = 'Y ~ betal*X          # Latent variable model (even though Y is observed)
+           X =~ 1*W1 + 1*W2     # Measurement model
+           # Variances (covariances would go here too)
+           X~~phi*X             # Var(X) = phi
+           Y~~psi*Y             # Var(epsilon) = psi
+           W1~~omega1*W1        # Var(e1) = omega1
+           W2~~omega2*W2        # Var(e2) = omega2
+
> dfit1 = lavaan(dmodel1, data=babydouble)
> summary(dfit1)

```

lavaan 0.6-11 ended normally after 23 iterations

Estimator	ML
Optimization method	NLMINB
Number of model parameters	5
Number of observations	150

Model Test User Model:

Test statistic	0.007
Degrees of freedom	1
P-value (Chi-square)	0.933

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
X =~				
W1	1.000			
W2	1.000			

Regressions:

		Estimate	Std.Err	z-value	P(> z)
Y ~					
X	(bet1)	0.707	0.290	2.442	0.015

Variances:

		Estimate	Std.Err	z-value	P(> z)
X	(phi)	1.104	0.181	6.104	0.000
.Y	(psi)	9.775	1.153	8.481	0.000
.W1	(omg1)	0.834	0.158	5.265	0.000
.W2	(omg2)	0.800	0.156	5.123	0.000

```

>
> parameterEstimates(dfit1)
  lhs op rhs label est se z pvalue ci.lower ci.upper
1 Y ~ X beta1 0.707 0.290 2.442 0.015 0.140 1.275
2 X =~ W1 1.000 0.000 NA NA 1.000 1.000
3 X =~ W2 1.000 0.000 NA NA 1.000 1.000
4 X ~~ X phi 1.104 0.181 6.104 0.000 0.750 1.459
5 Y ~~ Y psi 9.775 1.153 8.481 0.000 7.516 12.034
6 W1 ~~ W1 omega1 0.834 0.158 5.265 0.000 0.524 1.145
7 W2 ~~ W2 omega2 0.800 0.156 5.123 0.000 0.494 1.105

> parTable(dfit1)
  id lhs op rhs user block group free ustart exo label plabel start est se
1 1 Y ~ X 1 1 1 1 1 NA 0 beta1 .p1. 0.000 0.707 0.290
2 2 X =~ W1 1 1 1 0 1 0 .p2. 1.000 1.000 0.000
3 3 X =~ W2 1 1 1 0 1 0 .p3. 1.000 1.000 0.000
4 4 X ~~ X 1 1 1 2 NA 0 phi .p4. 0.050 1.104 0.181
5 5 Y ~~ Y 1 1 1 3 NA 0 psi .p5. 5.164 9.775 1.153
6 6 W1 ~~ W1 1 1 1 4 NA 0 omega1 .p6. 0.968 0.834 0.158
7 7 W2 ~~ W2 1 1 1 5 NA 0 omega2 .p7. 0.953 0.800 0.156

> coef(dfit1) # A vector of MLEs
beta1 phi psi omega1 omega2
0.707 1.104 9.775 0.834 0.800

> fitted(dfit1) # Sigma(thetahat) and mu(thetahat)
$scov
 W1 W2 Y
W1 1.939
W2 1.104 1.904
Y 0.781 0.781 10.327

>
> vcov(dfit1)
beta1 phi psi omega1 omega2
beta1 0.084
phi -0.007 0.033
psi -0.035 0.002 1.328
omega1 0.003 -0.004 -0.002 0.025
omega2 0.003 -0.005 -0.002 -0.007 0.024

> logLik(dfit1)
'log Lik.' -878.512 (df=5)

```



```

> # And one attempt to fit a non-identified model
>
> dmodel0 = 'Y ~ beta1*X      # Latent variable model (even though Y is observed)
+           X =~ 1*W1       # Measurement model
+           # Variances (covariances would go here too)
+           X~~phi*X        # Var(X) = phi
+           Y~~psi*Y        # Var(epsilon) = psi
+           W1~~omegal*W1   # Var(e1) = omegal
+
> dfit0 = lavaan(dmodel0, data=babydouble)

```

```

Warning message:
In lav_model_vcov(lavmodel = lavmodel, lavsamplestats = lavsamplestats, :
lavaan WARNING:
  Could not compute standard errors! The information matrix could
  not be inverted. This may be a symptom that the model is not
  identified.

```

```

> summary(dfit0)
lavaan 0.6-11 ended normally after 17 iterations

```

Estimator	ML
Optimization method	NLMINB
Number of model parameters	4

Number of observations	150
------------------------	-----

Model Test User Model:

Test statistic	NA
Degrees of freedom	-1
P-value (Unknown)	NA

Parameter Estimates:

Standard errors	Standard
Information	Expected
Information saturated (h1) model	Structured

Latent Variables:

	Estimate	Std.Err	z-value	P(> z)
X =~				
W1	1.000			

Regressions:

	Estimate	Std.Err	z-value	P(> z)
Y ~				
X (bet1)	0.734	NA		

Variances:

	Estimate	Std.Err	z-value	P(> z)
X (phi)	1.044	NA		
.Y (psi)	9.765	NA		
.W1 (omg1)	0.892	NA		

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<http://www.utstat.toronto.edu/brunner/oldclass/2053f22>