

STA 2212S

Feb. 5

0. Screen shot yesterday ; Covid link ; Stat 200

1. HW 2

2. ~~HW~~  $\chi^2$  g of fit

3. HW 3

In AoS only g-of-fit test in  $\chi^2$ .

$\underline{X}_1, \underline{X}_2, \dots, \underline{X}_n$  iid Multinomial ( $m; \underline{p}$ )

$$\underline{X}_i \sim \text{Mult}(n; \underline{p}) \quad \underline{p} = (p_1, \dots, p_m) \quad \sum_{j=1}^m p_j = 1$$

Simple case  $H_0: \underline{p} = \underline{p}_0$

e.g.  $(\frac{1}{m}, \frac{1}{m}, \dots, \frac{1}{m})$  uniform

e.g.  $(\frac{1}{16}, \frac{3}{16}, \frac{3}{16}, \frac{9}{16})$  Mendel

maybe  $H_0: \underline{p} = \underline{p}(\underline{\theta}) \quad \dim(\underline{\theta}) < m$

Test of  $H_0$ :

	1	...	m
$N_j$	$N_1$	...	$N_m$
$np_j(\underline{\theta})$	$np_1(\underline{\theta})$	...	$np_m(\underline{\theta})$
$E$	$E$		

$N_j = \# X_i \text{ in cell } j$

$$\chi^2_{\text{test statistic}} = \sum_{j=1}^m \frac{\{N_j - np_j(\hat{\theta})\}^2}{np_j(\hat{\theta})} \quad \frac{(O - E)^2}{E}$$

$$\underline{\theta} \leftarrow \hat{\underline{\theta}}$$

Example Test Hardy-Weinberg equilibrium

predicts blood type as

$$p(\underline{\theta}): \begin{matrix} M & MN & N \\ (1-\theta)^2 & 2\theta(1-\theta) & \theta^2 \end{matrix} \quad \sum_{i=1}^3 = 1$$

### External validation with APPROVe study

[08 Baron et al.]

Vioxx vs placebo

GI subgroups	p-value for HTE significance	CVT subgroups	p-value for HTE significance
✓ History of GI event	0.022	✓ History of atherosclerosis	0.048
History of hypertension & prior usage of steroids	(*small size, no events)	✓ Usage of aspirin indicated a/c to FDA	0.016
Old age & prior usage of steroids	(*small size, no events)	✓ Old age & male gender	0.012

\*inconclusive

n.c.

	M	MN	N	
E	340.6	502.8	1856	1049
O	342	500	187	1049

$\hat{\theta} = 0.4247$   
 $n p_1(\hat{\theta})$   
 $\chi^2 = \frac{(340.6 - 342)^2}{340.6} + \frac{(502.8 - 500)^2}{502.8} + \frac{(185.6 - 187)^2}{185.6} = 0.0319$

$\chi^2_{df}$

"2 independent cells",  $\theta$  has been est'd  
 $n$  fixed

$$2 - 1 = 1 \text{ d.f.}$$

	D	A
T	a	b
C	c	d

$\chi^2 = \frac{(ad - bc)^2}{n} \sim \chi^2_1$

~~$\theta$  is ind't of  $\sigma^2$~~   
 $\theta$ : rows are ind't of cols