Distributions for Parameters

Nancy Reid University of Toronto

Australian National University

Mar 4 2020



Reproducibility and Statistical theory



David Spiegelhalter @d_spiegel

This paper motivates the call for the end of significance. A 25% mortality reduction, but because P=0.06 (two-sided), they declare it 'did not reduce' mortality. Appalling. jamanetwork.com/journals/jama/...



JAMA | Original Investigation | CARING FOR THE CRITICALLY ILL PATIENT

Effect of a Resuscitation Strategy Targeting Peripheral Perfusion Status vs Serum Lactate Levels on 28-Day Mortality Among Patients With Septic Shock The ANDROMEDA-SHOCK Randomized Clinical Trial

Glenn Hernández, MD, PhD; Gustavo A. Ospina-Tascón, MD, PhD; Lucas Petri Damiani, MSc; Elisa Estenssoro, MD; Arnaldo Dubin, MD, PhD; Javier Hurtado, MD; Gilberto Friedman, MD, PhD; Ricardo Castro, MD, MPH; Leyla Alegría, RN, MSc; Jean-Louis Teboul, MD, PhD; Maurizio Cecconi, MD, FFICM; Glorgio Ferri, MD; Manuel Jibaja, MD; Ronald Pairumani, MD; Paula Fernández, MD; Diego Barahona, MD; Vladimir Granda-Luna, MD, PhD; Alexandre Biasi Cavalcanti, MD, PhD; Jan Bakker, MD, PhD; for the ANDROMEDA-SHOCK Investigators and the Latin America Intensive Care Network (LIVEN)

Andromeda Trial

Hernández et al. 2019

- comparing two treatments for septic shock
- randomized clinical trial
- estimated hazard ratio 0.75 [0.55, 1.02]
- 2-sided p-value 0.06

after adjusting for confounders

34.9% vs 43.4% unadjusted

- Discussion: " a peripheral perfusion-targeted resuscitation strategy did not result in a significantly lower 28-day mortality when compared with a lactate level-targeted strategy"
- Abstract: "Among patients with septic shock, a resuscitation strategy targeting normalization of capillary refill time, compared with a strategy targeting serum lactate levels, did not reduce all-cause 28-day mortality."

- 2014: Basic and Applied Social Psychology published an editorial banning *p*-values actually "null hypothesis significance testing"
- "prior to publication, authors will need to remove all vestiges of the NHSTP ... *p*-values, ... , statements about 'significant differences' or lack thereof, and so on"

"confidence intervals are also banned"

- 2014: *Nature* published a News Feature by R. Nuzzo: "*p*-values, the gold standard of statistical validity, are not as reliable as many scientists assume"
- 2016: American Statistical Association released a public statement on statistical significance and *p*-values



732 North Washington Street, Alexandria, VA 22314 • (703) 684-1221 • Toll Free: (888) 231-3473 • www.amstat.org • www.twitter.com/AmstatNews

AMERICAN STATISTICAL ASSOCIATION RELEASES STATEMENT ON STATISTICAL SIGNIFICANCE AND P-VALUES

Provides Principles to Improve the Conduct and Interpretation of Quantitative

Science

March 7, 2016

2016

• 2017: Another *Nature* article *p* < 0.005

• Articles solicited for special issue of American Statistician

comment

Redefine statistical significance

We propose to change the default P-value threshold for statistical significance from 0.05 to 0.005 for claims of new discoveries.

Daniel J. Benjamin, James O. Berger, Magnus Johannesson, Brian A. Nosek, E.-J. Wagenmakers, Richard Berk, Kenneth A. Bollom, Björn Brembs, Lawrence Brown, Coin Camerer, David Cesarini, Christopher D. Chambers, Merlise Clyde, Thomas D. Cook, Paul De Boeck, Zoltan Dienes, Anna Dreber, Kenny Easwaran, Charles Efferson, Ernst Fehr, Fiona Fidler, Andy P. Field, Malcolm Forster. Edward I. George, Richard Gonzalez, Steven Goodman, Edwin Green, Donald P. Green, Anthony Greenwald, Jarrod D. Hadfield, Larry V. Hedges, Leonhard Heid, Teck Hua Ho, Herbert Holjtink, Daniel J. Hruschka, Kosuke Imal, Guido Imbens, John P. A. Ioannidis, Minjeong Jeon, James Holland Jones, Michael Krichler, David Laibson, John List, Roderick Little, Arthur Lupia, Edouard Machery, Scott E. Maxwell, Michael McCarthy, Don Moore, Stephen L. Morgan, Marcus Munafo, Shinichi Nakagawa, Brendan Nyhan, Timothy H. Parker, Luis Pericchi, Marco Perugini, Jeff Rouder, Judith Rousseau, Victoria Savalei, Felix D. Schhordord, Thomas Sellek, Betsy Sinclair, Dustin Tingley, Trisha Van Zandt, Simine Vazire, Duncan J. Watts, Christopher Winship, Robert L. Wolpert, Yu Xie, Cristobal Young, Jonathan Zimma and Valen E. Johnson

... a recent timeline

- 2019: American Statistician published special issue 43 articles; 400 pages
- Editorial introduction advised "abandon 'statistical significance' "
- Nature publishes a letter with 800+ signatories
- "we are not advocating a ban on P values, confidence intervals or other statistical measures – only that we should not treat them categorically
- "This includes dichotomization as statistically significant or not, as well as categorization based on other statistical measures such as Bayes factors."



When wen the last time you hand time you are applied on the provided of the two groups because the difference was batatically non-significant? If your experisons enables outs, there's batter of the provided of the provided of the two and the provided of the provided of the frequently happens, a plot or table showed it there existing the was difference.

Here do statistics to other lead accretists to derry difference that these not accretist in statistics can plaidly arel Per several genertrons, researchers have been various that a statistically non-significant result does not "prove the null hypothesis (the hypothesis that there is no difference between groups or not effect of a transmission strength and results (prove 'score other hypothesis. Such missionsperiods here for any energy of the mission services here in correct the hypothesis. literature with overstated claims and, less farmously, led to claims of coefficts between studies where none exists.

We have some proposals to keep scientists from falling prey to these misconceptions.

PERVASIVE PROBLEM

Let's be clear about what must step: we should never conclude there is 'no difference' or 'no association' just because a P value is larger than a threshold such as 0.05 **b**

21 MARCE 2019 | VOL 357 | NATURE | 30 0 2019 Spinger Nature Limited All rights reserved.



TORTINI

For your delectation and delight, desultory dicta on the law of delicts.

Archives »



"Lawyers and judges pay close attention to standards, guidances, and consenus statements from respected and recognized professional organizations."

"Despite the fairly clear and careful statement of principles, legal actors did not take long to misrepresent the ASA principles." 2016

"distorted into strident assertions that statistical significance was unnecessary for scientific conclusions."



HARVARD DATA SCIENCE REVIEW

P-Values on Trial: Selective Reporting of (Best Practice Guides Against) Selective Reporting

by Deborah Mayo

outlines a 2018 Supreme Court case appealing a conviction for wire fraud, based on misleading investors Harkonen v. United States 13-180

the fraud centered on *p*-hacking the results of a Phase III trial of a drug

marketed by Harkonen

in the appeal "his defenders argued that the ASA guide provides compelling new evidence that the scientific theory upon which petitioner's conviction was based [that of statistical significance testing] is demonstrably false"

What to do?

report actual p-value, not "*", p < 0.05, etc.

to sensible number of decimal points

- supplement *p*-value with sample size, estimated power, etc.
- clarify 'exploratory' and 'confirmatory' p-values
- · report effect sizes and estimated standard errors
- report confidence intervals
- pre-register trials, specifying primary and secondary outcomes
- pre-specify data analysis
- provide a *p*-value function
- or some analogous distribution

significance function

Spiegelhalter 2017

Bayes posterior

Distributions for parameters

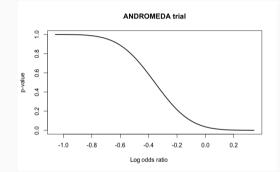
Fraser 1991

ANDROMEDA trial

	Died	Lived	
New	74	138	212
Old	92	120	212
Total	166	258	424

2-sided *p*-value = 0.07

likelihood ratio test no adjustment for covariates



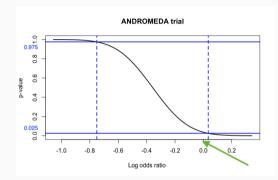
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ANDROMEDA trial

	Died	Lived	
New	74	138	212
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Total	166	258	424

2-sided *p*-value = 0.07

likelihood ratio test no adjustment for covariates



90% confidence interval: [-0.688, -0.030] 95% confidence interval: [-0.751, 0.034] 99% confidence interval: [-0.825, 0.107]

SOME PROBLEMS CONNECTED WITH STATISTICAL INFERENCE

By D. R. Cox

Birkbeck College, University of London¹

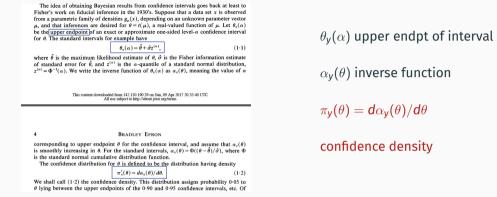
 Introduction. This paper is based on an invited address given to a joint meeting of the Institute of Mathematical Statistics and the Biometric Society at Princeton, N. J., 20th April, 1956. It consists of some general comments, few of them new, about statistical inference.

Since the address was given publications by Fisher [11], [12], [13], have produced a spirited discussion [7], [21], [24], [31] on the general nature of statistical methods. I have not attempted to revise the paper so as to comment point by point on the specific issues raised in this controversy, although I have, of course, hecked that the literature of the controversy does not lead me to change the opinions expressed in the final form of the paper. **Parts of the paper are con**troversiti; these are not put forward in any dogmatic spirite.

2. Inferences and decisions. A statistical inference will be defined for the

- "... the method of confidence intervals, as usually formulated, gives only one interval at some preselected level of probability"
- "... in ... simple cases ... there seems no reason why we should not work with confidence distributions for the unknown parameter
- "These can either be defined directly, or ... introduced in terms of the set of all confidence intervals"

Confidence Distribution



- "assigns probability 0.05 to θ between upper endpoints of 0.90 and 0.95 confidence intervals, ..."
- "Of course this is logically incorrect, but it has powerful intuitive appeal"
- "... no nuisance parameters [this] is exactly Fisher's fiducial distribution"

Seidenfeld 1992; Zabell 1992

528 Dr Fisher, Inverse probability

Inverse Probability. By R. A. FISHER, Sc.D., F.R.S., Gonville and Caius College; Statistical Dept., Rothamsted Experimental Station. [*Received* 23 July, *read* 28 July 1930.]

$$\mathrm{d}f = -\frac{\partial}{\partial\theta}F(Y,\theta)\mathrm{d}\theta$$

fiducial probability density for θ , given statistic Y

"It is not to be lightly supposed that men of the mental calibre of Laplace and Gauss ... could fall into error on a question of prime theoretical importance, without an uncommonly good reason"

Distributions for parameters

- significance function
- confidence distribution
- fiducial probability

 $p(\theta) = \Pr(y \ge y^{\circ} \mid \theta)$ $\alpha_{y}(\theta) = \theta_{y}^{-1}(\alpha)$ $df = -(\partial F / \partial \theta)(Y; \theta) d\theta$

structural probability

a re-formulation of fiducial probability for transformation models Fraser 1966

belief functions

ANU Mar 2020

Dempster '66; Schafer '76

In spite of the naming, these are not 'real' probability distributions Don't obey the rules of probability calculus

Bayes 1763

LII. An Essay towards solving a Problem in the Doctrine of Chances. By the late Rev. Mr. Bayes, F. R. S. communicated by Mr. Price, in a Letter to John Canton, A. M. F. R. S.

Dear Sir,

Read Dec. 23, I Now fend you an effay which I have 1763 . I found among the papers of our deceafed friend Mr. Bayes, and which, in my opinion, has great merit, and well deferves to be preferved. Experimental philofophy, you will find, is nearly interefted in the fubject of it; and on this account there feems to be particular reafon for thinking that a communication of it to the Royal Society cannot be improper.

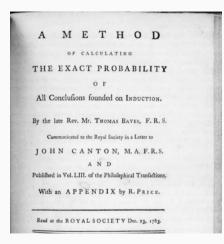
 $\pi(\theta \mid \mathbf{y}^{o}) = f(\mathbf{y}^{o}; \theta)\pi(\theta)/m(\mathbf{y}^{o})$

a 'real' probability distribution for $\boldsymbol{\theta}$

 y^{o} is fixed probability comes from $\pi(\theta)$

$$\Pr(\Theta \in \mathsf{A} \mid y^{\mathsf{o}}) = \int_{\mathsf{A}} \pi(\theta \mid y^{\mathsf{o}}) d\theta$$

Posterior Distribution



 $\pi(\theta \mid y^{o}) = f(y^{o}; \theta)\pi(\theta)/m(y^{o})$

a 'real' probability distribution for $\boldsymbol{\theta}$

 y^{o} is fixed probability comes from $\pi(\theta)$

$$\Pr(\Theta \in \mathsf{A} \mid y^{\mathsf{o}}) = \int_{\mathsf{A}} \pi(\theta \mid y^{\mathsf{o}}) d\theta$$

Stigler 2013

Bayes 1763

Why do we want distributions on parameters?

- inference is intuitive
- combines easily with decision theory
- · de-emphasizes point estimation and arbitrary cut-offs
- "it's tempting to conclude that μ is more likely to be near the middle of this interval, and if outside, not very far outside"

Cox 2006

• "assigns probability 0.05 to θ lying between the upper endpoints of the 0.90 and 0.95 confidence intervals, etc."

Efron 1993

• all inference statements are seem to be probability statements about unknowns

Nature of Probability

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- probability to describe physical haphazard variability
 - probabilities represent features of the "real" world in somewhat idealized form
 - subject to empirical test and improvement
 - · conclusions of statistical analysis expressed in terms of interpretable parameters
 - enhanced understanding of the data generating process
- probability to describe the uncertainty of knowledge
 - measures rational, supposedly impersonal, degree of belief. given relevant information
 - measures a particular person's degree of belief, subject typically to some constraints of self-consistency Ramsev, de Finetti, Savage
- "In short, the [Bayesian] paradigm does not produce probabilities from no probabilities"

aleatory/empirical

Cox 2006; R & Cox 2015

Jeffrevs

epistemic

Fraser 2011



The First Workshop on BFF Inference and Statistical Foundations (BFF 2014)

November 10 - November 14, 2014

7th Bayes, Fiducial and Frequentis Statistics Conference

BFF 一生友達

Methodological, Computational, and Ethical Principles for Data Science

May 6 - 8, 2020, The Fields Institute Location: Fields Institute, Room 230

... BFF 1 – 6

- posterior distribution 1763
- fiducial probability 1930
- confidence distribution 1958

- structural probability 1964
- significance function 1991

- objective Bayes
- generalized fiducial inference

Hannig 2009–; Taraldsen 2017

1995-

• confidence distributions and confidence curves Hjort, Schweder, Xie 2013-

- approximate significance functions Brazzale et al 2007; Fraser & R 1993
- inferential models Martin & Liu 2013-

- belief functions 1967
 - high-dimensional inference and model selection

computation

model complexity

model dimension

data

science

- posterior distribution
- fiducial probability
- confidence distribution
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Hannig; Taraldsen

Martin & Liu

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Brazzale et al 2007; Fraser & R 1993

belief functions

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Objective Bayes

Objective Bayes

- there are many proposals for priors meant to be non-informative
- examples include reference, default, matching, vague, ... priors
- a popular choice is Jeffreys' prior $\pi(heta) \propto |i(heta)|^{1/2}$ expected Fisher information
- what interpretation do we put on the posterior distribution? empirical? epistemic?
- we may avoid the need for a different version of probability by appeal to a notion of calibration Cox 2006, R & Cox 2015
- as with other measuring devices, within this scheme of repetition, probability is defined as a hypothetical frequency
- it is unacceptable if a procedure yielding high-probability regions in some non-frequency sense are poorly calibrated
- such procedures, used repeatedly, give misleading conclusions

... objective Bayes

- there are many proposals for priors meant to be non-informative
- examples include reference, default, matching, vague, ... priors
- a popular choice is Jeffreys' prior $\pi(heta) \propto |i(heta)|^{1/2}$

expected Fisher information

• some versions may not be correctly calibrated

requires checking in each example

· calibrated versions must be targetted on the parameter of interest

Fraser 2011

e.g. Jeffrevs'

- only in very special cases can calibration be achieved for more than one parameter in the model, from the same prior
- the simplicity of a fully Bayesian approach to inference is lost

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... objective Bayes

- the simplicity of a fully Bayesian approach to inference is lost
- for example

$$\pi(\psi \mid \mathbf{y}) = \int_{\psi(heta) = \psi} \pi(heta \mid \mathbf{y}) d heta, \quad ext{ for any } \psi: \Theta \searrow \Psi$$

lower dimension

- · the prior can have unexpected influence on the posterior
- even if they are seemingly noninformative

objective Bayes fails

• Stein's example:

 $\begin{array}{rcl} y_i & \sim & N(\theta_i, 1/n), \quad i = 1, \dots, k \\ \pi(\theta_i) & \propto & 1 \\ \pi(\theta \mid y) & \propto & N(y, l_k/n) \end{array}$

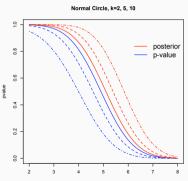
Gelman 2008

Example

Stein, 1959

- $y_i \sim N(\theta_i, 1/n), \quad i = 1, \dots, k; \quad \pi(\theta_i) \propto 1$
- posterior distribution of $a^{T}\theta$ is well-calibrated
- marginal posterior distribution of $\psi = \Sigma \theta_i^2$ is not
- discrepancy is a function of $\frac{k-1}{\psi\sqrt{n}}$
- $p(\psi) = \Pr\{\chi_k^2(n\psi^2) \ge n ||y||^2\}$

 $\mathsf{s}(\psi) = \mathsf{Pr}\{\chi_k^2(n||\mathbf{y}||^2) \ge n\psi^2\}$



- · calibrated posterior distributions must be targetted on the parameter of interest
- · matching priors set out this requirement explicitly

defined by calibration of posterior quantiles

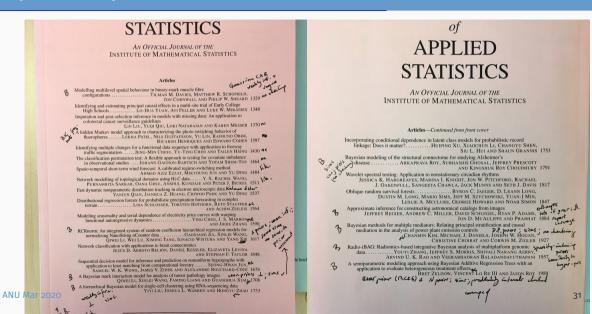
• reference priors are also targetted

although with a different goal than calibration

- vague priors, hierarchical priors, weakly informative priors, ... are not (usually) targetted on a particular parameter of interest
- AoAS September 2018: 9/24 articles used Bayesian methods
- one checked the coverage of posterior intervals
- one used simulations to evaluate point estimates

Haphazard sample

AoAS Sept 2019



Distributions for parameters

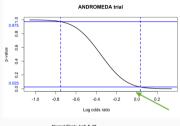
- what about fiducial, confidence, significance, inferential models, etc.?
- do they provide a way around the problems with objective Bayes?
- no, but
- requirement of targetting on parameter of interest is perhaps more obvious
- confidence approach is to pre-specify, or identify, from the model, a quantity that measures the parameter of interest
 focus parameter, Hjort & Schweder, 2016
- significance function approach is to use higher-order asymptotic theory to tell you what that quantity should be $$\rm F\&R,2018$$

Example 1: 2 \times 2 table

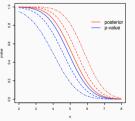
Based on conditional distribution of odds-ratio, given marginal totals

Example 2: $y_i \sim N(\theta_i, 1/n)$

Based on marginal distribution of Σy_i^2







- posterior distribution
- fiducial probability
- confidence distribution
- structural probability
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- objective Bayes
- generalized fiducial inference

Hannig; Taraldsen

Martin & Liu

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Brazzale et al 2007; Fraser & R 1993

belief functions

inferential models

high-dimensional inference and model selection

High-dimensional inference and model selection

Bayesian linear regression

Lasso

- $Y = X\beta + \epsilon$, $\epsilon \sim N_n(0, I)$, $\beta \in \mathbb{R}^p$, p >> n
- assumption of sparsity many components of β are o
- prior specification first on dimension *s*, then on subset $S \subset \{1, ..., p\}$ with |S| = s, finally on $\beta_S = \{\beta_i, i \in S\}$

$$\pi(eta,\mathsf{S})\propto\pi_p(|\mathsf{S}|)rac{\mathsf{1}}{\binom{p}{|\mathsf{S}|}}g_\mathsf{S}(eta_\mathsf{S})\delta_\mathsf{O}(eta_{\mathsf{S}^c})$$

• example

$$\pi_p(|\mathsf{S}|) \propto (cp^a)^{-s}, \quad \beta_j \sim \text{i.i.d. Laplace}$$

Castillo et al.

• example

$$\pi_p = \text{Bin}(p, r), \quad \beta_j \sim \text{i.i.d.} (1 - r)\delta_0 + r \text{ Laplace}, \quad r \sim \text{Beta}(1, p^u)$$

spike and slab

- under conditions on design matrix X
- and on the scale parameter in the Laplace prior

- $\inf\{\frac{||X\beta||_2}{||X|||\beta||_2} : |S_\beta| \le s\} > 0$
 - $\frac{||X||}{p} \le \lambda \le 2||X||(\log p)^{1/2}$
- + obtain various consistency results on posterior estimates of |S|, S and eta
- in particular, Bayesian credible sets for β are well-calibrated
- special case n = p, X = I: "sequence model" $Y_i \sim N(\beta_i, 1), i = 1, ..., n$

Stein's example

• prototype for nonparametric Bayes

• $y_i \sim N(\theta_i, 1), \quad i = 1, \dots, n; \quad \theta \text{ sparse}$

nonparametric Bayes

• prior specification first on dimension *s*, then on subset $S \subset \{1, ..., p\}$ with |S| = s, finally on $\theta_S = \{\theta_i, i \in S\}$

$$\pi(heta, \mathsf{S}) \propto \pi_p(|\mathsf{S}|) rac{\mathsf{1}}{\binom{p}{|\mathsf{S}|}} g_\mathsf{S}(heta_\mathsf{S}) \delta_\mathsf{O}(heta_\mathsf{S^c})$$

as above

$$\pi_p(|S|) \propto (cp^a)^{-s}, \quad \text{but } \theta_S \sim \text{ Laplace } \rightarrow N(Y_S, \sigma^2 \tau^{-1} I_{|S|})$$

• and tempered likelihood

generalized Bayes

$$\pi(\theta, \mathsf{S} \mid \mathsf{y}) \propto \{\mathsf{L}_n(\theta_\mathsf{S}; \mathsf{y})\}^{\boldsymbol{lpha}} \pi(\theta, \mathsf{S})$$

- posterior coverage for linear functions of $\boldsymbol{\theta}$

simpler than Castillo et al.

Signal strength

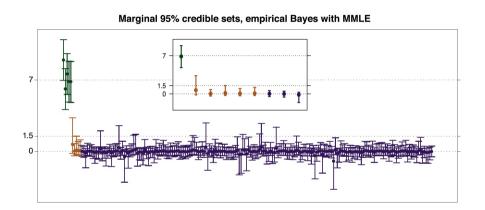


Figure 1: 95% marginal credible intervals based on the MMLE empirical Bayes method, constructed using the 2.5% and 97.5% quantiles, for a single observation Y^n of length n = 200 with $p_n = 10$ nonzero parameters, the first 5 (from the left) being 7 (green), the next 5 equal to 1.5 (orange); the remaining 190 parameters are coded (blue). The inserted plot zooms in on credible intervals 5 to 13, thus showing one large mean and

- posterior distribution
- fiducial probability
- confidence distribution
- structural probability
- significance function

- objective Bayes
- generalized fiducial inference

Hannig; Taraldsen

- confidence distributions and confidence curves Hjort, Schweder, Xie
- approximate significance functions

Brazzale et al 2007; Fraser & R 1993

belief functions

inferential models

Martin & Liu

high-dimensional inference and model selection

- "Nonpenalized variable selection in high-dimensional linear regression settings via generalized fiducial inference
- fiducial density obtained from likelihood function \times Jeffreys' prior $\times h(\theta)$
- $h(\theta)$ encodes a constraint on the parameter space that separates "small" values from "large ones"
- this enables them to show that their method will identify the correct model

- significance function approach identifies a pivotal quantity for parameter of interest
- built on likelihood ratio test

• when p is fixed, $r^*(\psi) \sim N(0, 1)$

•
$$r = \pm [2\{\ell(\hat{\psi}, \hat{\lambda}) - \ell(\psi, \hat{\lambda}_{\psi})\}]^{1/2}$$
, $q = (\hat{\psi} - \psi)j_{prof}^{1/2}(\hat{\psi})$ likelihood root, Wald statistic
• $\rho = \frac{|j_{\lambda\lambda}(\hat{\psi}, \hat{\lambda})|}{|j_{\lambda\lambda}(\psi, \hat{\lambda}_{\psi})|}$ nuisance parameters

$$r^*(\psi) = r(\psi) + \frac{1}{r(\psi)} \log\left\{\frac{q(\psi)\rho(\psi)}{r(\psi)}\right\} = r(\psi) + \frac{1}{r(\psi)} \log\left\{\frac{q(\psi)}{r(\psi)}\right\} + \frac{1}{r} \log\left\{\frac{\rho(\psi)}{r(\psi)}\right\}$$

data dependence suppressed

with error $O(n^{-3/2})$

• nuisance parameter adjustment grows as p^3/n information adjustment grows as p^2/n

$$p = O(n^{lpha}), lpha < 0.5$$

- sparse regression or sparse normal means
- prior on sparsity × prior on means or spike and slab; Castillo et al
- normal prior on means; Cauchy hyperprior on variance
 or
 horseshoe; Carvalho et al
- · empirical prior on means; tempered likelihood function

Martin & Ning

• consistency and asymptotic normality theorems re posterior for the means

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Summary

Statistical theory, reproducibility and data science

- dichotomizing conclusions based on *p*-values is not a good idea
- statistical science is more nuanced than that
- science rarely advances on the basis of a single study
- · posterior distributions need to be treated with care
- they can depend heavily on the prior, even when it seems uninformative
- several current versions of fiducial inference: confidence, significance, generalized fiducial
- "making a Bayesian omelette without cracking the Bayesian eggs"
- all these methods require a reduction of data and parameter space to a scalar dimension
- how do we do this ??
- ANU Mar 20 foundations

- · avoid apparent discoveries based on spurious patterns
- shed light on the structure of the problem
- obtain calibrated inferences about interpretable parameters
- provide a realistic assessment of precision
- understand when/why methods work/fail

- something that works
- gives 'sensible' answers
- not too sensitive to model assumptions
- computable in reasonable time
- provides interpretable parameters





Data Science Workflow - The Process for husiness-science in





Thank you!



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