

Identity for Statistics:

Calibration in Statistics

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May 1 2010
Fields Institute

www.utstat.utoronto.ca/dfraser/documents/fields10.pdf

What's up?

1	Statistics	1349	O
2	Identity	1763	B
3	Economist	1922	L
4	Theorem	1930	C
5	Priors	1937	N
6	Linear parameters	1958	Li
7	Curved parameters	1973	DSZ
8	Curved models	2010	
9	Calibration!		

1 Statistics: Why?

Why are we here? Statistics

MANY Thanks to organizers!

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Dumb
numbers!

The clock was set ticking
long before I knew!

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" " " " it as <u>wrong</u>	&	<u>condemned</u> it
" " " were <u>mystified</u>		

- an aura of the religious ... ?

The issues still pervade...: despite attempts to hide

"Bayes 1763"

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Deep things involved!

Beliefs ... re the earth!
... re how to think!

Toleration in statistics ... of contradictions?

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... intolerable in science

What do sensible people think of us?

2 Identity

20

How do others see Statistics?

- You say you are a Statistician! ... Reactions: #!&...
 - Used to be that way for Mathematicians (-25BP). . they fixed it!
 - What can we do?
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2 Identity

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- 'shoot ourselves in the foot' publicly!
- promote a religious view of our insights!

3. The Economist 2000 sept 28

In praise of Bayes Upbeat... "proponent's views..."

"... value of a statistical method ... apparent..."

"... results... easier to understand..."

"... clinical trials... faster"

"Not bad for an old dead white male"

Not much on: What the method is...

"... math. rule ... how you should change ... beliefs..."

Some "f" bashing...

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"Evidently there is life in The old reverend yet."

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4 The Theorem

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Good theorem: Two inputs $f(x)$, $f(y|x)$
one output $f(x|y)$
Inconvertible!

An application: one of inputs is missing

So you make one up! Do some cosmetics...

then claim the output is valid?

Even MAT 137 students can handle that!

Worse than " $\frac{0}{0}$ "!

Context:

There was a value... θ

" was a process $f(y;\theta)$

" was a consequent value y°

they are all in the past!

What do we know about the value... θ ?

Do we assert probability? On what basis?

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Not Bayes!
Name?

- 1. Real $\frac{\pi(\cdot)}{\pi(\cdot)}$ Known random source for the θ

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Subjective ← Opinion

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Does the Theorem apply to Application?

Case 1. Yes!

Case 3. No! ... but things 'sort of work'

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It is "Approximate confidence"

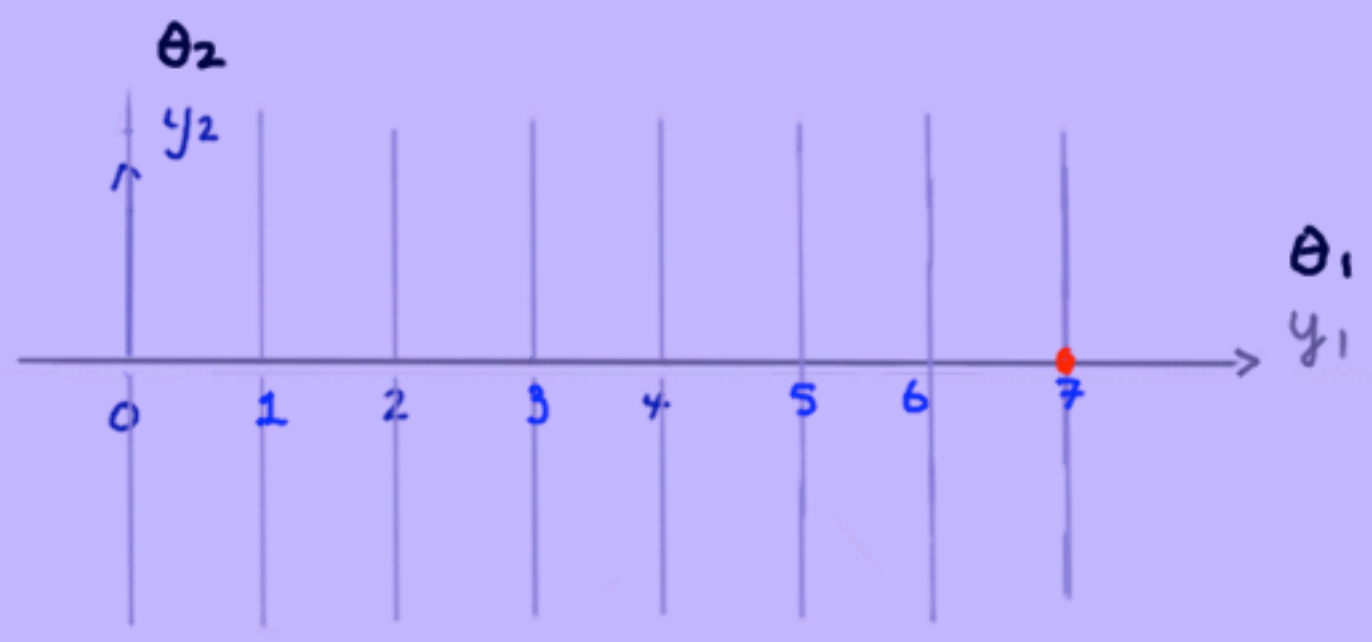
Laplace liked the answers!

... after all | $y = X\beta + \sigma z$
 | β, σ linear!

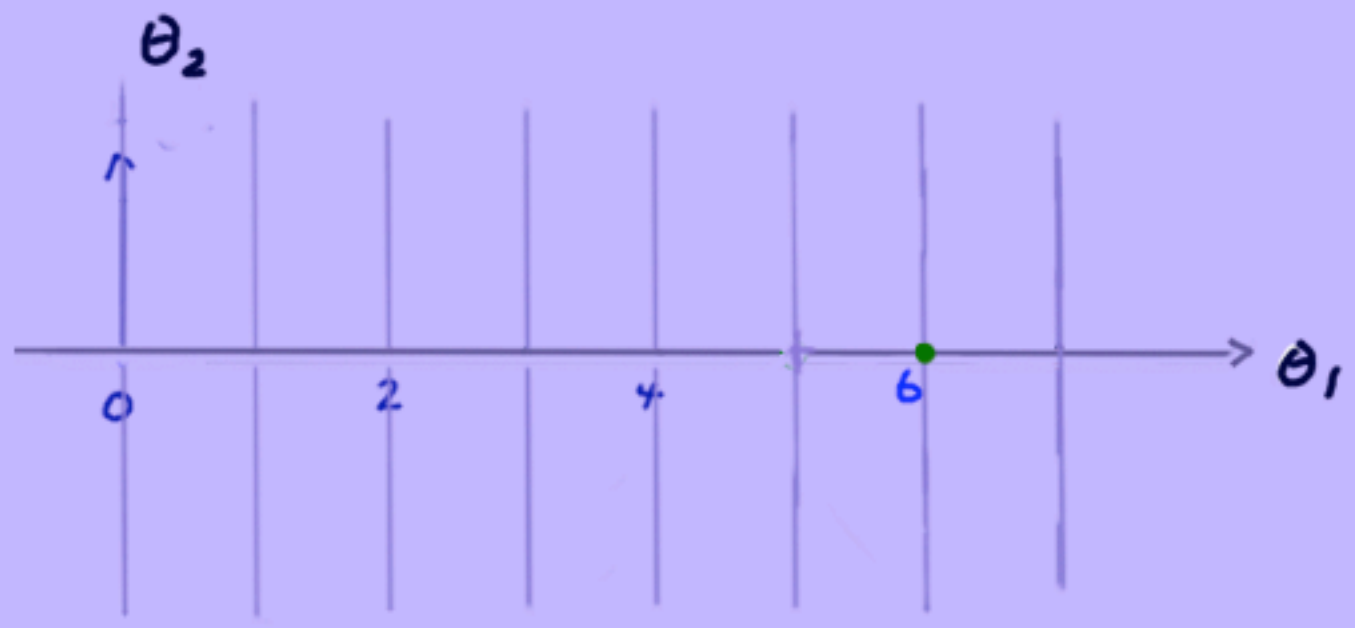
6 Linearity: $N(\theta; I)$ on R^2 : Contours of Interest $\psi(\theta) = \theta_1$

Linear

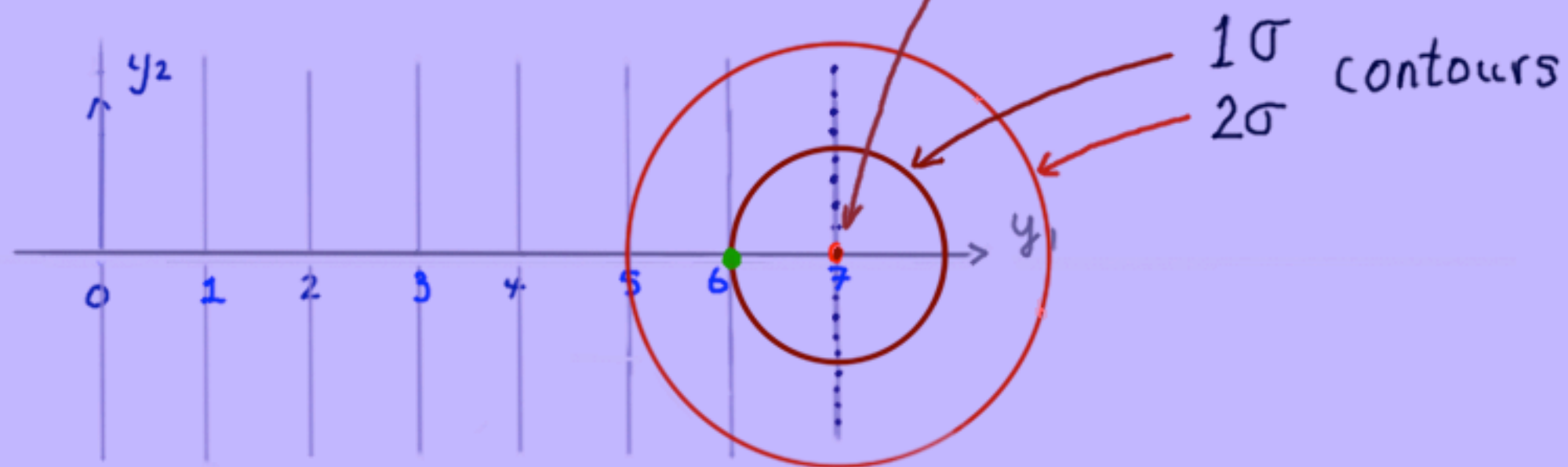
(i) What probability says:



(ii) What Bayes says:



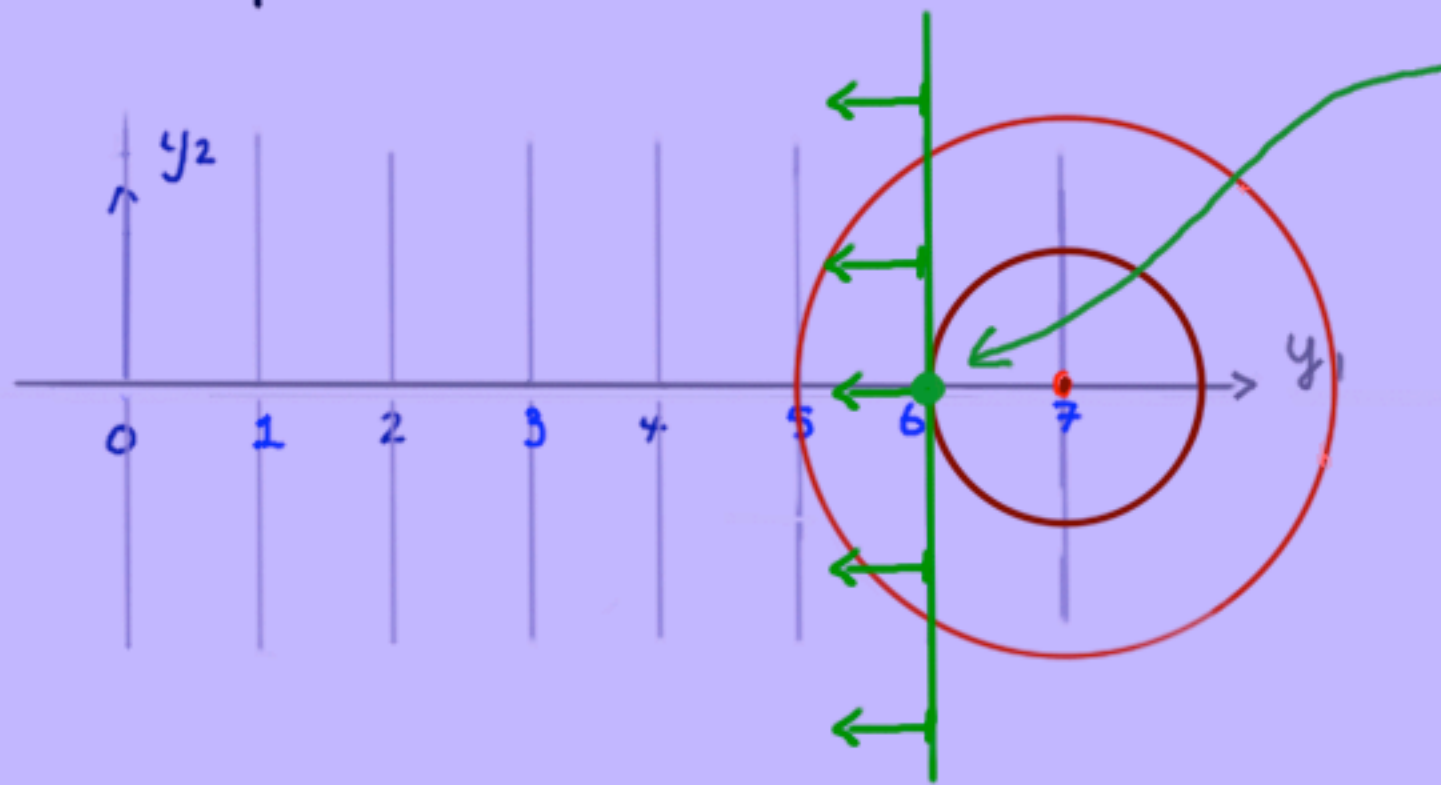
(i) What probability says: If $\theta_1 = 7$ then $y \sim N(\begin{pmatrix} 7 \\ \theta_2 \end{pmatrix}; I)$ $y_1 \sim N(7, 1)$



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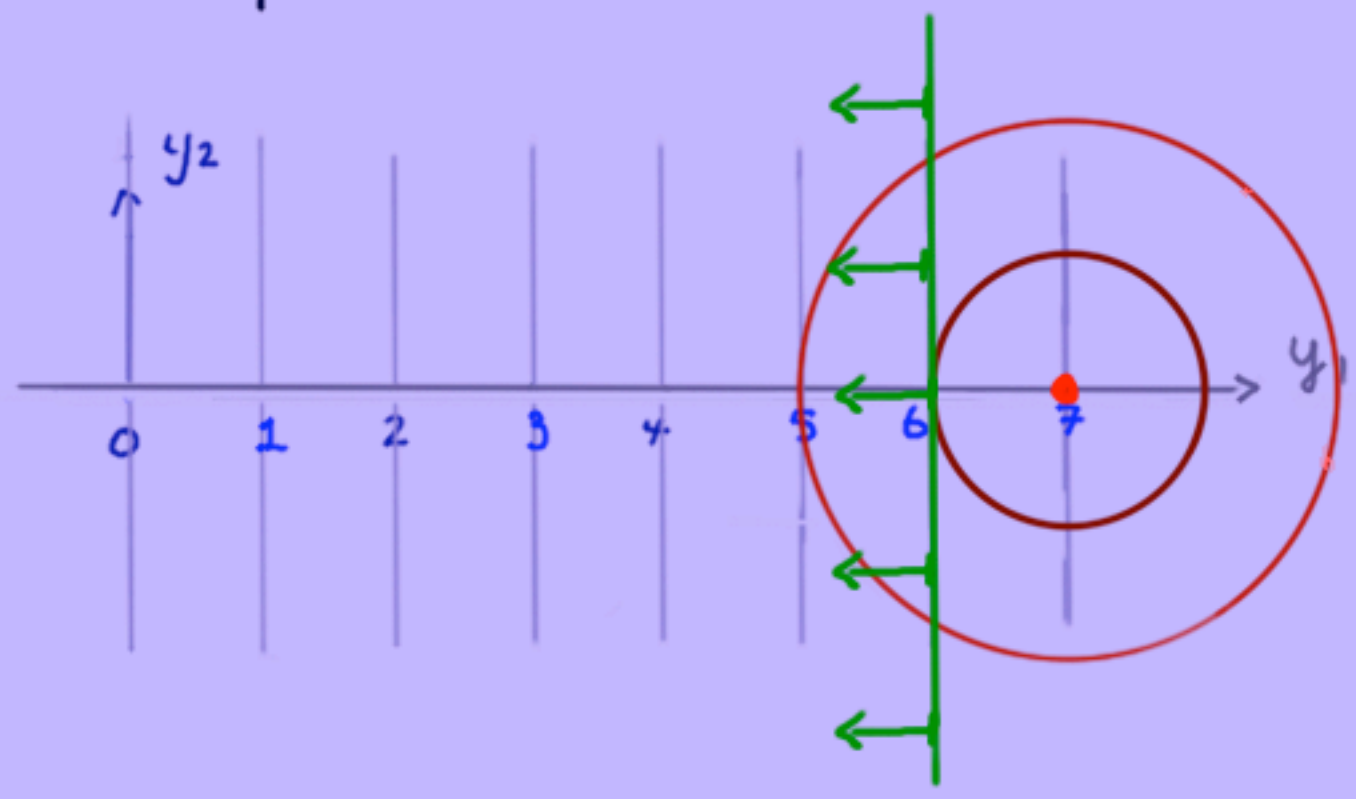
For data $y_1^o = 6 \dots$

$$\text{Prob left of data} = \Phi(-1) = \Phi\left(\frac{6-7}{1}\right) = \\ = p\text{-value} = 16\%$$

(ii) What Bayes says:

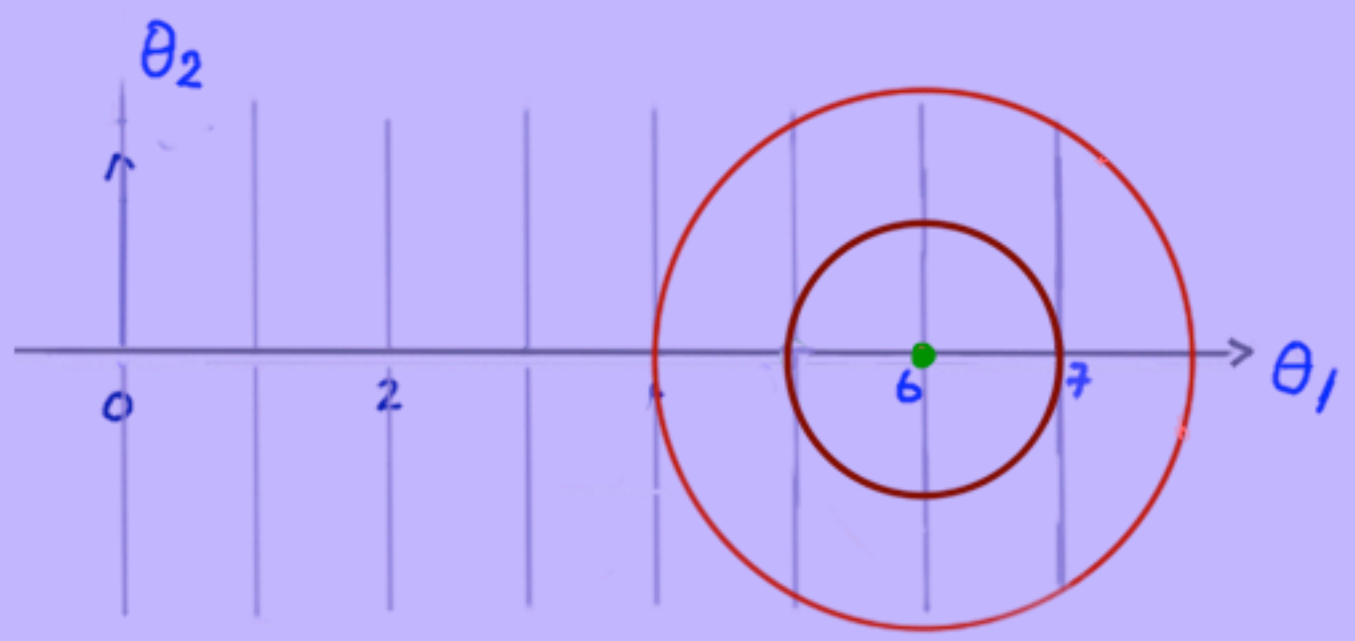


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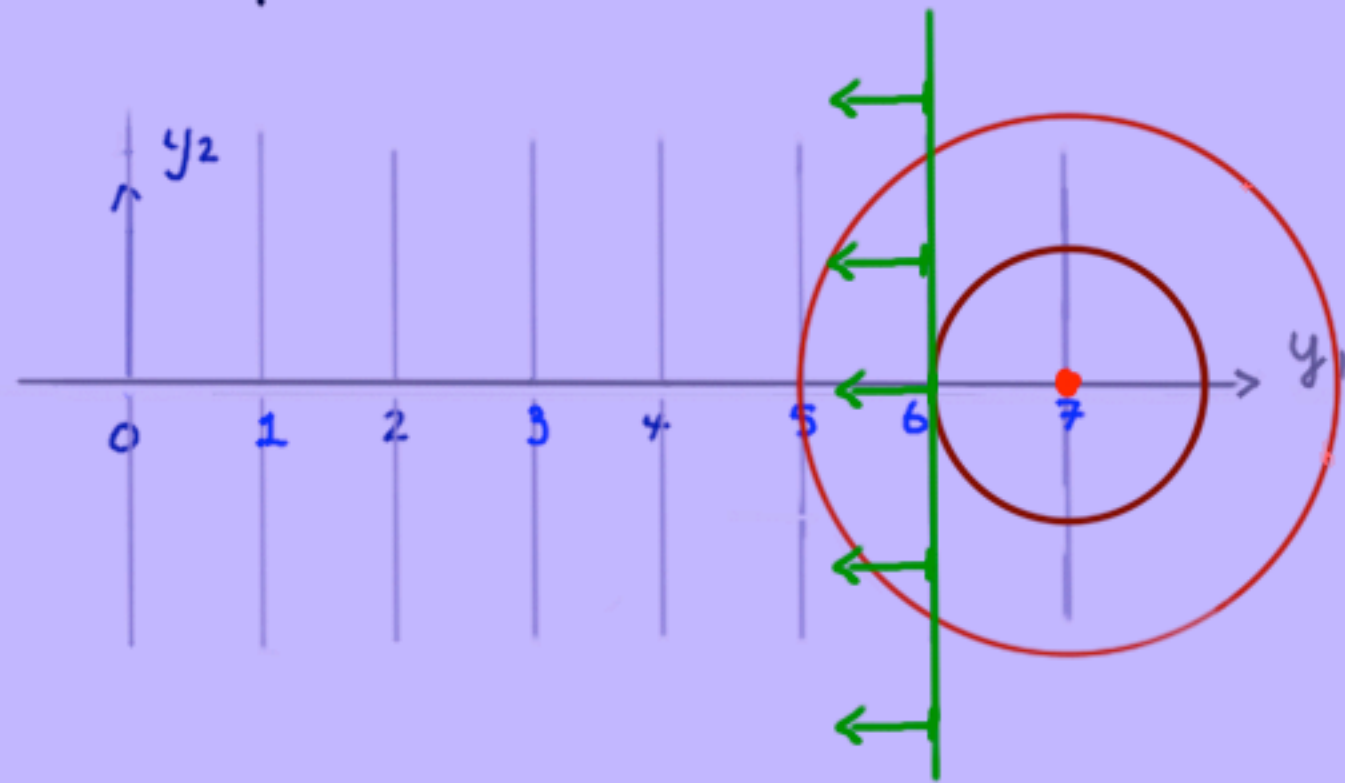


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(ii) What Bayes says: If $y^o = 6$ then $\theta \sim N\left\{\begin{pmatrix} 6 \\ 0 \end{pmatrix}; I\right\}$ $\theta_1 \sim N(6, 1)$



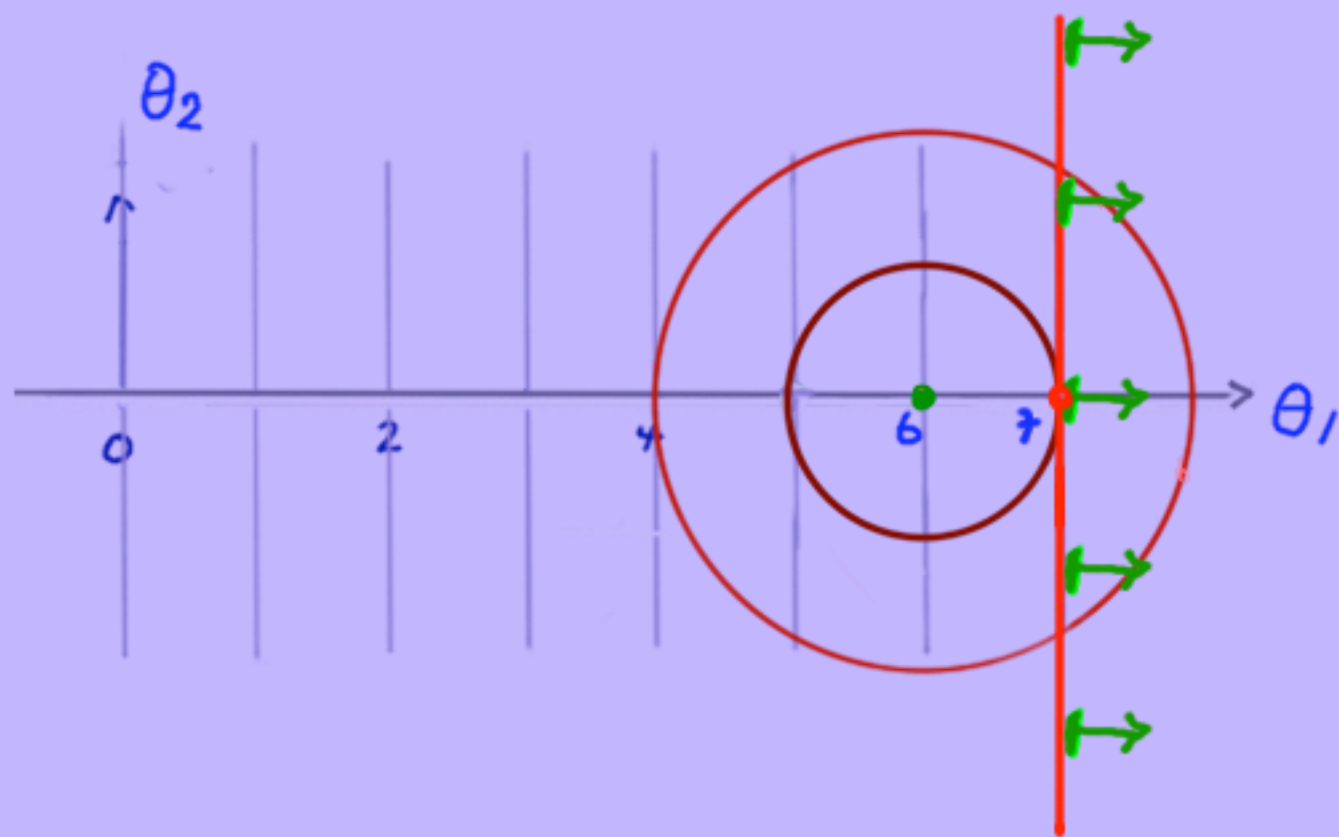
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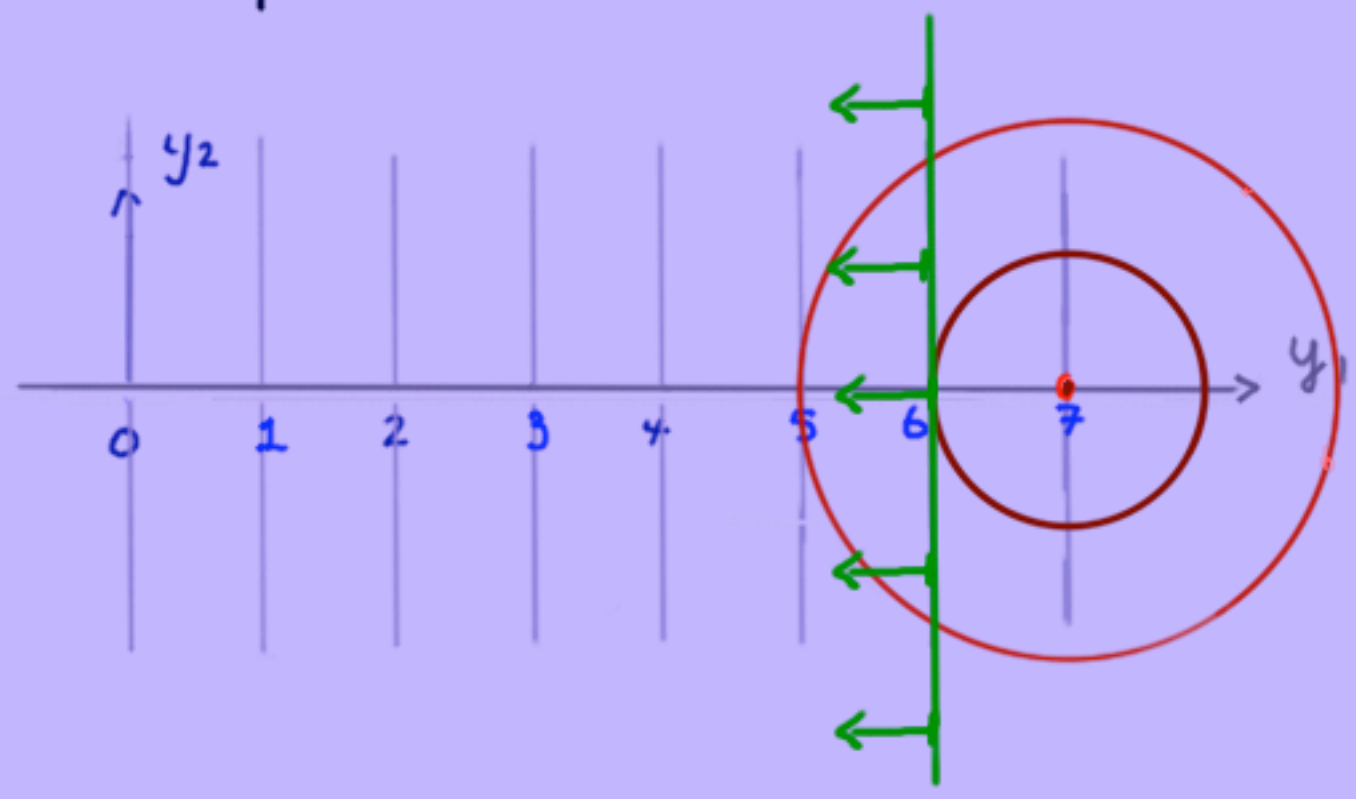
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For para. value $\theta_1 = 7 \dots$

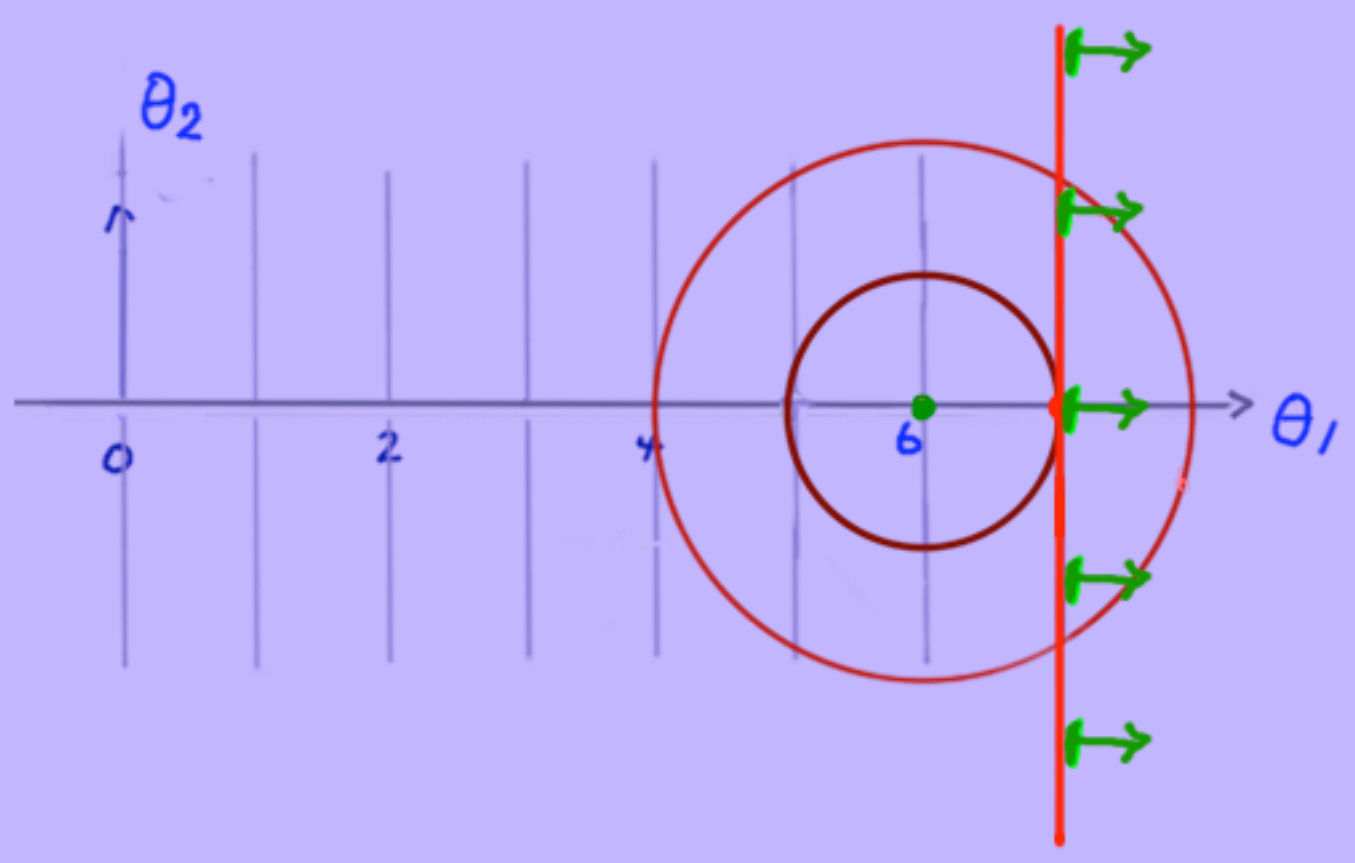
'Prob' larger than $\theta_1 = 7$ = $s\text{-value} = 16\%$ "posterior survivor value"

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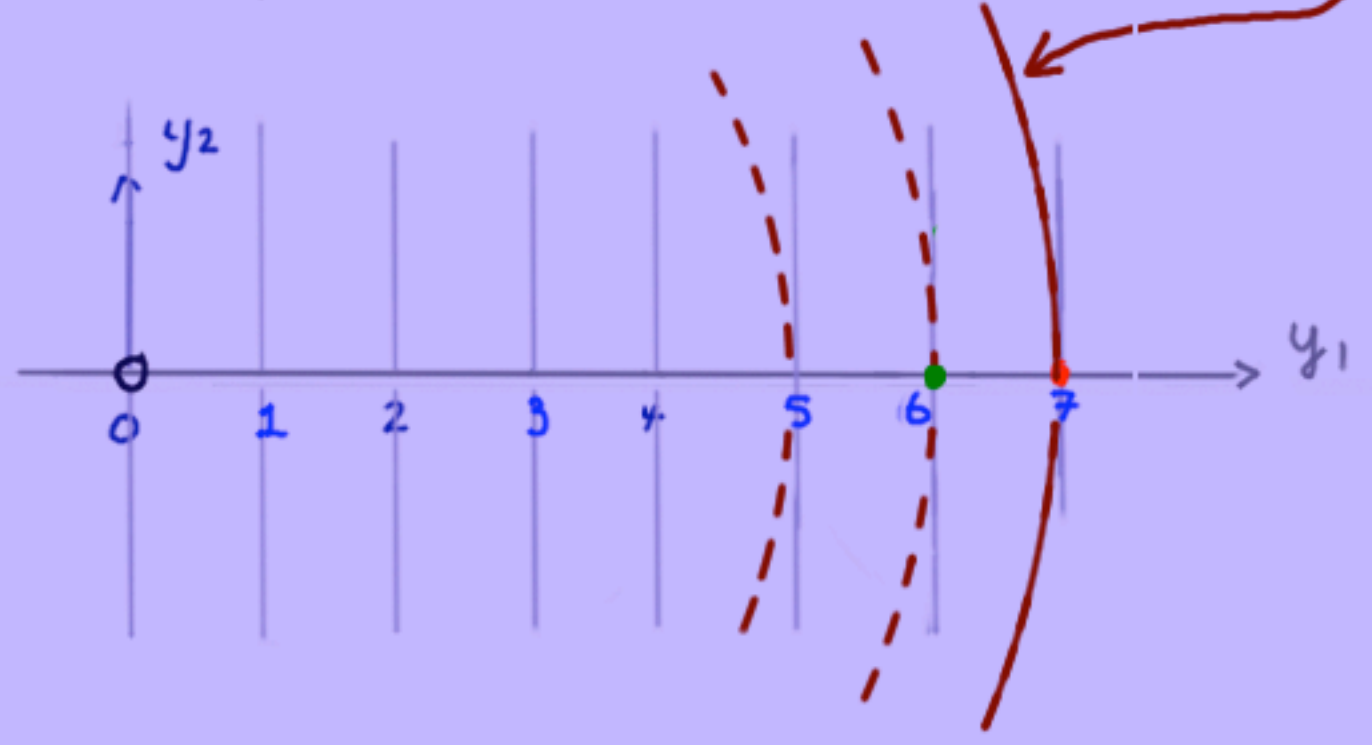
for para. value $\theta_1 = 7 \dots$
 'Prob' larger than $\theta_1 = 7$ } "posterior
 $= s\text{-value} = 16\%$ } survivor
 value"

They are equal! ... for any linear
 $16\% = 16\%$ parameter

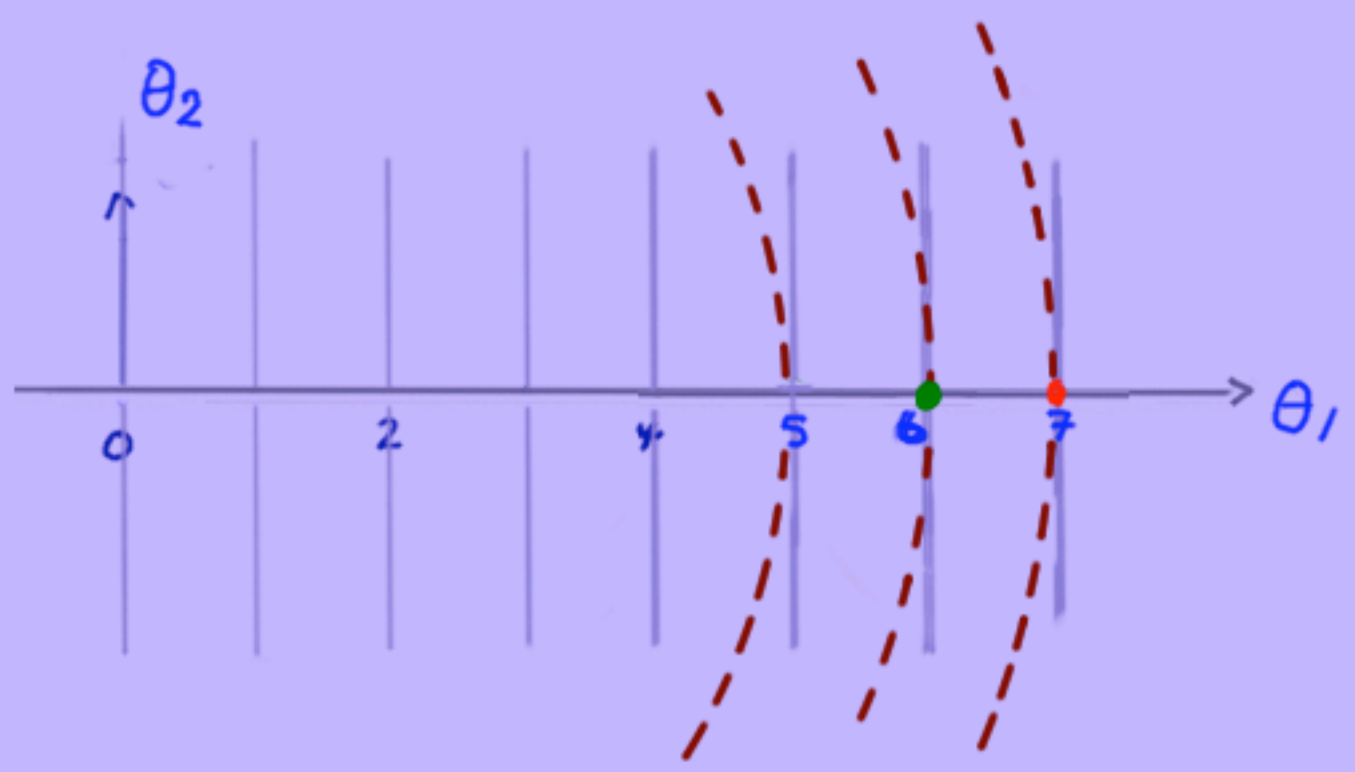
Bayes is "right on"!
 Bayes "works"!
 Bayes is easy, exact! **BUT...**

7 What about Curved parameters? Ex $\psi(\theta) = \{\theta_1^2 + \theta_2^2\}^{1/2}$ 70

(i) What probability says: If $\psi = 7$



(ii) What Bayes says: If $y^0 = 6$

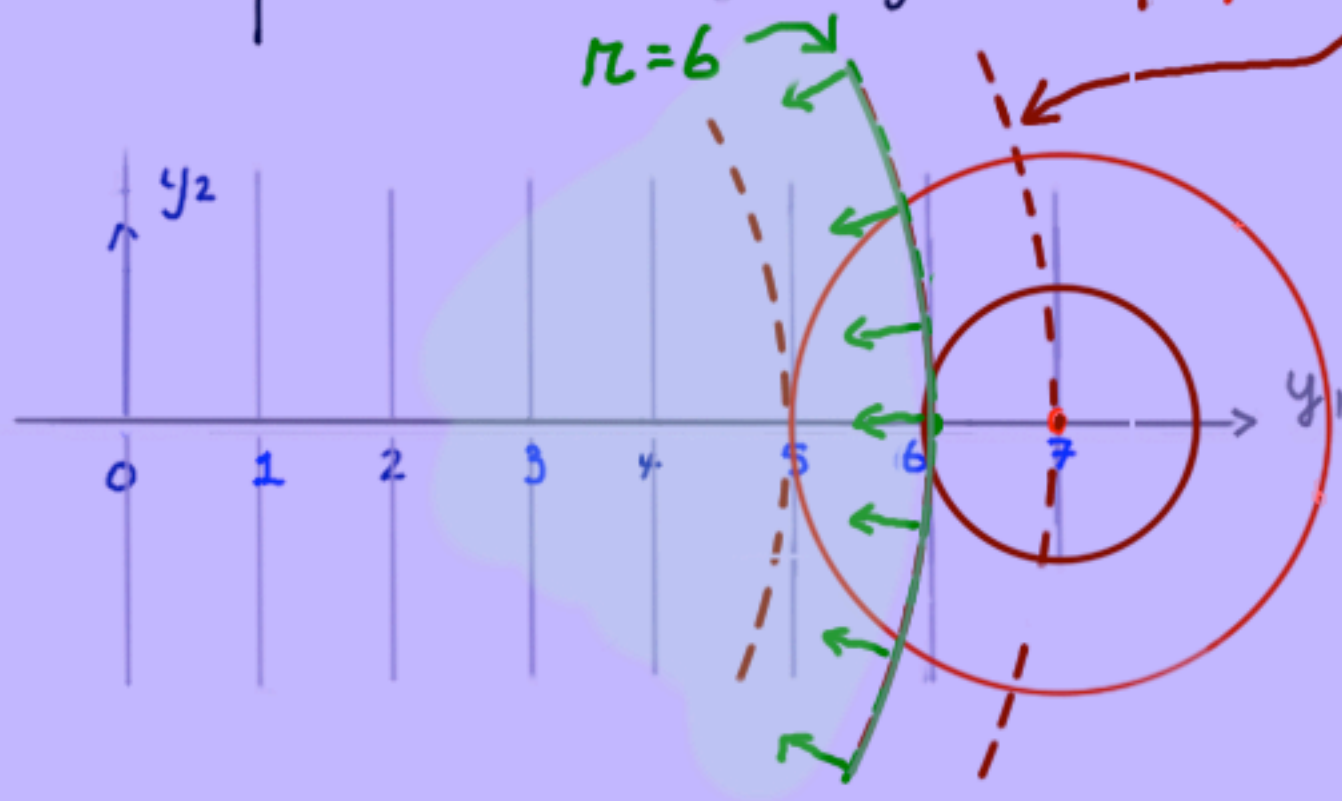


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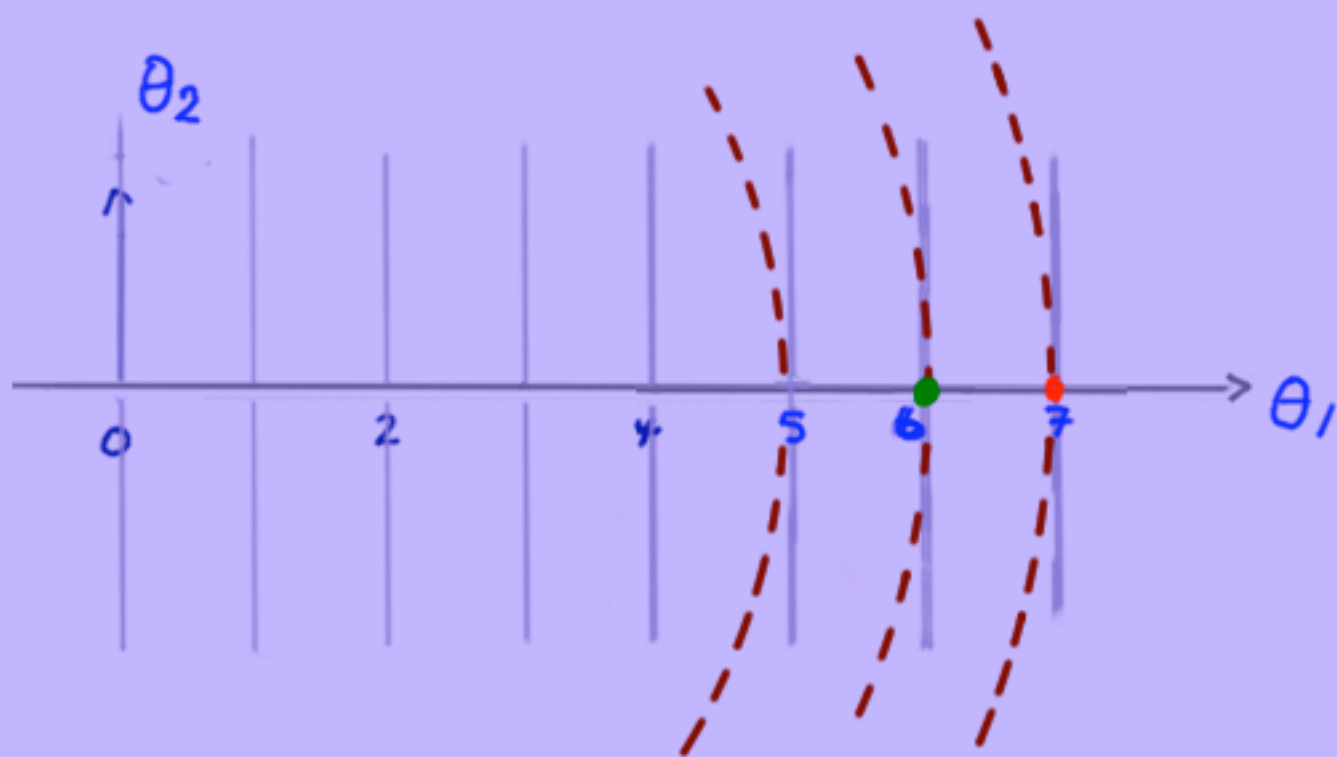
For data $y_i^0 = 6 \dots$

Prob left of data = $H_2(6^2; 7^2)$

= p-value = 14.1%



(ii) What Bayes does: If $y^0 = 6$



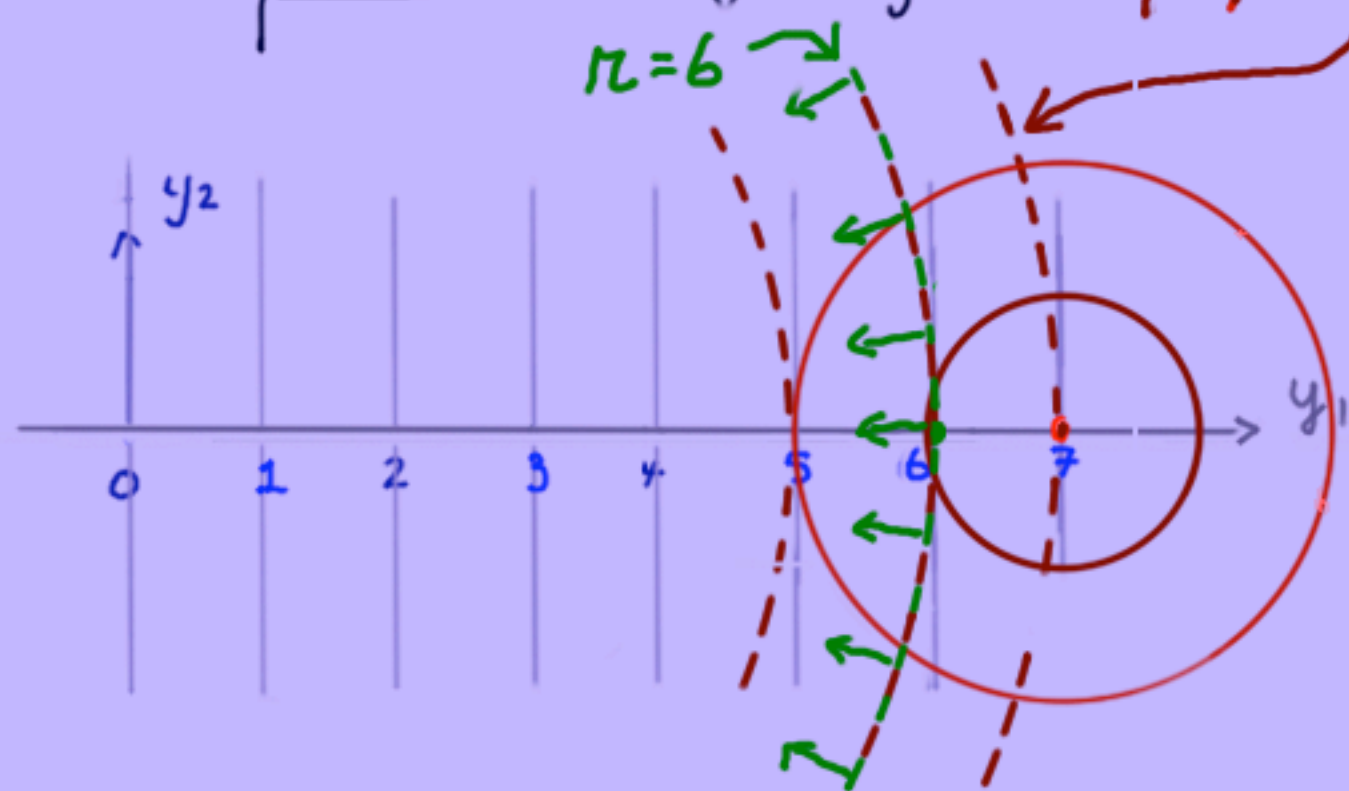
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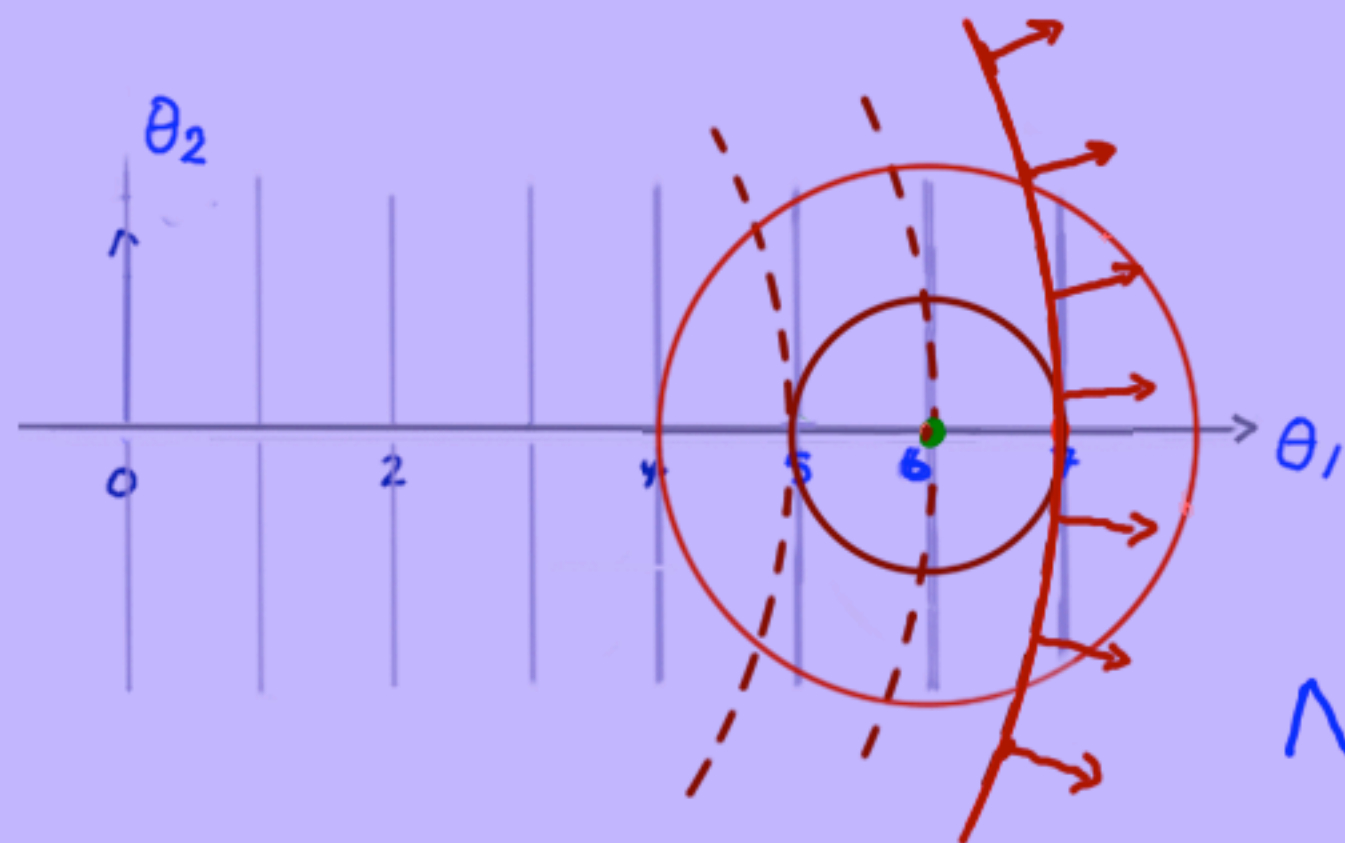
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(ii) What Bayes says: If $y^0 = 6$ then $\theta^2 \sim NC \chi^2$ with 2 df and $NC = 6^2$



'Prob' larger than $|\theta| = 7$

$$= 1 - H_2(7^2; 6^2)$$

$$= s\text{-value} = \underline{\underline{17.8\%}}$$

"posterior
survivor
value"

Not hard to see why

they are different:

- In nature of Bayes!

Curvature!

And... Assess $|\theta| \geq 7$ with other data points

Data y_i	4	5	6	7
p-value	.10%	1.9%	<u>14.1%</u>	47.1%
s-value	.18%	2.8%	<u>17.8%</u>	52.9%

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With positive curvature $\delta(\psi) > p(\psi) \dots$ always
 uniformly

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"Two ways of thinking of same problem?"

"Hidden" in DSZ 1973

"Paradigm" is broken!

8 Curved models!

Ex: $y \sim N(\theta, \sigma^2(\theta))$

$$\sigma^2(\theta) = 1 + \gamma \theta^2 / 2n$$

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$$\Phi(z_\beta) = \beta$$

Ex: $y \sim N(\theta, \sigma^2(\theta))$

$$\sigma^2(\theta) = 1 + \gamma \theta^2 / 2n$$

Linear $\gamma = 0$

Curved $\gamma > 0$

β -confidence
(lower bound)

$$\hat{\theta}_\beta = y - z_\beta$$

$$\hat{\theta}_\beta = y - z_\beta \left\{ 1 + \gamma \frac{(y - z_\beta)^2}{4n} \right\}$$

$$O(n^{-3/2})$$

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A "prior" cannot give this β -confidence quantile!

..... cannot convert likelihood to confidence!

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Stat. Sc.
247.pdf

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Bayes can't handle curvature!

DS 2 didn't broadcast the real message

and
Case 2
priors

No need to use opinion priors to analyze
unless statistics seems too hard!

Does it matter: Bayes can't handle curvature?

- a "number" is called a "probability"
 - and it doesn't have the performance property
 - Is it... "Wall St" deception?
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Stainforth, Allen, Tredger, Smith (2007) Phil Trans Roy Soc A365

Two weather models:

Flat priors for parameter

Simulations

Contradictory results

Different measurement processes

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- "... garbage in, garbage out."
- "The difficulty comes when you do not know what garbage looks like"

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...in Phil Trans. Roy. Soc. ?

...in The Economist ?

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Bayes posterior: Great for exploring with likelihood !

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The Tool Box needs a lot of calibration !

Some references

- Jeffreys (1939) Theory of Probability Oxford
- Neyman (1937) Phil Trans Roy Soc
- Jeffreys (1946) An invariant form ... Proc Roy Soc A
- Dawid Stone Zidek (1973) JRSSB
- Reid, F. (2010) Biometrika
- Stainforth, Allen, Tredger, Smith (2007) Phil Trans Roy Soc A365
- F., Reid, Marras, Yi (2010) JRSSB (Default priors)
- F., (2010) "Is Bayes posterior..." Stat Sc in review
- Fraser, F., Staicu (2010) Bernoulli to appear (Conditioning)

Some references

Jeffreys (1939) Theory of Probability Oxford
Neyman (1937) Phil Trans Roy Soc
Jeffreys (1946) An invariant form ... Proc Roy Soc A
Dawid Stone Zidek (1973) JRSSB
Reid, F. (2010) Biometrika 251. pdf
Stainforth, Allen, Tredger, Smith (2007) Phil Trans Roy Soc A365
F., Reid, Marras, Yi (2010) JRSSB (Default priors) 239. pdf
F., (2010) "Is Bayes posterior..." Stat Sc in review 247. pdf
Fraser, F., Staicu (2010) Bernoulli to appear (Conditioning) 240. pdf



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