

# Covariance Structure Approach to Within-Cases

```
/* grapefruit2.sas */
options linesize=79 pagesize=500 noovp formdlim='_';
title "Oneway ANOVA with repeated measures: Covariance Structure Approach";
title2 'Grapefruit data (Kutner et al. 5th ed. Prob 27.6)';

data grape1;
  infile 'grapefruit1.data' firstobs=2; /* Skip the labels */
  input store sales1-sales3;
  label sales1 = 'Sales at Price 1'
        sales2 = 'Sales at Price 2'
        sales3 = 'Sales at Price 3';
  d12 = sales1-sales2; d13 = sales1-sales3; d23=sales2-sales3;

proc glm;
  title3 'Multivariate approach with proc glm';
  model sales1-sales3 = ;
  repeated price / short summary mean;

data grape2;      /* This data set will have 3n cases. */
  set grape1;
  price = 1; sales = sales1; output; /* Output creates a new case. */
  price = 2; sales = sales2; output;
  price = 3; sales = sales3; output;
  keep store price sales;

proc print;
  title3 'Data set with one case per observation';

proc mixed;
  title3 'Proc mixed with unknown covariance structure';
  title4 'Compare F = 29.66 with df = 2, 6';
  class price;
  model sales = price;
  repeated / type=un subject=store r;

proc mixed;
  title3 'Proc mixed with compound symmetry cov. structure and contrasts';
  title4 'Compare F = 49.35 with df = 2, 14';
  class price;
  model sales = price;
  contrast '1vs2' price 1 -1 0;
  contrast '1vs3' price 1 0 -1;
  contrast '2vs3' price 0 1 -1;
  repeated / type=cs subject=store r;
```

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Oneway ANOVA with repeated measures: Covariance Structure Approach 1  
 Grapefruit data (Kutner et al. 5th ed. Prob 27.6)  
 Multivariate approach with proc glm

The GLM Procedure

Number of Observations Read 8  
 Number of Observations Used 8

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Skipping the univariate output ...

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Oneway ANOVA with repeated measures: Covariance Structure Approach 5  
 Grapefruit data (Kutner et al. 5th ed. Prob 27.6)  
 Multivariate approach with proc glm

The GLM Procedure

Repeated Measures Analysis of Variance

Repeated Measures Level Information

Dependent Variable	sales1	sales2	sales3
Level of price	1	2	3

MANOVA Test Criteria and Exact F Statistics  
 for the Hypothesis of no price Effect  
 H = Type III SSCP Matrix for price  
 E = Error SSCP Matrix

S=1 M=0 N=2

Statistic	Value	F Value	Num DF	Den DF	Pr > F
Wilks' Lambda	0.09185282	29.66	2	6	0.0008
Pillai's Trace	0.90814718	29.66	2	6	0.0008
Hotelling-Lawley Trace	9.88698145	29.66	2	6	0.0008
Roy's Greatest Root	9.88698145	29.66	2	6	0.0008

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The GLM Procedure

Repeated Measures Analysis of Variance

Univariate Tests of Hypotheses for Within Subject Effects

Source	DF	Type III SS	Mean Square	F Value	Pr > F
price	2	67.48083333	33.74041667	49.35	<.0001
Error(price)	14	9.57250000	0.68375000		

And skipping the remaining multivariate output.

Recall that the original data file looked like this:

Store	sales1	sales2	sales3
1	62.1	61.3	60.8
2	58.2	57.9	55.1
3	51.6	49.2	46.2
4	53.7	51.5	48.3
5	61.4	58.7	56.6
6	58.5	57.2	54.3
7	46.8	43.2	41.5
8	51.2	49.8	47.9

And here is the output from proc print:

Oneway ANOVA with repeated measures: Covariance Structure Approach 9  
Grapefruit data (Kutner et al. 5th ed. Prob 27.6)  
Data set with one case per observation

Obs	store	price	sales
1	1	1	62.1
2	1	2	61.3
3	1	3	60.8
4	2	1	58.2
5	2	2	57.9
6	2	3	55.1
7	3	1	51.6
8	3	2	49.2
9	3	3	46.2
10	4	1	53.7
11	4	2	51.5
12	4	3	48.3
13	5	1	61.4
14	5	2	58.7
15	5	3	56.6
16	6	1	58.5
17	6	2	57.2
18	6	3	54.3
19	7	1	46.8
20	7	2	43.2
21	7	3	41.5
22	8	1	51.2
23	8	2	49.8
24	8	3	47.9

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Oneway ANOVA with repeated measures: Covariance Structure Approach 10  
 Grapefruit data (Kutner et al. 5th ed. Prob 27.6)  
 Proc mixed with unknown covariance structure  
 Compare F = 29.66 with df = 2, 6

The Mixed Procedure

Model Information

Data Set	WORK.GRAPE2
Dependent Variable	sales
Covariance Structure	Unstructured
Subject Effect	store
Estimation Method	REML
Residual Variance Method	None
Fixed Effects SE Method	Model-Based
Degrees of Freedom Method	Between-Within

Class Level Information

Class	Levels	Values
price	3	1 2 3

Dimensions

Covariance Parameters	6
Columns in X	4
Columns in Z	0
Subjects	8
Max Obs Per Subject	3

Number of Observations

Number of Observations Read	24
Number of Observations Used	24
Number of Observations Not Used	0

Iteration History

Iteration	Evaluations	-2 Res Log Like	Criterion
0	1	141.05309845	
1	1	86.03317486	0.00000000

Convergence criteria met.

Estimated R Matrix for Subject 1

Row	Col1	Col2	Col3
1	29.6084	33.0114	34.0598
2	33.0114	37.5886	38.7000
3	34.0598	38.7000	40.6255

Covariance Parameter Estimates

Cov Parm	Subject	Estimate
UN(1,1)	store	29.6084
UN(2,1)	store	33.0114
UN(2,2)	store	37.5886
UN(3,1)	store	34.0598
UN(3,2)	store	38.7000
UN(3,3)	store	40.6255

Fit Statistics

-2 Res Log Likelihood	86.0
AIC (smaller is better)	98.0
AICC (smaller is better)	104.0
BIC (smaller is better)	98.5

Null Model Likelihood Ratio Test

DF	Chi-Square	Pr > ChiSq
5	55.02	<.0001

Type 3 Tests of Fixed Effects

Effect	Num DF	Den DF	F Value	Pr > F
price	2	7	34.60	0.0002

Compare F = 29.66 with df = 2, 6

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Oneway ANOVA with repeated measures: Covariance Structure Approach 11  
 Grapefruit data (Kutner et al. 5th ed. Prob 27.6)  
 Proc mixed with compound symmetry cov. structure and contrasts  
 Compare F = 49.35 with df = 2, 14

The Mixed Procedure

Model Information

Data Set	WORK.GRAPE2
Dependent Variable	sales
Covariance Structure	Compound Symmetry
Subject Effect	store
Estimation Method	REML
Residual Variance Method	Profile
Fixed Effects SE Method	Model-Based
Degrees of Freedom Method	Between-Within

Class Level Information

Class	Levels	Values
price	3	1 2 3

Dimensions

Covariance Parameters	2
Columns in X	4
Columns in Z	0
Subjects	8
Max Obs Per Subject	3

Number of Observations

Number of Observations Read	24
Number of Observations Used	24
Number of Observations Not Used	0

Iteration History

Iteration	Evaluations	-2 Res Log Like	Criterion
0	1	141.05309845	
1	1	93.18551859	0.00000000

Convergence criteria met.

Estimated R Matrix for Subject 1

Row	Col1	Col2	Col3
1	35.9408	35.2571	35.2571
2	35.2571	35.9408	35.2571
3	35.2571	35.2571	35.9408

Covariance Parameter Estimates

Cov Parm	Subject	Estimate
CS	store	35.2571
Residual		0.6838

Fit Statistics

-2 Res Log Likelihood	93.2
AIC (smaller is better)	97.2
AICC (smaller is better)	97.9
BIC (smaller is better)	97.3

Null Model Likelihood Ratio Test

DF	Chi-Square	Pr > ChiSq
1	47.87	<.0001

Type 3 Tests of Fixed Effects

Effect	Num DF	Den DF	F Value	Pr > F
price	2	14	49.35	<.0001

Contrasts

Label	Num DF	Den DF	F Value	Pr > F
1vs2	1	14	19.75	0.0006
1vs3	1	14	98.34	<.0001
2vs3	1	14	29.95	<.0001

# Eating Norm Study

```
/dos/brunner/442f09/lecture > head RepeatPliner.data
ID,cdnNorm,cdnOrder,ResEater,amtEatC,amtEatA,fullc,fulla,deptimec,deptimea
8,0.0,0.0,1.0,16.00,11.00,2.00,4.00,2.30,4.30
102,0.0,0.0,1.0,12.00,12.00,1.00,1.00,17.25,5.25
106,0.0,0.0,2.0,12.00,13.00,1.00,1.00,2.90,3.40
12,0.0,0.0,1.0,11.00,11.00,1.00,1.00,4.75,7.25
14,0.0,0.0,1.0,10.00,7.00,1.00,1.00,18.12,5.12
88,0.0,0.0,2.0,8.50,10.00,3.00,5.00,2.93,2.93
108,0.0,0.0,1.0,8.00,11.00,1.00,1.00,16.00,16.00
19,0.0,0.0,2.0,6.00,14.00,1.00,2.00,7.88,7.38
20,0.0,0.0,1.0,6.00,9.00,3.00,4.00,1.77,3.77
```

```
/* eatingnorm.sas */
options linesize=79 pagesize=500 noovp formdlim='_' nodate;
title 'Social facilitation in eating: ANCOVA with time-varying covariates';

proc format;
  value ofmt 0 = 'AloneConfederate' 1 = 'ConfederateAlone';
  value amtfmt 0 = 'A little' 1 = 'A lot';

data hungry;
  infile 'RepeatPliner.data' firstobs=2 delimiter=',';
  input ID cdnNorm cdnOrder ResEater amtEatC amtEatA fullC fullA deptimeC
        deptimeA;
  label
    cdnOrder = 'Order'
    cdnNorm = 'Amount eaten by Confederate'
    amtEatC = 'Amount eaten with confederate present'
    amtEatA = 'Amount eaten with confederate absent'
    fullC = 'Rated fullness before eating, confederate present'
    fullA = 'Rated fullness before eating, confederate absent'
    deptimeC = 'Deprivation time, confederate present'
    deptimeA = 'Deprivation time, confederate absent';
  format cdnOrder ofmt.;
  format cdnNorm amtfmt.;

proc freq;
  tables cdnOrder*cdnNorm / norow nocol nopercent missing;
```



```

data fressen; /* Separate cases for confederate present, absent */
set hungry;
confed = 'Present';
    amtEat = amtEatC; full = fullC; deptime = deptimeC; output;
confed = 'Absent';
    amtEat = amtEatA; full = fullA; deptime = deptimeA; output;
keep ID cdnNorm cdnOrder confed amtEat full deptime;
label
    cdnOrder = 'Order'
    cdnNorm = 'Amount eaten by Confederate'
    amtEat = 'Amount eaten'
    full = 'Rated fullness before eating'
    deptime = 'Food Deprivation time';
format cdnOrder ofmt.;
format cdnNorm amtfmt.;

proc print;

proc mixed;
title2 'Covariates: Deprivation time and rated fullness';
class cdnOrder cdnNorm confed;
model amtEat = deptime full cdnOrder|cdnNorm|confed;
repeated / type=un subject=id r;
lsmeans cdnOrder|cdnNorm|confed;

```

Social facilitation in eating: ANCOVA with time-varying covariates 1

The FREQ Procedure

Table of cdnOrder by cdnNorm

cdnOrder(Order)	cdnNorm(Amount eaten by Confederate)		Total
	A little	A lot	
AloneConfederate	17	19	36
ConfederateAlone	20	18	38
Total	37	37	74

Social facilitation in eating: ANCOVA with time-varying covariates 2

Obs	ID	cdnNorm	cdnOrder	confed	amt Eat	full	deptime
1	8	A little	AloneConfederate	Present	16.0	2	2.30
2	8	A little	AloneConfederate	Absent	11.0	4	4.30
3	102	A little	AloneConfederate	Present	12.0	1	17.25
4	102	A little	AloneConfederate	Absent	12.0	1	5.25
5	106	A little	AloneConfederate	Present	12.0	1	2.90
6	106	A little	AloneConfederate	Absent	13.0	1	3.40

7	12	A little	AloneConfederate	Present	11.0	1	4.75
8	12	A little	AloneConfederate	Absent	11.0	1	7.25
9	14	A little	AloneConfederate	Present	10.0	1	18.12
10	14	A little	AloneConfederate	Absent	7.0	1	5.12

. . .

145	41	A lot	ConfederateAlone	Present	4.0	1	3.48
146	41	A lot	ConfederateAlone	Absent	5.0	3	2.98
147	77	A lot	ConfederateAlone	Present	4.0	1	2.95
148	77	A lot	ConfederateAlone	Absent	5.0	1	2.95

Social facilitation in eating: ANCOVA with time-varying covariates 3  
Covariates: Deprivation time and rated fullness

The Mixed Procedure

Model Information

Data Set	WORK.FRESSEN
Dependent Variable	amtEat
Covariance Structure	Unstructured
Subject Effect	ID
Estimation Method	REML
Residual Variance Method	None
Fixed Effects SE Method	Model-Based
Degrees of Freedom Method	Between-Within

Class Level Information

Class	Levels	Values
cdnOrder	2	AloneConfederate ConfederateAlone
cdnNorm	2	A little A lot
confed	2	Absent Present

Dimensions

Covariance Parameters	3
Columns in X	29
Columns in Z	0
Subjects	74
Max Obs Per Subject	2

Number of Observations

Number of Observations Read	148
Number of Observations Used	148
Number of Observations Not Used	0

Iteration History

Iteration	Evaluations	-2 Res Log Like	Criterion
0	1	876.26433335	
1	2	821.28897703	0.00000037
2	1	821.28887267	0.00000000

Convergence criteria met.

Estimated R Matrix  
for Subject 1

Row	Col1	Col2
1	24.6631	19.1859
2	19.1859	27.0831

Covariance Parameter Estimates

Cov Parm	Subject	Estimate
UN(1,1)	ID	24.6631
UN(2,1)	ID	19.1859
UN(2,2)	ID	27.0831

Fit Statistics

-2 Res Log Likelihood	821.3
AIC (smaller is better)	827.3
AICC (smaller is better)	827.5
BIC (smaller is better)	834.2

Null Model Likelihood Ratio Test

DF	Chi-Square	Pr > ChiSq
2	54.98	<.0001

Type 3 Tests of Fixed Effects

Effect	Num DF	Den DF	F Value	Pr > F
deptime	1	70	0.10	0.7537
full	1	70	4.17	0.0450
cdnOrder	1	70	0.01	0.9187
cdnNorm	1	70	10.40	0.0019
cdnOrder*cdnNorm	1	70	0.41	0.5258
confed	1	70	4.98	0.0289
cdnOrder*confed	1	70	5.57	0.0210
cdnNorm*confed	1	70	14.28	0.0003
cdnOrd*cdnNor*confed	1	70	2.11	0.1506

Least Squares Means

Effect	confed	Order	Amount eaten by Confederate	Estimate
cdnOrder		AloneConfederate		9.7580
cdnOrder		ConfederateAlone		9.8717
<b>cdnNorm</b>			<b>A little</b>	<b>8.0104</b>
<b>cdnNorm</b>			<b>A lot</b>	<b>11.6193</b>
cdnOrder*cdnNorm		AloneConfederate	A little	8.3069
cdnOrder*cdnNorm		AloneConfederate	A lot	11.2091
cdnOrder*cdnNorm		ConfederateAlone	A little	7.7140
cdnOrder*cdnNorm		ConfederateAlone	A lot	12.0295
<b>confed</b>	<b>Absent</b>			<b>10.3000</b>
<b>confed</b>	<b>Present</b>			<b>9.3297</b>
<b>cdnOrder*confed</b>	<b>Absent</b>	<b>AloneConfederate</b>		<b>9.7403</b>
<b>cdnOrder*confed</b>	<b>Present</b>	<b>AloneConfederate</b>		<b>9.7757</b>
<b>cdnOrder*confed</b>	<b>Absent</b>	<b>ConfederateAlone</b>		<b>10.8596</b>
<b>cdnOrder*confed</b>	<b>Present</b>	<b>ConfederateAlone</b>		<b>8.8838</b>
<b>cdnNorm*confed</b>	<b>Absent</b>		<b>A little</b>	<b>9.3216</b>
<b>cdnNorm*confed</b>	<b>Present</b>		<b>A little</b>	<b>6.6992</b>
<b>cdnNorm*confed</b>	<b>Absent</b>		<b>A lot</b>	<b>11.2783</b>
<b>cdnNorm*confed</b>	<b>Present</b>		<b>A lot</b>	<b>11.9603</b>
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A little	9.4298
cdnOrd*cdnNor*confed	Present	AloneConfederate	A little	7.1839
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A lot	10.0508
cdnOrd*cdnNor*confed	Present	AloneConfederate	A lot	12.3674
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A little	9.2134
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A little	6.2145
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A lot	12.5058
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A lot	11.5531

Least Squares Means

Effect	confed	Order	Amount eaten by Confederate	Standard Error	DF
cdnOrder		AloneConfederate		0.7939	70
cdnOrder		ConfederateAlone		0.7724	70
cdnNorm			A little	0.7880	70
cdnNorm			A lot	0.7851	70
cdnOrder*cdnNorm		AloneConfederate	A little	1.1619	70
cdnOrder*cdnNorm		AloneConfederate	A lot	1.0942	70
cdnOrder*cdnNorm		ConfederateAlone	A little	1.0626	70
cdnOrder*cdnNorm		ConfederateAlone	A lot	1.1215	70
confed	Absent			0.6078	70
confed	Present			0.5799	70
cdnOrder*confed	Absent	AloneConfederate		0.8721	70
cdnOrder*confed	Present	AloneConfederate		0.8308	70
cdnOrder*confed	Absent	ConfederateAlone		0.8475	70
cdnOrder*confed	Present	ConfederateAlone		0.8094	70
cdnNorm*confed	Absent		A little	0.8745	70
cdnNorm*confed	Present		A little	0.8213	70
cdnNorm*confed	Absent		A lot	0.8591	70
cdnNorm*confed	Present		A lot	0.8233	70
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A little	1.2841	70
cdnOrd*cdnNor*confed	Present	AloneConfederate	A little	1.2138	70
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A lot	1.2025	70
cdnOrd*cdnNor*confed	Present	AloneConfederate	A lot	1.1445	70
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A little	1.1685	70
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A little	1.1110	70
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A lot	1.2283	70
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A lot	1.1747	70

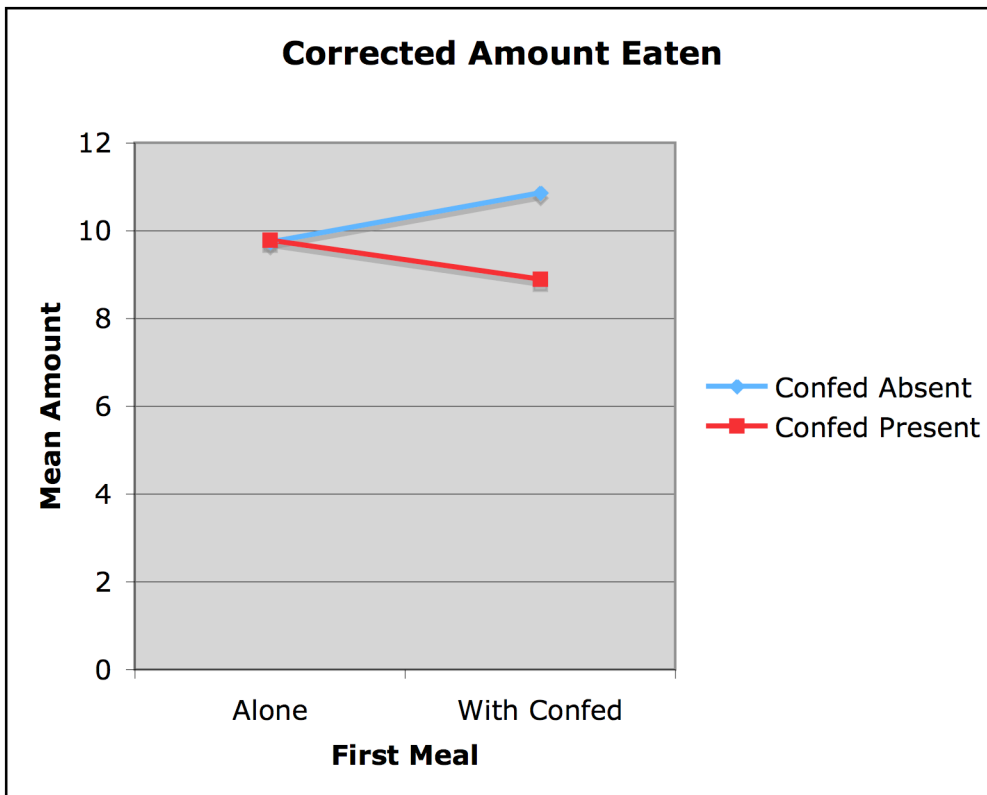
Least Squares Means

Effect	confed	Order	Amount eaten by Confederate	t Value	Pr >  t
cdnOrder		AloneConfederate		12.29	<.0001
cdnOrder		ConfederateAlone		12.78	<.0001
cdnNorm			A little	10.17	<.0001
cdnNorm			A lot	14.80	<.0001
cdnOrder*cdnNorm		AloneConfederate	A little	7.15	<.0001
cdnOrder*cdnNorm		AloneConfederate	A lot	10.24	<.0001
cdnOrder*cdnNorm		ConfederateAlone	A little	7.26	<.0001
cdnOrder*cdnNorm		ConfederateAlone	A lot	10.73	<.0001
confed	Absent			16.95	<.0001
confed	Present			16.09	<.0001
cdnOrder*confed	Absent	AloneConfederate		11.17	<.0001
cdnOrder*confed	Present	AloneConfederate		11.77	<.0001
cdnOrder*confed	Absent	ConfederateAlone		12.81	<.0001
cdnOrder*confed	Present	ConfederateAlone		10.98	<.0001
cdnNorm*confed	Absent		A little	10.66	<.0001
cdnNorm*confed	Present		A little	8.16	<.0001
cdnNorm*confed	Absent		A lot	13.13	<.0001
cdnNorm*confed	Present		A lot	14.53	<.0001
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A little	7.34	<.0001
cdnOrd*cdnNor*confed	Present	AloneConfederate	A little	5.92	<.0001
cdnOrd*cdnNor*confed	Absent	AloneConfederate	A lot	8.36	<.0001
cdnOrd*cdnNor*confed	Present	AloneConfederate	A lot	10.81	<.0001
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A little	7.88	<.0001
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A little	5.59	<.0001
cdnOrd*cdnNor*confed	Absent	ConfederateAlone	A lot	10.18	<.0001
cdnOrd*cdnNor*confed	Present	ConfederateAlone	A lot	9.84	<.0001

Need Two Plots

Effect	confed	Order	Amount eaten by Confederate	Estimate
<b>cdnOrder*confed</b>	<b>Absent</b>	<b>AloneConfederate</b>		<b>9.7403</b>
<b>cdnOrder*confed</b>	<b>Present</b>	<b>AloneConfederate</b>		<b>9.7757</b>
<b>cdnOrder*confed</b>	<b>Absent</b>	<b>ConfederateAlone</b>		<b>10.8596</b>
<b>cdnOrder*confed</b>	<b>Present</b>	<b>ConfederateAlone</b>		<b>8.8838</b>

	First Meal	
	Alone	With Confed
Confed Absent	<b>9.7403</b>	<b>10.8596</b>
Confed Present	<b>9.7757</b>	<b>8.8838</b>



Effect	confed	Order	Amount eaten by Confederate	Estimate
cdnNorm*confed	Absent		A little	9.3216
cdnNorm*confed	Present		A little	6.6992
cdnNorm*confed	Absent		A lot	11.2783
cdnNorm*confed	Present		A lot	11.9603

