

Name _____

Student Number _____

STA 431 Quiz 1

1. (5 points) Let the random variable x have expected value μ_x , let the random variable y have expected value μ_y , and let a be a non-zero constant. Circle one the of following statements and prove it, *using the definition of covariance* from the formula sheet.

$$\text{Cov}(ax, y) = a^2\text{Cov}(x, y), \quad \text{Cov}(ax, y) = a\text{Cov}(x, y), \quad \text{Cov}(ax, y) = \text{Cov}(x, y), \quad \text{Cov}(ax, y) = 0$$

2. (5 points) Let

$$y_1 = \alpha_1 + \beta_1 x + \epsilon_1$$

$$y_2 = \alpha_2 + \beta_2 x + \epsilon_2,$$

where $E(x) = \mu$, $Var(x) = \sigma_x^2$, $E(\epsilon_1) = E(\epsilon_2) = 0$, $Var(\epsilon_1) = \sigma_1^2$ and $Var(\epsilon_2) = \sigma_2^2$. The random variables x , ϵ_1 and ϵ_2 are independent. Using anything you wish from the formula sheet, calculate $Cov(y_1, y_2)$. **Circle your final answer.**