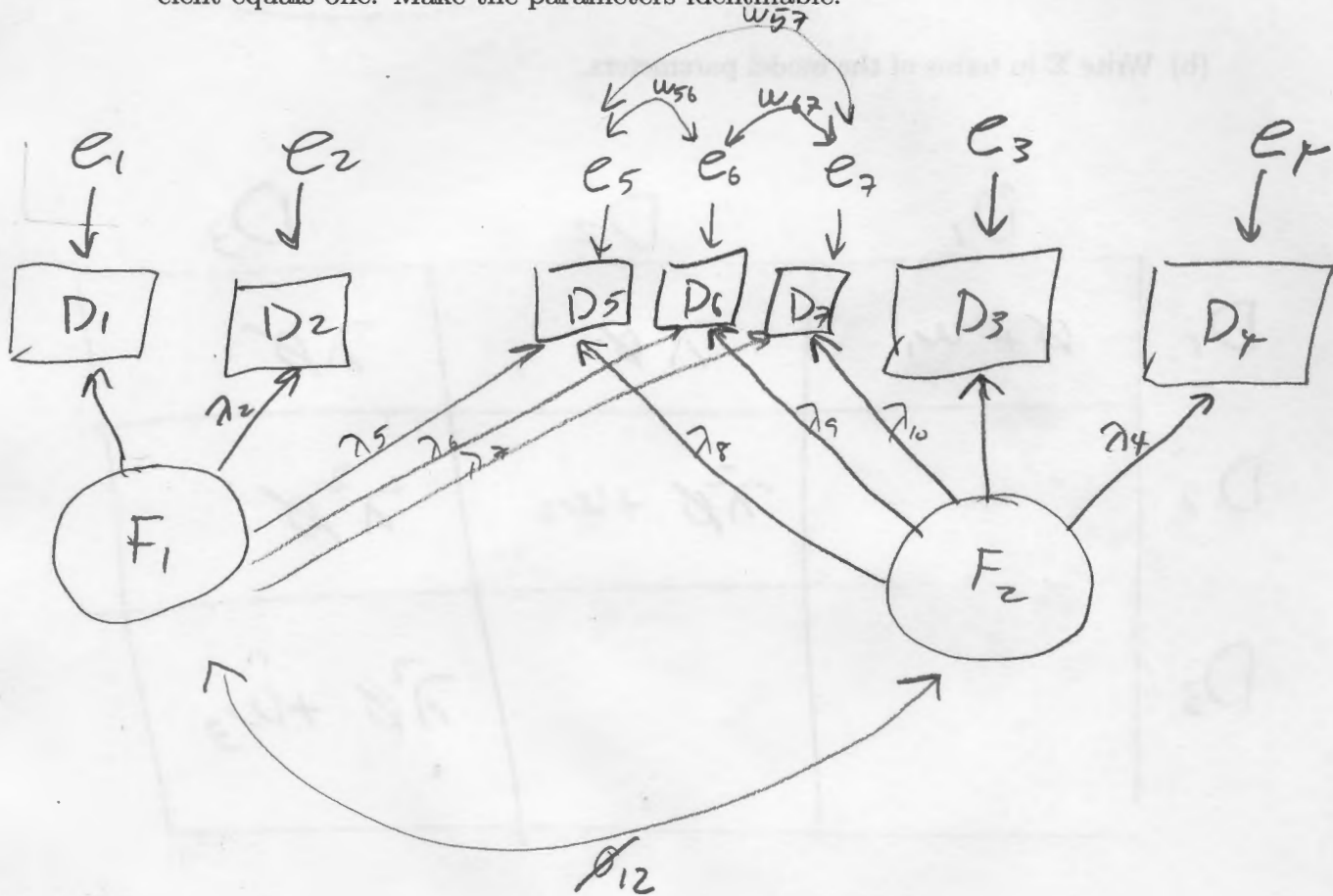


Name Jenny

Student Number \_\_\_\_\_

### STA 431 S2017 Quiz 11

1. (5 points) Make a path diagram with two *unstandardized* factors and seven observed variables that illustrates both the four-variable two-factor rule and the crossover rule. Write symbols on the arrows. If an arrow does not have a symbol it means the coefficient equals one. Make the parameters identifiable.



2. (5 points) Let

$$D_1 = F + e_1$$

$$D_2 = \lambda F + e_2$$

$$D_3 = \lambda F + e_3$$

where  $e_1, e_2, e_3, F$  are all independent,  $\text{Var}(e_j) = \omega_j$ ,  $\text{Var}(F) = \phi$  and  $\lambda \neq 0$ .

(a) What are the degrees of freedom of the chi-squared goodness of fit test for this model? The answer is a number.

5 parameters, 6 equations, so

$$df = 1$$

(b) Write  $\Sigma$  in terms of the model parameters.

	$D_1$	$D_2$	$D_3$
$D_1$	$\phi + \omega_1$	$\lambda\phi$	$\lambda\phi$
$D_2$		$\lambda^2\phi + \omega_2$	$\lambda^2\phi$
$D_3$			$\lambda^2\phi + \omega_3$

(c) Give the model-induced equality constraint or constraints on the  $\sigma_{ij}$  values. This is the null hypothesis of the goodness of fit test.

$$\sigma_{12} = \sigma_{13}$$