

Berkeley Data

```

/***** berkeley.sas *****/
options linesize=79 pagesize=35 noovp formdlim='_';
title 'Berkeley Graduate Admissions Data: ';

proc format;
  value sexfmt 1 = 'Female' 0 = 'Male';
  value ynfmt 1 = 'Yes' 0 = 'No';
data berkley;
  infile 'bogus.dat';
  input line sex dept $ admit count;
  format sex sexfmt.; format admit ynfmt.;

proc freq;
  tables sex*admit / nopercent nocol chisq;
  tables dept*sex / nopercent nocol chisq;
  tables dept*admit / nopercent nocol chisq;
  tables dept*sex*admit / nopercent nocol chisq;

```

The first few data lines:

| | | | | |
|---|---|---|---|-----|
| 1 | 0 | A | 1 | 512 |
| 2 | 0 | B | 1 | 353 |
| 3 | 0 | C | 1 | 120 |
| 4 | 0 | D | 1 | 138 |
| 5 | 0 | E | 1 | 53 |

Part of Berkeley.lst

The FREQ Procedure

Table of sex by admit

| sex | admit | | Total |
|--------|---------------|---------------|-------|
| | No | Yes | |
| Male | 1493 55.48 | 1198 44.52 | 2691 |
| Female | 1278 69.65 | 557 30.35 | 1835 |
| Total | 2771 | 1755 | 4526 |

Statistics for Table of sex by admit

| Statistic | DF | Value | Prob |
|------------|----|---------|--------|
| Chi-Square | 1 | 92.2053 | <.0001 |

Table of dept by sex

| dept | sex | | |
|-----------|--------------|--------------|-------|
| Frequency | | | |
| Row Pct | Male | Female | Total |
| A | 825 88.42 | 108 11.58 | 933 |
| B | 560 95.73 | 25 4.27 | 585 |
| C | 325 35.40 | 593 64.60 | 918 |
| D | 417 52.65 | 375 47.35 | 792 |
| E | 191 32.71 | 393 67.29 | 584 |
| F | 373 52.24 | 341 47.76 | 714 |
| Total | 2691 | 1835 | 4526 |

Berkeley Graduate Admissions Data: 4
23:27 Thursday, January 25, 2007

The FREQ Procedure

Statistics for Table of dept by sex

| Statistic | DF | Value | Prob |
|------------|----|-----------|--------|
| Chi-Square | 5 | 1068.3717 | <.0001 |

Table of dept by admit

| dept | admit | | Total |
|-------|--------------|--------------|-------|
| | No | Yes | |
| A | 332 35.58 | 601 64.42 | 933 |
| B | 215 36.75 | 370 63.25 | 585 |
| C | 596 64.92 | 322 35.08 | 918 |
| D | 523 66.04 | 269 33.96 | 792 |
| E | 437 74.83 | 147 25.17 | 584 |
| F | 668 93.56 | 46 6.44 | 714 |
| Total | 2771 | 1755 | 4526 |

Berkeley Graduate Admissions Data: 6
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The FREQ Procedure

Statistics for Table of dept by admit

| Statistic | DF | Value | Prob |
|------------|----|----------|--------|
| Chi-Square | 5 | 778.9065 | <.0001 |

Table 1 of sex by admit
Controlling for dept=A

| sex | | admit | | |
|-----------|--------------|--------------|--|-------|
| Frequency | | | | |
| Row Pct | No | Yes | | Total |
| Male | 313 37.94 | 512 62.06 | | 825 |
| Female | 19 17.59 | 89 82.41 | | 108 |
| Total | 332 | 601 | | 933 |

| Statistic | DF | Value | Prob |
|------------|----|---------|--------|
| Chi-Square | 1 | 17.2480 | <.0001 |

Table 2 of sex by admit
Controlling for dept=B

| sex | | admit | | |
|-----------|--------------|--------------|--|-------|
| Frequency | | | | |
| Row Pct | No | Yes | | Total |
| Male | 207 36.96 | 353 63.04 | | 560 |
| Female | 8 32.00 | 17 68.00 | | 25 |
| Total | 215 | 370 | | 585 |

| Statistic | DF | Value | Prob |
|------------|----|--------|--------|
| Chi-Square | 1 | 0.2537 | 0.6145 |

Table 3 of sex by admit
Controlling for dept=C

| sex | | admit | | |
|-----------|--------------|--------------|--|-------|
| Frequency | | | | |
| Row Pct | No | Yes | | Total |
| Male | 205 63.08 | 120 36.92 | | 325 |
| Female | 391 65.94 | 202 34.06 | | 593 |
| Total | 596 | 322 | | 918 |

| Statistic | DF | Value | Prob |
|------------|----|--------|--------|
| Chi-Square | 1 | 0.7535 | 0.3854 |

Table 4 of sex by admit
Controlling for dept=D

| sex | | admit | | |
|-----------|--------------|--------------|--|-------|
| Frequency | | | | |
| Row Pct | No | Yes | | Total |
| Male | 279 66.91 | 138 33.09 | | 417 |
| Female | 244 65.07 | 131 34.93 | | 375 |
| Total | 523 | 269 | | 792 |

| Statistic | DF | Value | Prob |
|------------|----|--------|--------|
| Chi-Square | 1 | 0.2980 | 0.5852 |

Table 5 of sex by admit
Controlling for dept=E

| sex | admit | | Total |
|--------|--------------|-------------|-------|
| | No | Yes | |
| Male | 138 72.25 | 53 27.75 | 191 |
| Female | 299 76.08 | 94 23.92 | 393 |
| Total | 437 | 147 | 584 |

| Statistic | DF | Value | Prob |
|------------|----|--------|--------|
| Chi-Square | 1 | 1.0011 | 0.3171 |

Table 6 of sex by admit
Controlling for dept=F

| sex | admit | | Total |
|--------|--------------|------------|-------|
| | No | Yes | |
| Male | 351 94.10 | 22 5.90 | 373 |
| Female | 317 92.96 | 24 7.04 | 341 |
| Total | 668 | 46 | 714 |

| Statistic | DF | Value | Prob |
|------------|----|--------|--------|
| Chi-Square | 1 | 0.3841 | 0.5354 |

Table 3.1: Percentage of female applicants and overall percentage of applicants accepted for six departments

| Department | Percent applicants female | Percentage applicants accepted |
|------------|---------------------------|--------------------------------|
| <i>A</i> | 11.58% | 64.42% |
| <i>B</i> | 4.27 | 63.25 |
| <i>C</i> | 64.60 | 35.08 |
| <i>D</i> | 47.35 | 33.96 |
| <i>E</i> | 67.29 | 25.17 |
| <i>F</i> | 47.76 | 6.44 |

this produced the overall tendency for men to be admitted more than women.

By the way, does this mean that the University of California at Berkeley was *not* discriminating against women? By no means. Why does a department admit very few applicants relative to the number who apply? Because they do not have enough professors and other resources to offer more classes. This implies that the departments popular with men were getting more resources, relative to the level of interest measured by number of applicants. Why? Maybe because men were running the show. The “show,” by the way definitely includes the U. S. military, which funds a lot of engineering and similar stuff at big American universities.

The Berkeley data, a classic example of *Simpson’s paradox*, illustrate the following uncomfortable fact about observational studies. When you include a new variable in an analysis, the results you have could get weaker, they could get stronger, or they could reverse direction — all depending upon the inter-relations of the independent variables. Basically, if an observational study does not include every potential confounding variable you can think of, there is going to be trouble.

Now, the distinguishing feature of the “elementary” tests is that they all involve one independent variable and one dependent variable. Consequently, they can be *extremely* misleading when applied to the data from observational studies, and are best used as tools for preliminary exploration.

Pooling the chi-square tests When using sub-tables to control for a categorical independent variable, it is helpful to have a single test that allows you to answer a question like this: If you control for variable *A*, is *B* related

```

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title 'Berkeley Graduate Admissions Data: ';

proc format;
  value sexfmt 1 = 'Female' 0 = 'Male';
  value ynfmt 1 = 'Yes' 0 = 'No';
data berkley;
  input line sex dept $ admit count;
  format sex sexfmt.; format admit ynfmt.;
  datalines;
1      0      A      1      512
2      0      B      1      353
3      0      C      1      120
4      0      D      1      138
5      0      E      1      53
6      0      F      1      22
7      1      A      1      89
8      1      B      1      17
9      1      C      1      202
10     1      D      1      131
11     1      E      1      94
12     1      F      1      24
13     0      A      0      313
14     0      B      0      207
15     0      C      0      205
16     0      D      0      279
17     0      E      0      138
18     0      F      0      351
19     1      A      0      19
20     1      B      0      8
21     1      C      0      391
22     1      D      0      244
23     1      E      0      299
24     1      F      0      317
;
proc freq;
  tables sex*admit / nopercent nocol chisq;
  tables dept*sex / nopercent nocol chisq;
  tables dept*admit / nopercent nocol chisq;
  tables dept*sex*admit / nopercent nocol chisq;
  /* Get 21.745 > 12.59159 */
  weight count;

```