## Sample Questions: Discrete Random Variables

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1. Roll two fair dice. Let X denote the sum of the two numbers.

- (a) What is p(12)? The answer is a number.
- (b) What is F(12)? The answer is a number.
- (c) What is p(27)? The answer is a number.
- (d) What is F(27)? The answer is a number.
- (e) What is p(4)? The answer is a number.
- (f) What is F(4)? The answer is a number.
- (g) What is F(4.5)? The answer is a number.
- (h) What is p(4.5)? The answer is a number.

- 2. A biased coin has  $P(\text{Head}) = \frac{1}{3}$ . Toss it twice.
  - (a) List the elements of the sample space  $\Omega$ , together with their probabilities.

(b) Let X equal the number of heads. For what values of x is P(X = x) > 0?

(c) Give p(x) and F(x) just for x = 0, 1, 2.

- (d) What is p(1.5)?
- (e) What is F(1.5)?
- (f) What is p(-9)?
- (g) What is F(-9)?
- (h) What is p(114)?
- (i) What is F(114)?

(j) Graph F(x).

3. Let the discrete random variable X have probability mass function p(x) = cx for x = 1, 2, 3, 4 and zero otherwise. What is the constant c?

4. Prove that the binomial probabilities sum to one. The formula sheet for Test 2 will have the Binomial Theorem:  $(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^k b^{n-k}$ 

- 5. Let X have a binomial distribution with n=5 and  $p=\frac{1}{4}$ .
  - (a) What is p(0)? The answer is a number.
  - (b) What is F(0)? The answer is a number.
  - (c) What is F(5)? The answer is a number.
  - (d) What is p(2)? The answer is a number.
  - (e) What is F(1)? The answer is a number.

6.	Cheap umbrellas are shipped to the dollar store in boxes of 20. The probability that the umbrella is defective (you can't even use it once) is 0.10. We will assume that being defective or not for the 20 umbrellas in a box are independent events, though this assumption may not be safe in practice, depending on the manufacturing and shipping process.						
	(a)	What is the probability that all 20 umbrellas are okay? The answer is a number.					
	(b)	Obtain that last number as $p(0)$ for one of the standard probability distributions.					
	(c)	That is the probability that exactly two umbrellas are defective? The answer is a number.					
	(d)	What is the probability that two or fewer umbrellas are defective? The answer is a number.					

7.	In a box of 2	0 umbrellas,	2 are defec	etive. If yo	ou sample 5	umbrell as	randomly	without
	replacement,	what is the	probability	of at least	one defect	ive? The ar	nswer is a	number.

8. Going back to the assumptions of Question 6, the probability of a defective umbrella is 0.10, they are independent, and they are shipped in boxes of 20. You choose a box at random, and then sample 5 umbrellas randomly without replacement, what is the probability of at least one defective? The answer is a number.

- 9. It is true love, but still the chances your significant other will break up with you on any given day is a tenth of one percent. Assuming 365 days in a year and independence, what is the probability that
- 10. (a) Your relationship will last at least one year. The answer is a number.

(b) Your relationship will last between one year and two years. That is if X is the day on which the relationship ends, what is  $P(366 \le X \le 730)$ ?

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