

Name _____

Student Number _____

University of Toronto in Mississauga

December Examinations 2005

STA 442F

Duration - 3 hours

Aids allowed: Calculator. Printouts will be supplied.

$$F = \left(\frac{n-p}{s}\right)\left(\frac{a}{1-a}\right) \quad a = \frac{R_F^2 - R_R^2}{1 - R_R^2} = \frac{sF}{n-p+sF}$$

1. (8 Points) Make up an original study that would employ a one-way multivariate analysis of covariance with one quantitative covariate and two dependent variables. Give a paragraph briefly describing the study, followed by list of the variables; classify each variable as independent or dependent, and quantitative or categorical.

Continued on page 2

2. (8 Points) Answer each question below True or False. Write “T” or “F” on the line. You must get at least 9 out of 10 correct in order to get credit for this question.

- _____ In an observational study, a statistically significant relationship between the independent variable and the dependent variable can provide some evidence of a causal relationship if the study is well controlled.
- _____ If a subject (case) provides data for more than one value of an independent variable, we call that independent variable a *within-subjects* variable.
- _____ We observe $r = -0.70$, $p = .009$. We conclude that that high values of X tend to go with low values of Y and low values of X tend to go with high values of Y .
- _____ If $p < .05$ we say the results are statistically significant at the .05 level, and we conclude that the independent variable and the dependent variable are unrelated.
- _____ In a study attempting to predict income from education and race, there is a significant interaction between education and race. This means that income and race are related.
- _____ When you add another independent variable in multiple regression, R^2 cannot go down.
- _____ We observe $r = 0.50$, $p = .002$. This means that 50% of the variation in the dependent variable is explained by a linear relationship with the independent variable.
- _____ An experimental study is one in which cases are randomly assigned to the different values of an independent variable.
- _____ When a relationship between the independent variable and the dependent variable is *not* statistically significant, we conclude there is no relationship between the two variables in the population.
- _____ A multivariate analysis is one with multiple independent variables.

3. (7 Points) Recall the **cars data**, in which you want to test for differences in fuel efficiency as a function of country (actually, region) of origin, while controlling for weight (X_1) and length (X_2) of vehicle. You need to set up a regression model using *cell means coding*; there will be no β_0 in the model.

(a) List all the independent variables in your model. Say how the dummy variables are defined.

(b) Make a table with three rows, one for each country. Make a column for each dummy variable, and show the value of the dummy variable for each country. Make one more column, a wider one. In that column, give the expected value of Y . Your expected value formulas must have only numbers, betas (β) and the symbols X_1 and X_2 .

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4. Now please look at the printout for the cars data, and answer these questions:

(a) (5 Points) We want to test whether fuel efficiency is related to *any* of weight, length and country of origin. The null hypothesis is that fuel efficiency is not related to any of these variables.

i. What is the value of the test statistic? The answer is a single number.

ii. What is the p -value? The answer is a number or possibly a range of numbers, if $p < .0001$.

iii. Are the results statistically significant at the 0.05 level? Answer Yes or No.

(b) (3 Points) For any country of origin, and holding weight constant at a fixed level, is length positively related to fuel efficiency, or is it negatively related? How do you know? Your answer to this question should be the words “Positively Related” or “Negatively related,” and a single number — a parameter estimate.

(c) (5 Points) Controlling for country of origin, we want to test whether fuel efficiency is related to weight, length, or both.

i. What is the value of the test statistic? The answer is a single number.

ii. What is the p -value? The answer is a number or possibly a range of numbers, if $p < .0001$.

iii. Are the results statistically significant at the 0.05 level? Answer Yes or No.

Continued on page 5

- (d) (6 Points) Controlling for weight and length, we want to test whether fuel efficiency is related to country of origin.
- What is the value of the test statistic? The answer is a single number.
 - What is the p -value? The answer is a number or possibly a range of numbers, if $p < .0001$.
 - Are the results statistically significant at the 0.05 level? Answer Yes or No.
 - After allowing for the reduced model, what proportion of the remaining variation is explained by this effect?
- (e) (14 Points) Now we will look at *one* of the pairwise comparisons.
- We want to test the difference between cars of U.S. versus Japanese origin, controlling for weight and length.
 - What is the value of the test statistic? The answer is a single number.
 - What is the p -value? The answer is a number or possibly a range of numbers, if $p < .0001$.
 - Are the results statistically significant at the 0.05 level? Answer Yes or No.
 - Are the results still statistically significant with a Bonferroni correction for the fact that we are making three pairwise comparisons? Answer Yes or No.
 - After allowing for the reduced model, what proportion of the remaining variation is explained by this effect?

Continued on page 6

- ii. What is the predicted fuel efficiency in Kilometers per litre for a Japanese car of average weight and length? By average, I mean set weight and length to their sample mean values. The answer to this question is a single number. Please “show your work” by writing down the expression you are trying to calculate, and then doing it with your calculator.

- iii. What is the predicted fuel efficiency in Kilometers per litre for a U.S. car of average weight and length? By average, I mean set weight and length to their sample mean values. The answer to this question is a single number. Please “show your work” by writing down the expression you are trying to calculate, and then doing it with your calculator.

- iv. In plain, non-statistical language, what do you conclude about the relative fuel efficiency of U.S. and Japanese cars *once you allow for length and weight*? The answer is one short sentence; you have more room than you need.

Continued on page 7

5. (8 Points) Consider the Titanic data. For just adults, we want to know if survival was related to sex when one allows for class.
- (a) Give the value of the test statistic. Your answer is a single number.
 - (b) The test is significant beyond any doubt. What degrees of freedom would you use to calculate the p -value? Your answer is a single number.
 - (c) Are the Bonferroni-corrected tests on the sub-tables all significant at the 0.05 level? Answer Yes or No. If the answer is No, specify which ones are not significant.
 - (d) In plain, non-statistical language, what do you conclude from this analysis?
6. (5 Points) In the analysis of the **shoe data**, I followed up a significant main effect for period (Before, During and After the advertising campaign) with Bonferroni-corrected pairwise comparisons of marginal means. In plain, non-statistical language, what do you conclude from the pairwise comparisons? *Marks will be deducted if you use even a single statistical term.*

7. (8 Points) Make up an original study with one categorical within-subjects independent variable, one quantitative between-subjects independent variable, and one categorical dependent variable. Give a paragraph briefly describing the study, followed by list of the variables; classify each variable as independent or dependent, and categorical or quantitative. State whether each independent variable is between-subjects or within-subjects.

Continued on page 9

8. (5 Points) For the **exercise tolerance data**, please focus upon the following question: Does the relationship of Smoking to exercise tolerance depend on Fat level? Answer the question and describe the results in plain, non-statistical language. Your answer should be guided by the results of a statistical test, but you must not mention that test explicitly.
9. (5 Points) For the **farm data**, we want to know whether the effect of irrigation method depends upon the type of fertilizer.
- (a) What is the value of the test statistic? The answer is a single number.
 - (b) What is the p -value? The answer is a number or possibly a range of numbers, if $p < .0001$.
 - (c) Are the results statistically significant at the 0.05 level? Answer Yes or No.
 - (d) In plain, non-statistical language, what do you conclude?

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10. (8 Points) Give an example of a true experimental study with one independent variable, and the conclusions of the study are invalid because of a confounding variable. Hint: consider a drug study without a double blind.

11. (5 Points) In the **wine study**, 6 judges rated 4 wines on a scale from 0 to 40, presented in random order and with a double blind. Based on the Bonferroni-corrected tests for pairwise differences between means, sort the wines into groups such that the members of each group of wines are *not* significantly different, and arrange the groups in order from highest to lowest quality. Here is an example of what I mean (of course this answer is incorrect):

“Wine 3 is rated highest, followed by Wines 1 and 4, followed by Wine 2.”

Total marks = 100 points

STA442F05 Final Printout

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```
-----
/***** cars.sas *****/
options linesize=79 pagesize=200 noovp formdlm='-';
title 'Metric Cars Data: STA442/1008 Final Exam';

proc format; /* Used to label values of the categorical variables */
  value carfmt
    1 = 'US'
    2 = 'Japanese'
    3 = 'European' ;

data auto;
  infile 'mcars.dat' firstobs=2; /* Skip the first line */
  input id country kpl weight length;
/* Cell Means Indicator dummy vars */
  if country = 1 then c1=1; else c1=0;
  if country = 2 then c2=1; else c2=0;
  if country = 3 then c3=1; else c3=0;
  label country = 'Country of Origin'
        kpl = 'Kilometers per Litre';
  format country carfmt.;

proc reg simple;
  title 'ANCOVA with cell means coding using proc reg';
  model kpl = weight length c1 c2 c3 / noint;
  TestA: test c1 = c2 = c3 = 0;
  TestB: test c1 = c2 = c3;
  TestC: test c1 = c2;
  TestD: test c1 = c3;
  TestE: test c2 = c3;
  TestF: test c1 = c2 = 0;
  TestG: test c1 = c3 = 0;
  TestH: test c2 = c3 = 0;
  TestI: test weight=length=0;
  TestJ: test weight=length=0, c1 = c2 = c3;
  TestK: test weight=length=0, c1 = c2 = c3 = 0;
```

cars.lst

```
-----
ANCOVA with cell means coding using proc reg 1
15:56 Sunday, December 4, 2005
```

The REG Procedure

Descriptive Statistics

Variable	Sum	Mean	Uncorrected SS	Variance	Standard Deviation
Intercept	100.00000	1.00000	100.00000	0	0
weight	141345	1413.45000	212754681	131016	361.96142
length	48489	484.88600	23811410	3029.97113	55.04517
c1	73.00000	0.73000	73.00000	0.19909	0.44620
c2	13.00000	0.13000	13.00000	0.11424	0.33800
c3	14.00000	0.14000	14.00000	0.12162	0.34874
kpl	879.48000	8.79480	8440.74000	7.13019	2.67024

```
-----
ANCOVA with cell means coding using proc reg 2
15:56 Sunday, December 4, 2005
```

The REG Procedure

Model: MODEL1

Dependent Variable: kpl Kilometers per Litre

NOTE: No intercept in model. R-Square is redefined.

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	8195.93850	1639.18770	636.12	<.0001
Error	95	244.80150	2.57686		
Uncorrected Total	100	8440.74000			

Root MSE	1.60526	R-Square	0.9710
Dependent Mean	8.79480	Adj R-Sq	0.9695
Coeff Var	18.25237		

Parameter Estimates

Variable	Label	DF	Parameter Estimate	Standard Error	t Value
weight		1	-0.00207	0.00139	-1.49
length		1	-0.02874	0.00925	-3.11
c1		1	25.85295	2.83493	9.12
c2		1	24.49010	2.75828	8.88
c3		1	25.73537	2.69159	9.56

Parameter Estimates			
Variable	Label	DF	Pr > t
weight		1	0.1389
length		1	0.0025
c1		1	<.0001
c2		1	<.0001
c3		1	<.0001

Test TestA Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	3	81.87863	31.77	<.0001
Denominator	95	2.57686		

Test TestB Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	2	8.50611	3.30	0.0411
Denominator	95	2.57686		

Test TestC Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	1	15.74243	6.11	0.0152
Denominator	95	2.57686		

Test TestD Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	1	0.12092	0.05	0.8290
Denominator	95	2.57686		

Test TestE Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	1	10.32125	4.01	0.0482
Denominator	95	2.57686		

Test TestF Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	2	107.30322	41.64	<.0001
Denominator	95	2.57686		

Test TestG Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	2	120.43287	46.74	<.0001
Denominator	95	2.57686		

Test TestH Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	2	122.60725	47.58	<.0001
Denominator	95	2.57686		

Test TestI Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	2	169.74773	65.87	<.0001
Denominator	95	2.57686		

Test TestJ Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	4	115.27195	44.73	<.0001
Denominator	95	2.57686		

Test TestK Results for Dependent Variable kpl

Source	DF	Mean Square	F Value	Pr > F
Numerator	5	1639.18770	636.12	<.0001
Denominator	95	2.57686		

```

/* titanic2.sas */
title 'Titanic Data: STTA442 Final Check';
options linesize=79 pagesize=35 noovp formdlm='_';

proc format;
  value clfmt 0 = 'Crew';
  value agefmt 1 = 'Adult' 0 = 'Child';
  value sexfmt 1 = 'Male' 0 = 'Female';
  value ynfmt 0 = 'No' 1 = 'Yes';

data iceberg;
  infile 'titanic.dat';
  input class age sex survived;
  pasclass = class; if pasclass=0 then pasclass=.;
  manclass = class; if sex = 0 then manstat=.; if age=0 then manstat=.;
  adclass = class; if age=0 then adclass=.;
  label manclass = 'Class: Adult males only'
        adclass = 'Class: Adults only'
        pasclass = 'Passenger class';
  format class manclass adclass clfmt.;
  format age agefmt.; format sex sexfmt.; format survived ynfmt.;

proc freq;
  title2 'Just Adults';
  tables sex*survived*adclass
    / norow nopercent chisq expected;
  tables adclass*survived*sex
    / norow nopercent chisq expected;

data kids;
  set iceberg;
  if age=0;

proc freq;
  title2 'Just Children';
  tables survived * (class sex)
    / norow nopercent chisq expected;

```

titanic2.lst

```

Titanic Data: STTA442 Final Check
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table 1 of survived by adclass
Controlling for sex=Female

survived      adclass(Class: Adults only)

Frequency|
Expected|
Col Pct |Crew    | 1      | 2      | 3      | Total
-----+-----+-----+-----+-----+
No        | 3       | 4      | 13     | 89     | 109
          | 5.8988 | 36.932 | 23.852 | 42.318 |
          | 13.04  | 2.78   | 13.98  | 53.94  |
-----+-----+-----+-----+
Yes       | 20      | 140    | 80     | 76     | 316
          | 17.101 | 107.07 | 69.148 | 122.68 |
          | 86.96  | 97.22  | 86.02  | 46.06  |
-----+-----+-----+-----+
Total    | 23      | 144    | 93     | 165    | 425

Frequency Missing = 45

```

```

Titanic Data: STTA442 Final Check
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 1 of survived by adclass
Controlling for sex=Female

Statistic      DF      Value      Prob
-----+-----+-----+
Chi-Square      3      117.3107  <.0001
Likelihood Ratio Chi-Square  3      126.6013  <.0001
Mantel-Haenszel Chi-Square  1      95.5274  <.0001
Phi Coefficient           0.5254
Contingency Coefficient    0.4651
Cramer's V           0.5254

Effective Sample Size = 425
Frequency Missing = 45

```

Titanic Data: STTA442 Final Check 3
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table 2 of survived by adclass
Controlling for sex=Male

survived	adclass(Class: Adults only)				
Frequency Expected Col Pct	Crew	1	2	3	Total
No	670 687.22 77.73	118 139.52 67.43	154 133.94 91.67	387 368.33 83.77	1329
Yes	192 174.78 22.27	57 35.483 32.57	14 34.064 8.33	75 93.675 16.23	338
Total	862	175	168	462	1667

Frequency Missing = 64

Titanic Data: STTA442 Final Check 4
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 2 of survived by adclass
Controlling for sex=Male

Statistic	DF	Value	Prob
Chi-Square	3	37.9879	<.0001
Likelihood Ratio Chi-Square	3	39.6102	<.0001
Mantel-Haenszel Chi-Square	1	12.0997	0.0005
Phi Coefficient		0.1510	
Contingency Coefficient		0.1493	
Cramer's V		0.1510	

Effective Sample Size = 1667
Frequency Missing = 64

Titanic Data: STTA442 Final Check 5
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table 1 of survived by sex
Controlling for adclass=Crew

survived	sex		
Frequency Expected Col Pct	Female	Male	Total
No	3 17.49 13.04	670 655.51 77.73	673
Yes	20 5.5096 86.96	192 206.49 22.27	212
Total	23	862	885

Titanic Data: STTA442 Final Check 6
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 1 of survived by sex
Controlling for adclass=Crew

Statistic	DF	Value	Prob
Chi-Square	1	51.4522	<.0001
Likelihood Ratio Chi-Square	1	42.3508	<.0001
Continuity Adj. Chi-Square	1	47.9627	<.0001
Mantel-Haenszel Chi-Square	1	51.3941	<.0001
Phi Coefficient		-0.2411	
Contingency Coefficient		0.2344	
Cramer's V		-0.2411	

Fisher's Exact Test

Cell (1,1) Frequency (F)	3
Left-sided Pr <= F	1.655E-10
Right-sided Pr >= F	1.0000
Table Probability (P)	1.588E-10
Two-sided Pr <= P	1.655E-10

Sample Size = 885

Titanic Data: STTA442 Final Check 7
Just Adults 17:05 Sunday, December 4, 2005

Table 2 of survived by sex
Controlling for adclass=1

survived	sex		
Frequency	Female	Male	Total
Expected			
Col Pct			
No	4	118	122
	55.072	66.928	
	2.78	67.43	
Yes	140	57	197
	88.928	108.07	
	97.22	32.57	
Total	144	175	319

Titanic Data: STTA442 Final Check 8
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 2 of survived by sex
Controlling for adclass=1

Statistic	DF	Value	Prob
Chi-Square	1	139.8018	<.0001
Likelihood Ratio Chi-Square	1	166.9868	<.0001
Continuity Adj. Chi-Square	1	137.0779	<.0001
Mantel-Haenszel Chi-Square	1	139.3636	<.0001
Phi Coefficient		-0.6620	
Contingency Coefficient		0.5520	
Cramer's V		-0.6620	

Fisher's Exact Test

Cell (1,1) Frequency (F)	4
Left-sided Pr <= F	1.541E-37
Right-sided Pr >= F	1.0000
Table Probability (P)	1.521E-37
Two-sided Pr <= P	1.625E-37

Sample Size = 319

Titanic Data: STTA442 Final Check 9
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table 3 of survived by sex
Controlling for adclass=2

survived	sex		
Frequency	Female	Male	Total
Expected			
Col Pct			
No	13	154	167
	59.506	107.49	
	13.98	91.67	
Yes	80	14	94
	33.494	60.506	
	86.02	8.33	
Total	93	168	261

Titanic Data: STTA442 Final Check 10
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 3 of survived by sex
Controlling for adclass=2

Statistic	DF	Value	Prob
Chi-Square	1	156.7827	<.0001
Likelihood Ratio Chi-Square	1	169.5028	<.0001
Continuity Adj. Chi-Square	1	153.4296	<.0001
Mantel-Haenszel Chi-Square	1	156.1820	<.0001
Phi Coefficient		-0.7750	
Contingency Coefficient		0.6126	
Cramer's V		-0.7750	

Fisher's Exact Test

Cell (1,1) Frequency (F)	13
Left-sided Pr <= F	4.040E-38
Right-sided Pr >= F	1.0000
Table Probability (P)	3.981E-38
Two-sided Pr <= P	4.040E-38

Sample Size = 261

Titanic Data: STTA442 Final Check 11
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table 4 of survived by sex
Controlling for adclass=3

survived	sex		
Frequency	Female	Male	Total
Expected			
Col Pct			
No	89	387	476
	125.26	350.74	
	53.94	83.77	
Yes	76	75	151
	39.737	111.26	
	46.06	16.23	
Total	165	462	627

Titanic Data: STTA442 Final Check 12
Just Adults 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table 4 of survived by sex
Controlling for adclass=3

Statistic	DF	Value	Prob
Chi-Square	1	59.1594	<.0001
Likelihood Ratio Chi-Square	1	54.7194	<.0001
Continuity Adj. Chi-Square	1	57.5393	<.0001
Mantel-Haenszel Chi-Square	1	59.0651	<.0001
Phi Coefficient		-0.3072	
Contingency Coefficient		0.2936	
Cramer's V		-0.3072	

Fisher's Exact Test

Cell (1,1) Frequency (F)	89
Left-sided Pr <= F	1.414E-13
Right-sided Pr >= F	1.0000
Table Probability (P)	1.102E-13
Two-sided Pr <= P	2.336E-13

Sample Size = 627

Titanic Data: STTA442 Final Check 13
Just Children 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table of survived by class

survived	class			
Frequency	1	2	3	Total
Expected				
Col Pct				
No	0	0	52	52
	2.8624	11.45	37.688	
	0.00	0.00	65.82	
Yes	6	24	27	57
	3.1376	12.55	41.312	
	100.00	100.00	34.18	
Total	6	24	79	109

Titanic Data: STTA442 Final Check 14
Just Children 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table of survived by class

Statistic	DF	Value	Prob
Chi-Square	2	37.7615	<.0001
Likelihood Ratio Chi-Square	2	49.4084	<.0001
Mantel-Haenszel Chi-Square	1	32.4416	<.0001
Phi Coefficient		0.5886	
Contingency Coefficient		0.5072	
Cramer's V		0.5886	

WARNING: 33% of the cells have expected counts less than 5. Chi-Square may not be a valid test.

Sample Size = 109

Titanic Data: STTA442 Final Check 15
Just Children 17:05 Sunday, December 4, 2005

The FREQ Procedure

Table of survived by sex

survived		sex		Total
Frequency	Expected			
Col Pct		Female	Male	
-----+-----+-----+-----+-----				
No	17	35		52
	21.468	30.532		
	37.78	54.69		
-----+-----+-----+-----+-----				
Yes	28	29		57
	23.532	33.468		
	62.22	45.31		
-----+-----+-----+-----+-----				
Total	45	64		109

Titanic Data: STTA442 Final Check 16
Just Children 17:05 Sunday, December 4, 2005

The FREQ Procedure

Statistics for Table of survived by sex

Statistic	DF	Value	Prob
-----+-----+-----+-----			
Chi-Square	1	3.0284	0.0818
Likelihood Ratio Chi-Square	1	3.0502	0.0807
Continuity Adj. Chi-Square	1	2.3885	0.1222
Mantel-Haenszel Chi-Square	1	3.0006	0.0832
Phi Coefficient		-0.1667	
Contingency Coefficient		0.1644	
Cramer's V		-0.1667	

Fisher's Exact Test

-----+-----+-----		
Cell (1,1) Frequency (F)		17
Left-sided Pr <= F		0.0608
Right-sided Pr >= F		0.9739
-----+-----+-----		
Table Probability (P)		0.0347
Two-sided Pr <= P		0.1188

Sample Size = 109

```
/* extoler.sas */
title 'Exercise Tolerance Data: STTA442 Final Exam';
options linesize=79 pagesize=200 noovp formdlm='_';

proc format;
  value sexfmt 1 = 'Male' 2 = 'Female';
  value fatfmt 1 = 'Low' 2 = 'High';
  value smfmt 1 = 'Light' 2 = 'Heavy';

data nopain;
  infile 'extoler.dat' firstobs=2; /* Skip the first line */
  input Toler Sex Fat Smoke;
  format sex sexfmt.; format fat fatfmt.; format smoke smfmt.;
  label toler = 'Exercise tolerance in minutes';

proc glm;
  class Sex Fat Smoke;
  model toler = Sex|Fat|Smoke;
  means Sex|Fat|Smoke;
```

extoler.lst

Exercise Tolerance Data: STTA442 Final Exam 1
23:36 Sunday, December 4, 2005

The GLM Procedure

Class Level Information

Class	Levels	Values
Sex	2	Female Male
Fat	2	High Low
Smoke	2	Heavy Light

Number of observations 24

Dependent Variable: Toler		Exercise tolerance in minutes			
		Sum of			
Source	DF	Squares	Mean Square	F Value	Pr > F
Model	7	588.5829167	84.0832738	9.01	0.0002
Error	16	149.3666667	9.3354167		
Corrected Total	23	737.9495833			

	R-Square	Coeff Var	Root MSE	Toler	Mean	
	0.797592	18.77833	3.055391	16.27083		
Source	DF	Type I SS	Mean Square	F Value	Pr > F	
Sex	1	176.5837500	176.5837500	18.92	0.0005	
Fat	1	242.5704167	242.5704167	25.98	0.0001	
Sex*Fat	1	13.6504167	13.6504167	1.46	0.2441	
Smoke	1	70.3837500	70.3837500	7.54	0.0144	
Sex*Smoke	1	11.0704167	11.0704167	1.19	0.2923	
Fat*Smoke	1	72.4537500	72.4537500	7.76	0.0132	
Sex*Fat*Smoke	1	1.8704167	1.8704167	0.20	0.6604	
Source	DF	Type III SS	Mean Square	F Value	Pr > F	
Sex	1	176.5837500	176.5837500	18.92	0.0005	
Fat	1	242.5704167	242.5704167	25.98	0.0001	
Sex*Fat	1	13.6504167	13.6504167	1.46	0.2441	
Smoke	1	70.3837500	70.3837500	7.54	0.0144	
Sex*Smoke	1	11.0704167	11.0704167	1.19	0.2923	
Fat*Smoke	1	72.4537500	72.4537500	7.76	0.0132	
Sex*Fat*Smoke	1	1.8704167	1.8704167	0.20	0.6604	

Exercise Tolerance Data: STTA442 Final Exam 3
23:36 Sunday, December 4, 2005

The GLM Procedure

Level of Sex	N	-----Toler----- Mean	Std Dev
Female	12	13.5583333	4.72102807
Male	12	18.9833333	5.36145050

Level of Fat	N	-----Toler----- Mean	Std Dev
High	12	13.0916667	3.72667493
Low	12	19.4500000	5.58089273

Level of Sex	Level of Fat	N	-----Toler----- Mean	Std Dev
Female	High	6	11.1333333	3.61146323
Female	Low	6	15.9833333	4.67735680
Male	High	6	15.0500000	2.88218667
Male	Low	6	22.9166667	4.21920214

Level of Smoke	N	-----Toler----- Mean	Std Dev
Heavy	12	14.5583333	4.85713315
Light	12	17.9833333	6.09065355

Level of Sex	Level of Smoke	N	-----Toler----- Mean	Std Dev
Female	Heavy	6	11.1666667	3.20104150
Female	Light	6	15.9500000	5.00589652
Male	Heavy	6	17.9500000	3.74793276
Male	Light	6	20.0166667	6.82859185

Level of Fat	Level of Smoke	N	-----Toler----- Mean	Std Dev
High	Heavy	6	13.1166667	4.82303501
High	Light	6	13.0666667	2.70012345
Low	Heavy	6	16.0000000	4.86333219
Low	Light	6	22.9000000	4.03782119

Level of Sex	Level of Fat	Level of Smoke	N	-----Toler----- Mean	Std Dev
Female	High	Heavy	3	10.2000000	4.15090352
Female	High	Light	3	12.0666667	3.57258077
Female	Low	Heavy	3	12.1333333	2.36290781
Female	Low	Light	3	19.8333333	2.15483951
Male	High	Heavy	3	16.0333333	3.92470806
Male	High	Light	3	14.0666667	1.56950098
Male	Low	Heavy	3	19.8666667	2.94844592
Male	Low	Light	3	25.9666667	2.81128678

```

/* finalfarm.sas */
options linesize=79 pagesize=100 noovp formdlim='_';
title 'STA442F05 Final Exam: Farm data from NWK Prob 29.20, p. 1204';

data wheat;
  infile 'farm2.dat' firstobs=2; /* Skip the first line */
  input Field IgMethod Yield1 Yield2;
  label igmethod = 'Irrigation Method'
        yield1 = 'Crop Yield with Fertilizer 1'
        yield2 = 'Crop Yield with Fertilizer 2';

proc means mean stddev n;
  class igmethod;
  var Yield1 Yield2;

proc glm;
  class igmethod;
  model yield1 yield2 = igmethod;
  repeated Fertilizr / short summary;

```

finalfarm.lst

STA442F05 Final Exam: Farm data from NWK Prob 29.20, p. 1204					1
20:38 Monday, December 5, 2005					
The MEANS Procedure					
Irrigation Method	N Obs	Variable	Label	Mean	

1	5	Yield1	Crop Yield with Fertilizer 1	35.4000000	
		Yield2	Crop Yield with Fertilizer 2	39.2000000	
2	5	Yield1	Crop Yield with Fertilizer 1	52.2000000	
		Yield2	Crop Yield with Fertilizer 2	55.8000000	

Irrigation Method	N Obs	Variable	Label	Std Dev	N

1	5	Yield1	Crop Yield with Fertilizer 1	6.5038450	5
		Yield2	Crop Yield with Fertilizer 2	6.8337398	5
2	5	Yield1	Crop Yield with Fertilizer 1	7.0498227	5
		Yield2	Crop Yield with Fertilizer 2	8.5848704	5

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The GLM Procedure

Class Level Information

Class	Levels	Values
IgMethod	2	1 2
Number of observations		10

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The GLM Procedure

Dependent Variable: Yield1 Crop Yield with Fertilizer 1

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	705.600000	705.600000	15.34	0.0044
Error	8	368.000000	46.000000		
Corrected Total	9	1073.600000			

R-Square	Coeff Var	Root MSE	Yield1 Mean
0.657228	15.48477	6.782330	43.80000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
IgMethod	1	705.600000	705.600000	15.34	0.0044

Source	DF	Type III SS	Mean Square	F Value	Pr > F
IgMethod	1	705.600000	705.600000	15.34	0.0044

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The GLM Procedure

Dependent Variable: Yield2 Crop Yield with Fertilizer 2

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	688.900000	688.900000	11.44	0.0096
Error	8	481.600000	60.200000		
Corrected Total	9	1170.500000			

R-Square	Coeff Var	Root MSE	Yield2 Mean
0.588552	16.33445	7.758866	47.50000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
IgMethod	1	688.9000000	688.9000000	11.44	0.0096

Source	DF	Type III SS	Mean Square	F Value	Pr > F
IgMethod	1	688.9000000	688.9000000	11.44	0.0096

The GLM Procedure
Repeated Measures Analysis of Variance

Repeated Measures Level Information

Dependent Variable	Yield1	Yield2
Level of Fertilizr	1	2

Manova Test Criteria and Exact F Statistics
for the Hypothesis of no Fertilizr Effect
H = Type III SSCP Matrix for Fertilizr
E = Error SSCP Matrix

	S=1	M=-0.5	N=3			
Statistic	Value	F Value	Num DF	Den DF	Pr > F	
Wilks' Lambda	0.14916097	45.63	1	8	0.0001	
Pillai's Trace	0.85083903	45.63	1	8	0.0001	
Hotelling-Lawley Trace	5.70416667	45.63	1	8	0.0001	
Roy's Greatest Root	5.70416667	45.63	1	8	0.0001	

Manova Test Criteria and Exact F Statistics for
the Hypothesis of no Fertilizr*IgMethod Effect
H = Type III SSCP Matrix for Fertilizr*IgMethod
E = Error SSCP Matrix

	S=1	M=-0.5	N=3			
Statistic	Value	F Value	Num DF	Den DF	Pr > F	
Wilks' Lambda	0.99585062	0.03	1	8	0.8597	
Pillai's Trace	0.00414938	0.03	1	8	0.8597	
Hotelling-Lawley Trace	0.00416667	0.03	1	8	0.8597	
Roy's Greatest Root	0.00416667	0.03	1	8	0.8597	

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The GLM Procedure
Repeated Measures Analysis of Variance
Tests of Hypotheses for Between Subjects Effects

Source	DF	Type III SS	Mean Square	F Value	Pr > F
IgMethod	1	1394.450000	1394.450000	13.32	0.0065
Error	8	837.600000	104.700000		

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The GLM Procedure
Repeated Measures Analysis of Variance
Univariate Tests of Hypotheses for Within Subject Effects

Source	DF	Type III SS	Mean Square	F Value	Pr > F
Fertilizr	1	68.45000000	68.45000000	45.63	0.0001
Fertilizr*IgMethod	1	0.05000000	0.05000000	0.03	0.8597
Error(Fertilizr)	8	12.00000000	1.50000000		

```

/* finalshoe.sas */
options linesize=79 pagesize=100 noovp formdlim='_';
title 'STA442F05 Final Exam: Shoe data from NWK Table 29.10';

data uvfoot;
  infile 'shoes.dat' firstobs=2; /* Skip the first line */
  input row ident period campaign sales;

proc mixed cl;
  class period campaign;
  model sales = period|campaign;
  repeated / type = un subject = ident;
  lsmeans period / adjust=bon;

```

finalshoe.lst

```

STA442F05 Final Exam: Shoe data from NWK Table 29.10      1
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```

The Mixed Procedure

Model Information

Data Set	WORK.UVFOOT
Dependent Variable	sales
Covariance Structure	Unstructured
Subject Effect	ident
Estimation Method	REML
Residual Variance Method	None
Fixed Effects SE Method	Model-Based
Degrees of Freedom Method	Between-Within

Class Level Information

Class	Levels	Values
period	3	1 2 3
campaign	2	1 2

Dimensions

Covariance Parameters	6
Columns in X	12
Columns in Z	0
Subjects	10
Max Obs Per Subject	3
Observations Used	30
Observations Not Used	0
Total Observations	30

Iteration History

Iteration	Evaluations	-2 Res Log Like	Criterion
0	1	347.69129449	
1	1	256.26815630	0.00000000

Convergence criteria met.

Covariance Parameter Estimates

Cov Parm	Subject	Estimate	Alpha	Lower	Upper
UN(1,1)	ident	75290	0.05	34350	276326
UN(2,1)	ident	79440	0.05	1502.45	157377
UN(2,2)	ident	84197	0.05	38414	309017
UN(3,1)	ident	72731	0.05	1410.04	144051
UN(3,2)	ident	76682	0.05	1373.22	151990
UN(3,3)	ident	70440	0.05	32138	258527

Fit Statistics

-2 Res Log Likelihood	256.3
AIC (smaller is better)	268.3
AICC (smaller is better)	273.2
BIC (smaller is better)	270.1

Null Model Likelihood Ratio Test

DF	Chi-Square	Pr > ChiSq
5	91.42	<.0001

Type 3 Tests of Fixed Effects

Effect	Num DF	Den DF	F Value	Pr > F
period	2	8	54.03	<.0001
campaign	1	8	0.73	0.4166
period*campaign	2	8	2.94	0.1101

Least Squares Means

Effect	period	Estimate	Standard Error	DF	t Value	Pr > t
period	1	648.40	86.7695	8	7.47	<.0001
period	2	728.80	91.7588	8	7.94	<.0001
period	3	616.40	83.9284	8	7.34	<.0001

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The Mixed Procedure

Differences of Least Squares Means

Effect	period	_period	Estimate	Standard Error	DF	t Value	Pr > t
period	1	2	-80.4000	7.7910	8	-10.32	<.0001
period	1	3	32.0000	5.1764	8	6.18	0.0003
period	2	3	112.40	11.2821	8	9.96	<.0001

Differences of Least Squares Means

Effect	period	_period	Adjustment	Adj P
period	1	2	Bonferroni	<.0001
period	1	3	Bonferroni	0.0008
period	2	3	Bonferroni	<.0001

```
/* finalwine.sas */
options linesize=79 pagesize=100 noovp formdlim='_';
title 'STA442F05 Final Exam: Wine tasting data from NWK p. 1169';

data wine;
  infile 'wine.dat' firstobs=2; /* Skip the first line (header) */
  input Judge Wine Rating;

proc means mean stddev;
  class wine;
  var rating;

proc mixed;
  class wine;
  model rating = wine;
  repeated / type = cs subject = judge;
  lsmeans wine / adjust=bon;
```

finalwine.lst

STA442F05 Final Exam: Wine tasting data from NWK p. 1169 1
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The MEANS Procedure

Analysis Variable : Rating

Wine	N Obs	Mean	Std Dev
1	6	20.0000000	3.7416574
2	6	22.0000000	3.1622777
3	6	26.6666667	2.6583203
4	6	26.0000000	2.6076810

STA442F05 Final Exam: Wine tasting data from NWK p. 1169 2
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The Mixed Procedure

Model Information

Data Set	WORK.WINE
Dependent Variable	Rating
Covariance Structure	Compound Symmetry
Subject Effect	Judge
Estimation Method	REML
Residual Variance Method	Profile
Fixed Effects SE Method	Model-Based
Degrees of Freedom Method	Between-Within

Class Level Information

Class	Levels	Values
Wine	4	1 2 3 4

Iteration History

Iteration	Evaluations	-2 Res Log Like	Criterion
0	1	108.88011634	
1	1	82.62155007	0.00000000

Convergence criteria met.

Covariance Parameter Estimates

Cov Parm	Subject	Estimate
CS	Judge	8.4000
Residual		1.0667

Fit Statistics

-2 Res Log Likelihood	82.6
AIC (smaller is better)	86.6
AICC (smaller is better)	87.3
BIC (smaller is better)	86.2

Null Model Likelihood Ratio Test

DF	Chi-Square	Pr > ChiSq
1	26.26	<.0001

Type 3 Tests of Fixed Effects

Effect	Num DF	Den DF	F Value	Pr > F
Wine	3	15	57.50	<.0001

Least Squares Means

Effect	Wine	Estimate	Standard Error	DF	t Value	Pr > t
Wine	1	20.0000	1.2561	15	15.92	<.0001
Wine	2	22.0000	1.2561	15	17.51	<.0001
Wine	3	26.6667	1.2561	15	21.23	<.0001
Wine	4	26.0000	1.2561	15	20.70	<.0001

Differences of Least Squares Means

Effect	Wine	_Wine	Estimate	Standard Error	DF	t Value	Pr > t	Adjustment
Wine	1	2	-2.0000	0.5963	15	-3.35	0.0043	Bonferroni
Wine	1	3	-6.6667	0.5963	15	-11.18	<.0001	Bonferroni
Wine	1	4	-6.0000	0.5963	15	-10.06	<.0001	Bonferroni
Wine	2	3	-4.6667	0.5963	15	-7.83	<.0001	Bonferroni
Wine	2	4	-4.0000	0.5963	15	-6.71	<.0001	Bonferroni
Wine	3	4	0.6667	0.5963	15	1.12	0.2811	Bonferroni

The Mixed Procedure

Differences of Least
Squares Means

Effect	Wine	_Wine	Adj P
Wine	1	2	0.0261
Wine	1	3	<.0001
Wine	1	4	<.0001
Wine	2	3	<.0001
Wine	2	4	<.0001
Wine	3	4	1.0000